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Effective Field Theory Approach Flavour and Dark Matter

CERN

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Outline:

Introduction: Higher Dimensional Operators Lepton Flavour Violation Effects of gauge invariant dim-6 operators - Determination of the V_{ub} and V_{cb} Can NP explain the differences in the determinations Dark Matter detection Spin-independent cross section Dim 5 Dim 6 Dim 7 Conclusions

Introduction

Higher dimensional operators

- NP at the scale A>v must be invariant under the SM gauge group
- The heavy degrees of freedom can be integrated out T. Appelquist, J. Carazzone

The resulting effective operators must be Lorentz invariant, respect the SM gauge group and are suppressed by powers of 1/Λ.

B. Grzadkowski et al., arXiv:1008.4884 W. Buchmüller, D. Wyler, Nucl.Phys. B268 (1986) 621-653

Why EFT methods:

- Argue indecently of the specific NP model
 Properly connect physics at different scales via
 - Running
 - Mixing
 - Matching
- Correlate different experiments (complementarily of searches)
- Can be easily extended to account for DM, righthanded neutrinos, ...

Operator classification $L_{SM} = L_{SM}^{(4)} + 1/\Lambda \sum_{k} C_{k}^{(5)} Q_{k}^{(5)} + 1/\Lambda^{2} \sum_{k} C_{k}^{(6)} Q_{k}^{(6)} + O(1/\Lambda^{3})$ **Dim 5: 1 operator, the Weinberg operator** $Q_{\nu\nu} = \varepsilon_{jk} \varepsilon_{mn} \varphi^{j} \varphi^{m} (\ell_{p}^{k})^{T} C l_{r}^{n} = (\varphi^{\dagger} l_{p})^{T} C (\varphi^{\dagger} \ell_{r})$

- Dim 6: 59 operators
 - 30 four-fermion operators $Q_{le} = (\overline{\ell}_p \gamma_\mu \ell_r) (\overline{e}_s \gamma^\mu e_t)$
 - 4 pure field-strength tensor operators $Q_G = f^{ABC} G^{A\nu}_{\mu} G^{B\rho}_{\nu} G^{C\mu}_{\rho}$
 - 3 SM-scalar-doublet operators $Q_{\varphi} = (\varphi \varphi^{\dagger})^3$
 - 8 Higgs-field-strength operators $Q_{\varphi G} = \varphi^{\dagger} \varphi G_{\mu\nu}^{A} G^{A\mu\nu}$
 - **3 Higgs-fermion operators** $Q_{\varphi e} = \varphi^{\dagger} \varphi \overline{\ell}_{i} \varphi e_{j}$
 - 8 "magnetic" operators $Q_{eB} = \overline{\ell}_i \sigma_{\mu\nu} e_j \varphi B^{\mu\nu}$
 - 8 Higgs-fermion-derivative $Q_{\varphi\ell}^{(1)} = \varphi^{\dagger} D_{\mu} \varphi \overline{\ell}_{i} \gamma^{\mu} \ell_{j}$

General procedure

- Perform EW symmetry breaking
- Derive the Feynman rules
- Calculate the Feynman diagrams
- Perform the matching (integrate out W,Z, t and h)
- RGE evolution to the low scale
- Calculation of decay width, cross sections, etc.

Lepton Flavour Violation with dim-6 operators

A.C., S. Najjari, J. Rosiek, arXiv:1312.0632 A.C., M. Hoferichter, M. Procura, arXiv:1404.7134

Lepton flavour violation

In the SM (with massive neutrinos) lepton flavour violations is extremely suppressed by the small neutrino masses: $O(10^{-52})$

Any observation of LFV would establish physics beyond the SM.

