

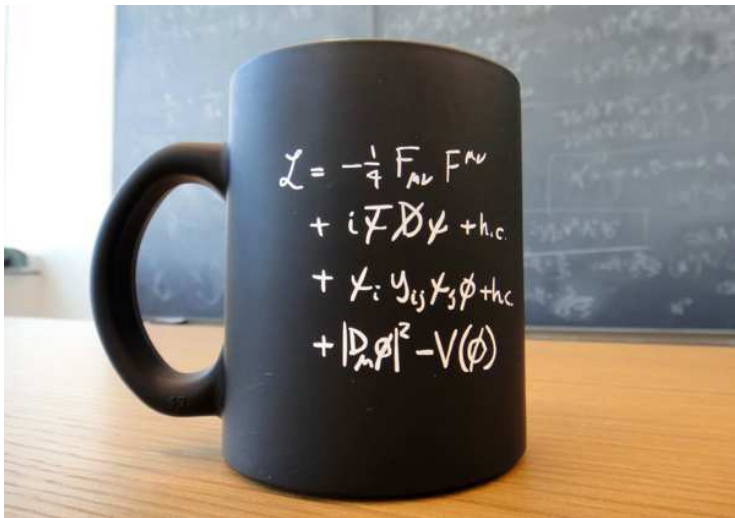
Neutrinos and Abelian Gauge Symmetries

Julian Heeck

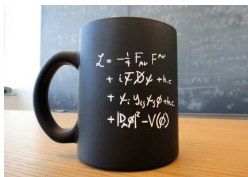
24.10.2014 – ULB

Standard Model of Particle Physics

Beautiful and simple:



Standard Model of Particle Physics



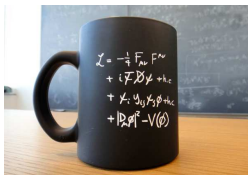
Not shown:

- Gauge group $SU(3)_{\text{color}} \times SU(2)_{\text{isospin}} \times U(1)_{\text{hypercharge}}$;
 $\Rightarrow 8 + 3 + 1$ **spin-1** bosons with field strength $F_{\mu\nu}$,
- Three copies of **spin- $\frac{1}{2}$** Weyl fields (families/generations) in rep.

$$\Psi_{1,2,3} \sim \underbrace{(\mathbf{3}, \mathbf{2}, \frac{1}{6}) \oplus (\mathbf{3}, \mathbf{1}, -\frac{2}{3}) \oplus (\mathbf{3}, \mathbf{1}, \frac{1}{3})}_{\text{quarks}} \oplus \underbrace{(\mathbf{1}, \mathbf{2}, -\frac{1}{2}) \oplus (\mathbf{1}, \mathbf{1}, 1)}_{\text{leptons}}$$

- One complex **spin-0** field $\phi \sim (\mathbf{1}, \mathbf{2}, -\frac{1}{2})$ which breaks $SU(2) \times U(1) \rightarrow U(1)_{\text{EM}}$ via $\langle \phi \rangle \simeq 250 \text{ GeV}$.
- About **18 free parameters**, all measured as of 2013 (Brout–Englert–Higgs boson mass).

Standard Model of Particle Physics



Also not shown (because beyond SM):

- Neutrinos have mass and mix.
- Dark matter.
- Baryon asymmetry of our Universe.

Symmetries of the Standard Model

- \mathcal{L}_{SM} renormalizable \Rightarrow only mass dimension ≤ 4 couplings.
- \mathcal{L}_{SM} invariant under phase shifts of quarks and individual leptons.

$U(1)^4$: B , L_e , L_μ , and L_τ classically conserved in the Standard Model.

- Nonperturbative instanton/sphaleron solutions break $\Delta(B + L) = 6$.

$U(1)_{B-L} \times U(1)_{L_e-L_\mu} \times U(1)_{L_\mu-L_\tau}$ *global* symmetry of quantum SM.

- After introducing three right-handed neutrinos ν_R :

$U(1)_{B-L} \times U(1)_{L_e-L_\mu} \times U(1)_{L_\mu-L_\tau}$ anomaly free *local* symmetry.¹

(Neutrinos automatically massive due to ν_R .)

Breaking \Rightarrow neutrino nature, hierarchies, mixing, baryon asymmetry,...

¹J.H., T. Araki, J. Kubo, JHEP **1207** (2012) [arXiv:1203.4951].

Outline

Neutrinos and abelian gauge symmetries

$$\underbrace{U(1)_{B-L} \times U(1)_{L_e-L_\mu} \times U(1)_{L_\mu-L_\tau}}_{\text{unflavored}} \underbrace{\hspace{10em}}_{\text{dark}} \cdot$$

Typically simple models:

- Few new particles and parameters.
- Renormalizable.
- Z' gives additional pheno.

Baryon and Lepton Number

- B and L classically conserved in the Standard Model.
- $B + L$ theoretically broken non-perturbatively: $\Delta(B + L) = 6$.
- $B - L$ *globally* conserved.

Fate of fundamental $U(1)_{B-L}$ from **experiments**.

Linked to neutrino nature and matter–antimatter asymmetry.

- $B - L$ *locally* conserved after adding three ν_R .
⇒ Neutrinos massive!

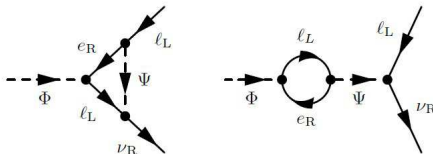
Three possibilities for (local) $U(1)_{B-L}$:

1. **Unbroken $B - L$** : Dirac neutrinos + leptogenesis.
2. **Majorana $B - L$** : $\Delta(B - L) = 2$, Majorana ν + leptogenesis.
3. **Dirac $B - L$** : $\Delta(B - L) = n \neq 2$, Dirac ν + Dirac leptogenesis.

Unbroken $B - L$

Almost² never considered, but very simple:³

- Neutrinos are Dirac, with Yukawa couplings $Y_\nu \sim m_\nu / \langle H \rangle \lesssim 10^{-11}$.
- Baryon asymmetry via **neutrino**genesis:⁴
 - New heavy scalar doublets decay so that $\Delta(B - L) = \Delta L = 0$, but $\Delta L_{\text{left}} = -\Delta L_{\text{right}} \neq 0$.



- Right-handed ν_R **not thermalized** due to tiny Yukawas.
 \Rightarrow Sphalerons only see ΔL_{left} , generate ΔB via $\Delta(B + L) = 6!$

²D. Feldman, P. Fileviez Perez, and P. Nath, arXiv:1109.2901.

³J.H., arXiv:1408.6845.

⁴K. Dick, M. Lindner, M. Ratz, and D. Wright, arXiv:hep-ph/9907562.

Signatures

- No $0\nu 2\beta$ or other $\Delta(B - L) \neq 0$ processes. . .
- Z' with tiny coupling $\alpha' \lesssim 10^{-50}$ or Stückelberg mass $M_{Z'}$:
 - Introduce *real* scalar σ with gauge trafo $\sigma \rightarrow \sigma + M_{Z'}\theta(x)$.

$$\Delta\mathcal{L} = \frac{1}{2} (M_{Z'} Z'^{\mu} + \partial^{\mu}\sigma) (M_{Z'} Z'_{\mu} + \partial_{\mu}\sigma)$$

is gauge invariant ($Z'_{\mu} \rightarrow Z'_{\mu} - \partial_{\mu}\theta$).

- Mass term $\frac{1}{2} M_{Z'}^2 Z'_{\mu} Z'^{\mu}$ is just gauge **fixing**, not **breaking**.

Abelian gauge bosons can have a mass without symmetry breaking.

- $M_{Z'}/g'$ not connected to m_{ν} or leptogenesis \Rightarrow no preferred scale!
- Limits from modified gravity, stellar energy losses, scattering/collider experiments, and Big Bang nucleosynthesis ($\bar{\nu}_R \gamma^{\mu} \nu_R Z'_{\mu}$).