- Current best limits on $\mu \rightarrow e$ transitions (from PSI):
 - $\operatorname{Br}[\mu \to e\gamma] \le 5.7 \times 10^{-13}$
 - $\operatorname{Br}[\mu \to eee] \le 1 \times 10^{-12}$
 - $\operatorname{Br}_{\operatorname{Au}}^{\operatorname{conv}}\left[\mu \to e\right] \leq 7 \times 10^{-13}$
- Future prospects: $Br[\mu \rightarrow e\gamma] \leq 6 \times 10^{-14}$ PSI $Br_{Al}^{conv}[\mu \rightarrow e] \leq 5 \times 10^{-17}$ FNAL, J-PARC $Br[\mu \rightarrow eee] \leq 7 \times 10^{-17}$ PSI (proposed)

Observabels

Contributions of dim-6 operators to

- $\ell \rightarrow \ell' \gamma$ (one loop)
- $\tau \to \mu \mu \mu, \tau \to e \mu \mu$, etc.
- EDM, AMM (one loop)
- $Z \to \ell \ell'$
- $\mu \rightarrow e$ conversion

At leading loop-order and at leading order in $1/\Lambda^2$ and m_{ℓ}/m_W

Operators for LFV

llll		$\ell\ell X \varphi$		$\ell\ell \varphi^2 D$ and $\ell\ell \varphi^3$	
$Q_{\ell\ell}$	$(ar{\ell}_i\gamma_\mu\ell_j)(ar{\ell}_k\gamma^\mu\ell_l)$	Q_{eW}	$(ar{\ell}_o\sigma^{\mu u}e_j) au^Iarphi W^I_{\mu u}$	$Q^{(1)}_{arphi\ell}$	$(arphi^\dagger i\overleftrightarrow{D}_\muarphi)(ar{\ell}_i\gamma^\mu\ell_j)$
Q_{ee}	$(ar{e}_i\gamma_\mu e_j)(ar{e}_k\gamma^\mu e_l)$	Q_{eB}	$(ar{\ell}_i\sigma^{\mu u}e_j)arphi B_{\mu u}$	$Q^{(3)}_{arphi\ell}$	$(arphi^\dagger i \overset{\leftrightarrow}{D}{}^I_\mu arphi) (ar{\ell}_i au^I \gamma^\mu \ell_j)$
$Q_{\ell e}$	$(ar{\ell}_i\gamma_\mu\ell_j)(ar{e}_k\gamma^\mu e_l)$			$Q_{arphi e}$	$(arphi^\dagger i\overleftrightarrow{D}_\muarphi)(ar{e}_i\gamma^\mu e_j)$
				$Q_{earphi 3}$	$(arphi^{\dagger}arphi)(ar{\ell}_i e_j arphi)$
$\ell \ell q q$					
$Q^{(1)}_{\ell q}$	$(ar{\ell}_i\gamma_\mu\ell_j)(ar{q}_k\gamma^\mu q_l)$	$Q_{\ell d}$	$(ar{\ell}_i\gamma_\mu\ell_j)(ar{d}_k\gamma^\mu d_l)$	$Q_{\ell u}$	$(ar{\ell}_i\gamma_\mu l_j)(ar{u}_k\gamma^\mu u_l)$
$Q_{\ell q}^{(3)}$	$(ar{\ell}_i\gamma_\mu au^I\ell_j)(ar{q}_k\gamma^\mu au^Iq_l)$	Q_{ed}	$(ar{e}_i\gamma_\mu e_j)(ar{d}_k\gamma^\mu d_l)$	Q_{eu}	$(ar{e}_i\gamma_\mu e_j)(ar{u}_k\gamma^\mu u_l)$
Q_{eq}	$(ar{e}_i\gamma^\mu e_j)(ar{q}_k\gamma_\mu q_l)$	$Q_{\ell e d q}$	$(ar{\ell}^a_i e_j)(ar{d}_k q^a_l)$	$Q_{\ell equ}^{(1)}$	$(ar{\ell}^a_i e_j)arepsilon_{ab}(ar{q}^b_k u_l)$
				$Q^{(3)}_{\ell equ}$	$(ar{\ell}^a_i\sigma_{\mu u}e_a)arepsilon_{ab}(ar{q}^b_k\sigma^{\mu u}u_l)$

- ℓ : left-handed lepton doublet e: right-handed charged lepton φ : SM-Scalar doublet $W^{\mu\nu}$: SU(2) field-strength tensor $B^{\mu\nu}$: U(1) field-strength tensor
- *i*, *j*, *k*, *l* : flavour indices \vec{D}_{μ} : covariant derivative