\Rightarrow **Unbroken (local) $B - L$ perfectly valid!**⁵

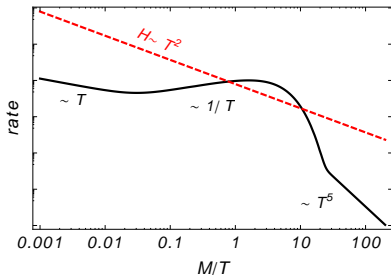
⁵J.H., arXiv:1408.6845.

Big Bang Nucleosynthesis

- ν_R are light (Dirac neutrinos) $\rightarrow N_{\text{eff}} \simeq 6$ for strong Z' interactions.
- Light Z' also contributes to N_{eff} .
- BBN ($T \sim 1$ MeV) limit: $N_{\text{eff}} < 4$ at 95% C.L.⁶

Thermally averaged rate via Z' :

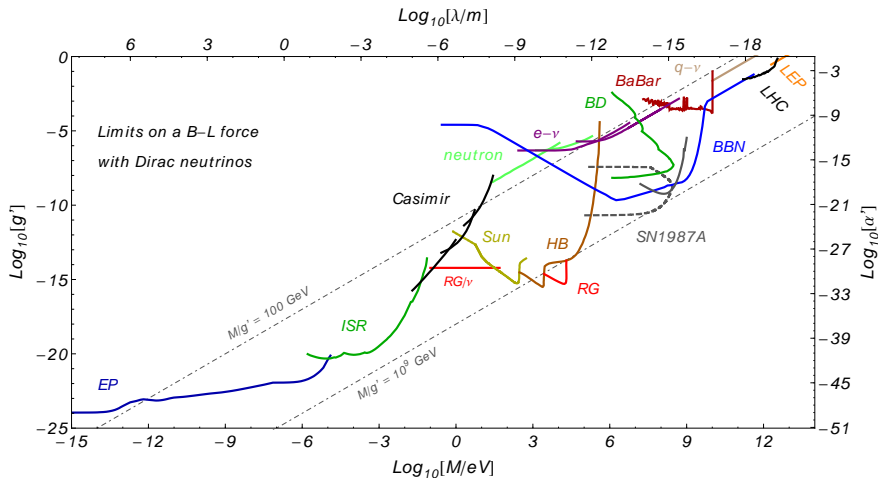
$$\langle \Gamma(\bar{f}f \leftrightarrow \bar{\nu}_R \nu_R) \rangle \propto \begin{cases} g'^4 T, & M_{Z'} \ll T, \\ g'^2 \frac{M_{Z'}^2}{T}, & M_{Z'} \lesssim T, \\ \frac{g'^4}{M_{Z'}^4} T^5, & M_{Z'} \gg T. \end{cases}$$



- Demand $\langle \Gamma(\bar{f}f \leftrightarrow \bar{\nu}_R \nu_R) \rangle < H(T) \sim T^2/M_{\text{Pl}}$ “at” BBN.

⁶Mangano, Serpico, PLB (2011), [arXiv:1103.1261].

The Money Shot



Applicable to any Z'_{B-L} (BBN, RG/ν , solid SN1987 depend on number of light ν_R).⁷

⁷J.H., arXiv:1408.6845.

Majorana $B - L$

- New scalar $\phi_{B-L=2}$ to break $U(1)_{B-L}$ by two units.

$$\mathcal{L} \supset Y_\nu \bar{\nu}_R H L + \frac{1}{2} Y_R \bar{\nu}_R \nu_R^c \phi_{B-L=2}^* + \text{h.c.}$$

- Spontaneous symmetry breaking gives mass matrix for (ν_L, ν_R^c) :

$$\mathcal{M} = \begin{pmatrix} 0 & Y_\nu^T \langle H \rangle \\ Y_\nu \langle H \rangle & Y_R \langle \phi_{B-L=2} \rangle \end{pmatrix}.$$

- High scale $Y_R \langle \phi_{B-L=2} \rangle \gg Y_\nu \langle H \rangle$:
small seesaw Majorana mass for active neutrinos:

$$\mathcal{M}_\nu \simeq - \frac{\langle H \rangle^2}{\langle \phi_{B-L=2} \rangle} Y_\nu^T Y_R^{-1} Y_\nu.$$