Derivation of the modified Feynman rules

After EW symmetry breaking
 General R_x gauge

Example: Z-lepton coupling

$$\begin{array}{l} \left| \ell_{i} \\ Z^{\mu} \xrightarrow{q \rightarrow} \ell_{f} \end{array} \right|^{\ell_{i}} & i \left(\gamma^{\mu} \left[\Gamma_{fi}^{ZL} P_{L} + \Gamma_{fi}^{ZR} P_{R} \right] + i \sigma^{\mu\nu} \left[C_{fi}^{ZL} P_{L} + C_{fi}^{ZR} P_{R} \right] q_{\nu} \right) \\ \Gamma_{fi}^{ZL} = \frac{e}{2s_{W}c_{W}} \left(\frac{v^{2}}{\Lambda^{2}} \left(C_{\phi\ell}^{(1)fi} + C_{\phi\ell}^{(3)fi} \right) + \left(1 - 2s_{W}^{2} \right) \delta_{fi} \right) \\ \Gamma_{fi}^{ZR} = \frac{e}{2s_{W}c_{W}} \left(\frac{v^{2}}{\Lambda^{2}} C_{\phi e}^{fi} - 2s_{W}^{2} \delta_{fi} \right) \\ C_{fi}^{ZR} = C_{if}^{ZL\star} = -\frac{v\sqrt{2}}{\Lambda^{2}} \left(s_{W}C_{eB}^{fi} + c_{W}C_{eW}^{fi} \right) \end{array}$$

Calculation of the diagrams



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 Gauge invariant structure of the operators
 R_x gauge $F_{TL}^{WG fi} = -\frac{10em_f C_{\varphi\ell}^{(3)fi}}{3(4\pi)^2}$ $F_{TR}^{WG fi} = -\frac{10em_i C_{\varphi\ell}^{(3)fi}}{3(4\pi)^2}$

$$F_{TL}^{4\ell fi} = \frac{2e}{(4\pi)^2} \sum_{j=1}^{3} C_{\ell e}^{fjji} m_j$$
$$F_{TR}^{4\ell fi} = \frac{2e}{(4\pi)^2} \sum_{j=1}^{3} C_{\ell e}^{jifj} m_j$$

 $\mathsf{Br}\left[\ell_i \to \ell_f \gamma\right] = \frac{m_{\ell_i}^3}{16\pi\Lambda^4 \,\Gamma_{\ell_i}} \left(\left|F_{TR}^{fi}\right|^2 + \left|F_{TL}^{fi}\right|^2\right)$

 $F_{TL}^{ZG fi} = \frac{4e \left[\left(C_{\varphi \ell}^{(1)fi} + C_{\varphi l}^{(3)fi} \right) m_f (1 + s_W^2) - C_{\varphi e}^{fi} m_i (\frac{3}{2} - s_W^2) \right]}{3(4\pi)^2}$

 $F_{TR}^{ZG fi} = \frac{4e \left[\left(C_{\varphi \ell}^{(1)fi} + C_{\varphi l}^{(3)fi} \right) m_i (1 + s_W^2) - C_{\varphi e}^{fi} m_f (\frac{3}{2} - s_W^2) \right]}{3(4\pi)^2}$

$$\begin{split} F_{TL}^{ql\ fi} &= -\frac{16e}{3(4\pi)^2} \sum_{j=1}^3 C_{\ell equ}^{(3)fijj\star} m_{u_j} \left(\Delta - \log \frac{m_{u_j}^2}{\mu^2} \right) \\ F_{TR}^{ql\ fi} &= -\frac{16e}{3(4\pi)^2} \sum_{j=1}^3 C_{\ell equ}^{(3)fijj} m_{u_j} \left(\Delta - \log \frac{m_{u_j}^2}{\mu^2} \right) \end{split}$$