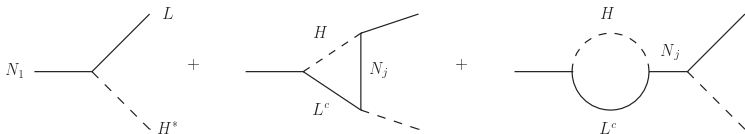
- Signature of Majorana $B - L$: neutrinoless double beta decay

$$(A, Z) \rightarrow (A, Z + 2) + 2e^- \quad \Leftrightarrow \quad \Delta(B - L) = 2.$$

Majorana $B - L$: Leptogenesis

$$\mathcal{L} \supset Y_\nu \bar{\nu}_R H L + \frac{1}{2} Y_R \bar{\nu}_R \nu_R^c \phi_{B-L=2}^* + \text{h.c.}$$

- Heavy ($\mathcal{M}_R \simeq Y_R \langle \phi_{B-L=2} \rangle \gtrsim 10^8 \text{ GeV}$) Majorana neutrinos $N = \nu_R + \nu_R^c$ decay out-of-equilibrium in early Universe.



- If CP violated in loops: $\Gamma(N \rightarrow HL) \neq \Gamma(N \rightarrow H^* \bar{L})$
 \Rightarrow Lepton asymmetry Δ_L !
- Sphalerons with $\Delta B = \Delta L = 3$ above $T \gtrsim \text{TeV}$ transfer Δ_L to baryon asymmetry Δ_B .

Dirac $B - L$

Break $B - L$, but by $n \neq 2$ units.⁸

⇒ Lepton number violating Dirac neutrinos.

- All fermions in $SM + \nu_R$ are odd under $B - L$
 ⇒ only **even** $\Delta(B - L)$ possible.
 ⇒ Lowest order new processes: $\Delta(B - L) = 4$:

$$\mathcal{O}_{d=6} : \bar{\nu}_R^c \nu_R \bar{\nu}_R^c \nu_R$$

$$\mathcal{O}_{d=8} : |H|^2 \bar{\nu}_R^c \nu_R \bar{\nu}_R^c \nu_R, (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) \bar{\nu}_R^c \nu_R, F_Y^{\mu\nu} \bar{\nu}_R^c \sigma_{\mu\nu} \nu_R \bar{\nu}_R^c \nu_R$$

$$\mathcal{O}_{d=10} : (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L), |H|^2 (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) \bar{\nu}_R^c \nu_R, \\ F_Y^{\mu\nu} (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) \bar{\nu}_R^c \sigma_{\mu\nu} \nu_R, W_a^{\mu\nu} (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger \tau^a L) \bar{\nu}_R^c \sigma_{\mu\nu} \nu_R, \\ (\bar{u}_R d_R^c)(\bar{d}_R \tilde{H}^\dagger L)(\bar{\nu}_R^c \nu_R), \dots$$

$$\mathcal{O}_{d=18} : (\bar{d}_R d_R^c \bar{u}_R u_R \bar{e}_R e_R)(\bar{d}_R d_R^c \bar{u}_R u_R \bar{e}_R e_R), \dots$$

$$\mathcal{O}_{d=20} : \left[\overline{((D_\mu L)^c \tilde{H})(H^\dagger D_\nu L)} \right]^2 \supset (\bar{e}_L^c W_\mu^+ W_\nu^+ e_L)(\bar{e}_L^c W^{+\mu} W^{+\nu} e_L), \dots$$

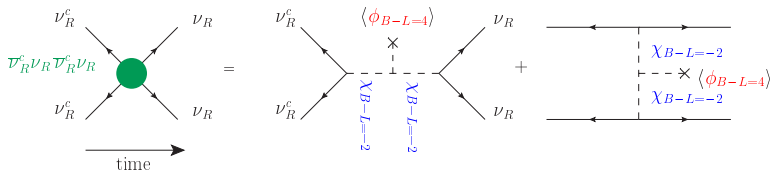
⁸Witten, hep-ph/0006332.