Numerical results



$$\tau \rightarrow eee$$



$\mu \rightarrow e$ conversion



Determination of V_{ub} and V_{cb}

A.C., Stefan Pokorski, arXiv:1407.1320

Different determinations

■ V_{cb} | V_{cb} |= (4.242±0.086)×10⁻² (inclusive) | V_{cb} |= (3.904±0.075)×10⁻² ($B \rightarrow D^* \ell \nu$) | V_{cb} |= (3.850±0.191)×10⁻² ($B \rightarrow D \ell \nu$)



• V_{ub} $|V_{ub}| = (4.41^{+0.21}_{-0.23}) \times 10^{-3}$ (inclusive) $|V_{ub}| = (3.40^{+0.38}_{-0.33}) \times 10^{-3}$ ($B \to \pi \ell \nu$) $|V_{ub}| = (4.3 \pm 0.6) \times 10^{-3}$ ($B \to \tau \nu$) $|V_{ub}| = (3.4 \pm 0.3) \times 10^{-3}$ ($B \to \rho \ell \nu$)



Effective operators (at the B scale)

B. Dassinger et al. arXiv:0803.3561, S. Faller et al. arXiv:1105.3679

Four-fermion operators

 $O_{R}^{S} = \overline{\ell} P_{L} v \overline{q} P_{R} b$ $O_{L}^{S} = \overline{\ell} P_{L} v \overline{q} P_{L} b$ $O_{L}^{T} = \overline{\ell} \sigma_{\mu\nu} P_{L} v \overline{q} \sigma^{\mu\nu} P_{L} b$ Contribute

 $\sim |C_L^T|^2 \quad \text{all decays}$ $\sim |C_R^S + C_L^S|^2 \quad B \to D(\pi)\ell \nu$ $\sim |C_R^S - C_L^S|^2 \quad B \to D^*(\rho)\ell \nu$ $\sim |C_R^S|^2 + |C_L^S|^2 \text{ inclusive}$

Cannot explain the differences in the determinations

Modified W coupling

 $H_{eff} = \frac{4G_F V_{qb}}{\sqrt{2}} \overline{\ell} \gamma^{\mu} P_L v \left((1 + c_L^{qb}) \overline{q} \gamma_{\mu} P_L b + g_L^{qb} \overline{q} i \vec{D}_{\mu} P_L b + d_L^{qb} i \partial^{\nu} \left(\overline{q} i \sigma_{\mu\nu} P_L b \right) + L \to R \right)$

Effects of NP

Exclusive determination at zero recoil: V_{cb}

$$V_{cb} = \frac{V_{cb}^{SM}}{1 + c_{L}^{cb} + c_{R}^{cb} - 1.6 \text{GeV}(d_{R}^{cb} + d_{L}^{cb}) + 5.5 \text{GeV}(g_{R}^{cb} + g_{L}^{cb})} (B \to D\ell\nu)$$

$$V_{cb} = \frac{V_{cb}^{SM}}{1 + c_{L}^{cb} - c_{R}^{cb} + 3.3 \text{GeV}(d_{R}^{cb} - d_{L}^{cb})} (B \to D^{*}\ell\nu)$$

$$V_{ub} = \frac{V_{ub}^{SM}}{1 + c_{L}^{ub} + c_{R}^{ub} - 4.9 \text{GeV}(d_{R}^{ub} + d_{L}^{ub}) + 5.5 \text{GeV}(g_{R}^{ub} + g_{L}^{ub})} (B \to \pi\ell\nu)$$

$$V_{ub} = \frac{V_{ub}^{SM}}{1 + c_{L}^{ub} - c_{R}^{ub} + 4.5 \text{GeV}(d_{R}^{ub} - d_{L}^{ub})} (B \to \rho\ell\nu)$$

Inclusive determination on weakly affected

New Physics Effects in V_{cb}

Right-handed W coupling

"magnetic" operator





New Physics Effects in V_{ub}

Right-handed W coupling

"magnetic" operator









Side remark: Right-handed W-coupling in the MSSM

A.C. arXiv:0907.2461

Genuine vertexcorrection



$$-i\Lambda_{u_{f}d_{i}}^{W\,\tilde{g}} = \frac{g_{2}}{\sqrt{2}}\frac{i\alpha_{s}}{3\pi}\gamma^{\mu}\sum_{s,t=1}^{6}\sum_{j,k=1}^{3}\binom{W_{fs}^{\tilde{u}}W_{ks}^{\tilde{u}*}V_{kj}^{CKM}W_{jt}^{\tilde{d}}W_{it}^{\tilde{d}*}P_{L}}{+W_{f+3,s}^{\tilde{u}}W_{ks}^{\tilde{u}*}V_{kj}^{CKM}W_{jt}^{\tilde{d}}W_{i+3,t}^{\tilde{d}}P_{R})C_{2}\left(m_{\tilde{u}_{s}},m_{\tilde{d}_{t}},m_{\tilde{g}}\right)$$

 Corrections to the left-handed coupling suppressed because the hermitian part of the WFR cancels with the genuine vertex correction.

Right-handed coupling not suppressed!

Where are SUSY effects possible?

- \$\delta_{\mathcal{fi}}^{d \LR/RL}\$ strongly constrained from FCNC processes.
 \$\delta_{\mathcal{fi}}^{u \LR}\$ less constrained from FCNCs \$(B \rightarrow K^* \mu^+ \mu^-)\$)\$
 \$\delta_{\mathcal{1}2,21}^{u \LR, \LL, \RR}\$ constrained from D mixing
- $\delta_{13,23}^{u RL}$ unconstrained from FCNCs
- Large $\delta_{33}^{d LR}$ possible if A^b or tan(β) is large.
- V_{ud} , V_{us} , V_{cd} , V_{cs} are to large for observable effects

\longrightarrow Only V_{ub}, V_{cb} can be affected by SUSY effects.

Largest SUSY effect in V_{ub} possible.



Results

 In terms of SU(2) invariant operators d_L corresponds to

 $Q_{uW}^{ij} = 1 / \Lambda^2 \left(\overline{q}_i \sigma^{\mu\nu} u_j \right) \tau^I \tilde{\varphi} W_{\mu\nu}^I$

Direct connection to Z-quark couplings

Excluded order one corrections to Z-bb couplings

NP at the scale Λ cannot explain the differences in the determinations of V_{ub} and V_{cb}.

Effective field theory approach to Dark Matter

A.C., F. d'Eramo, M. Procura, arXiv:1402.1173 A.C., M. Hoferichter, M. Procura arXiv:1312.4951 A.C., U. Haisch, arXiv:1408:5046

Spin independent scattering cross section Up to Dim 7 (at the direct detection scale)

$$\sigma_N^{\text{SI}} \approx \frac{m_N^2}{\pi \Lambda^4} \left| \sum_{q=u,d} C_{qq}^{VV} f_{V_q}^N + \frac{m_N}{\Lambda} \left(\sum_{q=u,d,s} C_{qq}^{SS} f_q^N - 12\pi C_{gg}^S f_Q^N \right) \right|^2$$

$$L_{eff} = \sum_{X} C_{X} O_{X}$$

$$O_{gg}^{S} = \frac{\alpha_{s}}{\Lambda^{3}} \,\overline{\chi} \,\chi G_{\mu\nu} G^{\mu}$$

$$O_{qq}^{SS} = \frac{m_q}{\Lambda^3} \,\overline{\chi} \,\chi \,\overline{q} q$$

$$O_{qq}^{VV} = \frac{1}{\Lambda^2} \,\overline{\chi} \gamma^{\mu} \chi \overline{q} \,\gamma_{\mu} q$$

 f^N : nucleon couplings m_N : nucleon mass

The Wilson coefficients C_X must be connected to UV physics

Scalar quark content of the nucleon

Tradiational approach: SU(3) chiral pertubation Better: SU(2) chiral pertubation theory and f_s from lattice



EFT for Dark Matter

We assume that DM is:

- A SM singlet (other choices are also possible)
- A Dirac fermion (biggest number of operators)
- Interactions of DM with the SM arise through messengers at a high scale Λ
- Construct operators which are invariant under the SM gauge group
- This scale A must be connected to the direct detection scale via running, mixing and threshold effects.