UV Completion

- One scalar $\phi_{B-L=4}$ to break $B - L$, one scalar $\chi_{B-L=-2}$ as mediator.

$$\mathcal{L} \supset y_{\alpha\beta} \bar{L}_\alpha H \nu_{R,\beta} + \kappa_{\alpha\beta} \chi_{B-L=-2} \bar{\nu}_{R,\alpha} \nu_{R,\beta}^c + \text{h.c.}$$

- Neutrinos are Dirac (and $\Delta L = 2$ forbidden) if $\langle \chi_{B-L=-2} \rangle = 0$.
- Scalar potential $V \supset \mu \phi_{B-L=4} (\chi_{B-L=-2})^2 + \text{h.c.}$
- Lepton number violation $\Delta L = 4$ still possible!⁹



- Extension to left-right model can enhance rates.

⁹J.H. and W. Rodejohann, EPL **103**, 32001 (2013) [arXiv:1306.0580].

Phenomenology of LNV Dirac Neutrinos

How to check for $\Delta L = 4$?

- Collider processes:
 - LHC: $pp \rightarrow W^- W^- W^- W^- \ell^+ \ell^+ \ell^+ \ell^+ + X$,
 - Like-sign lepton collider: $e^- e^- \rightarrow W^- W^- W^- W^- \ell^+ \ell^+$.
- Nuclear decays ($0\nu 4\beta?$).¹⁰
- Rare meson decays etc.?

All tough, many particles in final state! (Even harder for $\Delta L > 4$...)

$\Delta L = 4$ can however easily be relevant in the early Universe
 \Rightarrow new Dirac leptogenesis mechanism!¹¹

¹⁰J.H. and W. Rodejohann, EPL **103**, 32001 (2013) [arXiv:1306.0580].

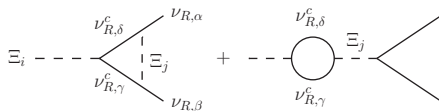
¹¹J.H., PRD **88**, 076004 (2013) [arXiv:1307.2241].

Dirac $B - L$: Leptogenesis

- Scalar potential $V(H, \phi, \chi) \supset -\mu \phi_{B-L=4} (\chi_{B-L=-2})^2$ breaks complex $\chi_{B-L=-2} = (\Xi_1 + i\Xi_2)/\sqrt{2}$ into two real scalars with mass

$$m_1^2 = m_c^2 - 2\mu \langle \phi_{B-L=4} \rangle, \quad m_2^2 = m_c^2 + 2\mu \langle \phi_{B-L=4} \rangle.$$

- Heavy mediator scalar Ξ_j decays to $\nu_R \nu_R$ or $\bar{\nu}_R \bar{\nu}_R$ out-of-equilibrium in early Universe.



- CP violation requires *second* scalar $\chi_{B-L=-2}$.

$$Y_{\nu_R} \equiv \frac{n_{\nu_R}}{s} \sim \frac{1}{g_*} \frac{\Gamma(\Xi_i \rightarrow \nu_R \nu_R) - \Gamma(\Xi_i \rightarrow \nu_R^c \nu_R^c)}{\Gamma(\Xi_i \rightarrow \nu_R \nu_R) + \Gamma(\Xi_i \rightarrow \nu_R^c \nu_R^c)}.$$

Asymmetry in ν_R . ✓ How to translate to baryon asymmetry?

Baryon Asymmetry

- Dirac-Yukawa coupling $Y_\nu = m_\nu / \langle H \rangle$ too small to equilibrate ν_R ...

Add second scalar doublet H_2 with large Yukawa $\bar{L}H_2\nu_R$:

- Neutrinophilic H_2 with small VEV $\langle H_2 \rangle \sim 1 \text{ eV}$.¹²
 \Rightarrow Dirac neutrinos light with large Yukawas.
- H_2 moves Y_{ν_R} to Y_{ν_L} .
- Sphalerons move Y_{ν_L} to Y_B .

\Rightarrow Different from **neutrinogenesis!**

- Necessary thermalization of $\nu_R \Rightarrow N_{\text{eff}} > 3!$
- $3.14 \lesssim N_{\text{eff}} \lesssim 3.29$ depending on H_2^+ mass and Yukawa coupling.
- Specific collider signatures of neutrinophilic H_2 .¹³

¹²E. Ma, PRL **86** (2001), F. Wang, W. Wang, J. M. Yang, EPL **76** (2006), S. Gabriel and S. Nandi, PLB **655** (2007).