Operators dim-5 $O_{M}^{T} = \frac{1}{\Lambda} \overline{\chi} \sigma^{\mu\nu} \chi B_{\mu\nu}, \quad O_{HH}^{S} = \frac{1}{\Lambda} \overline{\chi} \chi H^{\dagger} H, \quad O_{HH}^{P} = \frac{1}{\Lambda} \overline{\chi} \gamma^{5} \chi H^{\dagger} H$ $O_M^T :$ Tree-level contribution to direct detection • $O_{\mu\mu}^{P}$: Affects only spin dependent direct detection \circ O_{HH}^{S} : Enters only via matching corrections Matching: $C_{gg}^{S} = \frac{1}{12\pi} \frac{\Lambda^2}{m_{10}^2} C_{HH}^{S}$ $C_{qq}^{SS} = -\frac{\Lambda^2}{m_{\odot}^2} C_{HH}^S \qquad \bar{\chi}$ O_{HH}^S Mixing turns out to be small $C_{qq}^{SS}(\mu_0) = \left[\frac{1}{12\pi} \left(U_{m_b,m_t}^{(5)} + 2U_{\mu_0,m_b}^{(4)}\right) - 1 \left|\frac{\Lambda^2}{m_{.0}^2} C_{HH}^S\right] \chi$ $U_{\mu,\Lambda}^{(n_f)} = \frac{-3C_F}{\pi\beta} \ln \frac{\alpha_s(\Lambda)}{\alpha(\mu)}.$

$O_{qq}^{VV} = \frac{1}{\Lambda^2} \overline{\chi} \gamma^{\mu} \chi \, \overline{q} \gamma_{\mu} q$

- $O_{qq}^{VA} = \frac{1}{\Lambda^2} \overline{\chi} \gamma^{\mu} \chi \, \overline{q} \, \gamma_{\mu} q$
- $O^{V}_{\phi\phi D}=rac{i}{\Lambda^{2}}\,\overline{\chi}\,\gamma^{\mu}\chi\phi^{\dagger}ec{D}_{\mu}\phi$



No QCD effects

• EW-mixing of O_{qq}^{VA} into O_{HHD}^{V}

$$C_{\phi\phi D}^{V}(\mu) = C_{\phi\phi D}^{V}(\Lambda) - \frac{\alpha_{t}N_{c}}{\pi}C_{tt}^{VA}(\Lambda)\ln\frac{\mu}{\Lambda} - (t \to b)$$

Matching contributions

$$C_{uu}^{VV} \rightarrow C_{uu}^{VV} + \frac{1}{2}C_{HHD}^{V}, C_{dd}^{VV} \rightarrow C_{dd}^{VV} - \frac{1}{2}C_{HHD}^{V}$$

Bounds on previously unconstrained operators

Experimental constraints

$$C_{qq}^{VA} = 1$$



LHC

Operators dim-7

Field strength tensors especially interesting

 $O_B = \frac{1}{\Lambda^2} \,\overline{\chi} \chi B^{\mu\nu} B_{\mu\nu} \,, \quad O_W = \frac{1}{\Lambda^2} \,\overline{\chi} \chi W^{\mu\nu} W_{\mu\nu}$

Mixing into

$$O_{\phi}^{S} = \frac{1}{\Lambda^{3}} \overline{\chi} \chi \phi \phi^{\dagger} \phi \phi^{\dagger}$$
$$O_{qq}^{\phi} = \frac{Y^{q}}{\Lambda^{3}} \overline{\chi} \chi \overline{q} \phi q$$



Contributions to direct detection after EW symmetry breaking and integrating out the Higgs.

Constraints on C_{ww}

Interesting interplay between direct detection and LHC searches



Conclusions

- LVF is an excellent place to search for NP
 - $\mu \rightarrow e$ conversion sensitive to Higgs mediated flavour violation
- NP cannot explain the current differences in the determination of V_{ub} and V_{cb}
- Interesting loop effects in DM direct detections: new constraints on operators
- EFT provide a consistent framework to search for NP in a model independent way