¹³Davidson and Logan, PRD **80** (2009), arXiv:0906.3335.

Unflavored Summary

name	$\Delta(B - L)$	neutrino	BAU	signatures
Unbroken $B - L$	0	Dirac	neutrino genesis	$Z'(?), N_{\text{eff}} \simeq 3$
Majorana $B - L$	2	Majorana	leptogenesis	$0\nu 2\beta$
Dirac $B - L$	> 2 , e.g. 4	Dirac	Dirac leptogenesis	$0\nu 4\beta, N_{\text{eff}} \gtrsim 3.14$

- $B - L$ mystery: global, local, unbroken, broken by 2, 4, ... units?
- Currently testing: $\Delta L = 2$ via $0\nu 2\beta$.
- $\Delta L \geq 4$ way more challenging (experimentally and theoretically).
- Lepton number violation not synonymous with Majorana neutrinos.
- $\Delta L = 4$ lowest LNV of Dirac neutrinos.
- New Dirac leptogenesis ($3.14 \lesssim N_{\text{eff}} \lesssim 3.29$).

Let's add some flavor. . .

Neutrinos and abelian **flavor** symmetries

$$\underbrace{U(1)_{B-L}}_{\text{unflavored}} \times \overbrace{U(1)_{L_e-L_\mu} \times U(1)_{L_\mu-L_\tau}}^{\text{flavored}} \underbrace{\phantom{U(1)_{L_e-L_\mu} \times U(1)_{L_\mu-L_\tau}}}_{\text{dark}} .$$

Neutrino Mixing

Pontecorvo–Maki–Nakagawa–Sakata leptonic mixing matrix

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13}e^{i\alpha} & s_{13}e^{i(\beta-\delta_{\text{CP}})} \\ -c_{23}s_{12} - s_{23}s_{13}c_{12}e^{i\delta_{\text{CP}}} & (c_{23}c_{12} - s_{23}s_{13}s_{12}e^{i\delta_{\text{CP}}})e^{i\alpha} & s_{23}c_{13}e^{i\beta} \\ s_{23}s_{12} - c_{23}s_{13}c_{12}e^{i\delta_{\text{CP}}} & -(s_{23}c_{12} + c_{23}s_{13}s_{12}e^{i\delta_{\text{CP}}})e^{i\alpha} & c_{23}c_{13}e^{i\beta} \end{pmatrix}$$

with [\[Gonzalez-Garcia et al, arXiv:1409.5439\]](#)

$$\sin^2 \theta_{13} \simeq 0.02,$$

$$\sin^2 \theta_{12} \simeq 0.30,$$

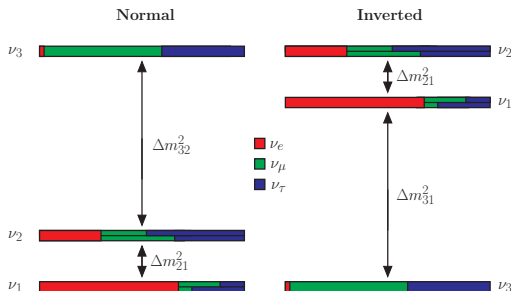
$$\Delta m_{21}^2 \simeq 7.5 \times 10^{-5} \text{ eV}^2,$$

$$\sin^2 \theta_{23} \simeq 0.45 \text{ (NO) or}$$

$$\sin^2 \theta_{23} \simeq 0.58 \text{ (IO),}$$

$$\Delta m_{31}^2 \simeq 2.46 \times 10^{-3} \text{ eV}^2 \text{ (NO) or}$$

$$\Delta m_{32}^2 \simeq -2.45 \times 10^{-3} \text{ eV}^2 \text{ (IO).}$$



Ordering (normal or inverted), absolute scale, phases?

Why these values? Symmetries!?

Neutrino Hierarchies

Majorana mass matrix $\mathcal{M}_\nu = U \text{diag}(m_1, m_2, m_3) U^T$ in special cases:

- 1 **Normal hierarchy** ($m_1 \simeq 0$) and best-fit values (phases zero):

$$\mathcal{M}_\nu \simeq \begin{pmatrix} 0.37 & 0.75 & 0.24 \\ \cdot & 2.47 & 2.11 \\ \cdot & \cdot & 2.99 \end{pmatrix} 10^{-2} \text{ eV} \sim \begin{pmatrix} 0 & 0 & 0 \\ 0 & \times & \times \\ 0 & \times & \times \end{pmatrix} \leftarrow L_e$$

- 2 **Inverted hierarchy** ($m_3 \simeq 0$) and $\alpha = \pi/2$:

$$\mathcal{M}_\nu \simeq \begin{pmatrix} 1.84 & -3.11 & 3.22 \\ \cdot & -0.14 & 0.88 \\ \cdot & \cdot & -1.77 \end{pmatrix} 10^{-2} \text{ eV} \sim \begin{pmatrix} 0 & \times & \times \\ \times & 0 & 0 \\ \times & 0 & 0 \end{pmatrix} \leftarrow L_e - L_\mu - L_\tau$$

- 3 **Quasi-degenerate** ($m_{1,2,3} \simeq 1 \text{ eV}$) and $\beta = \pi/2$:

$$\mathcal{M}_\nu \simeq \begin{pmatrix} 0.96 & -0.20 & -0.22 \\ \cdot & 0.11 & -0.97 \\ \cdot & \cdot & -0.07 \end{pmatrix} \text{ eV} \sim \begin{pmatrix} \times & 0 & 0 \\ 0 & 0 & \times \\ 0 & \times & 0 \end{pmatrix} \leftarrow L_\mu - L_\tau$$

Now what?

- Three interesting zeroth order approximations:

$$\mathcal{M}_\nu^{L_e} \sim \begin{pmatrix} 0 & 0 & 0 \\ 0 & \times & \times \\ 0 & \times & \times \end{pmatrix}, \quad \mathcal{M}_\nu^{L_e - L_\mu - L_\tau} \sim \begin{pmatrix} 0 & \times & \times \\ \times & 0 & 0 \\ \times & 0 & 0 \end{pmatrix}, \quad \mathcal{M}_\nu^{L_\mu - L_\tau} \sim \begin{pmatrix} \times & 0 & 0 \\ 0 & 0 & \times \\ 0 & \times & 0 \end{pmatrix}$$

[G. Branco, W. Grimus, L. Lavoura, *NPB (1989)*; S. Choubey, W. Rodejohann, *EPJC 40 (2005)*]

- Impose $U(1)_X$ to get \mathcal{M}_ν^X , then slightly break it.
 \Rightarrow Goldstone boson. . .
- Here: promote to **local** symmetry. Goldstone \rightarrow massive Z' .
- Remember: SM $+3\nu_R$ has anomaly free
 $U(1)_{B-L} \times U(1)_{L_e - L_\mu} \times U(1)_{L_\mu - L_\tau}$.

Simply take $U(1)_{B-3L_e}$, $U(1)_{B+3(L_e-L_\mu-L_\tau)}$, or $U(1)_{L_\mu-L_\tau}$?

Wrong end of the seesaw

- Imposing $U(1)_{B-3L_e}$ gives L_e symmetric \mathcal{M}_R , but **not** L_e symmetric

$$\mathcal{M}_\nu \simeq -m_D^T \mathcal{M}_R^{-1} m_D,$$

because $\mathcal{M}_R^{L_e}$ **not invertible!**

- Weird coincidence:

$$\mathcal{M}_R^{L_e - L_\mu - L_\tau} \sim \begin{pmatrix} \varepsilon & 1 & 1 \\ \cdot & \varepsilon & \varepsilon \\ \cdot & \cdot & \varepsilon \end{pmatrix} \Rightarrow \mathcal{M}_\nu \sim \mathcal{M}_R^{-1} \sim \begin{pmatrix} \varepsilon^2 & \varepsilon & \varepsilon \\ \cdot & 1 & 1 \\ \cdot & \cdot & 1 \end{pmatrix}.$$

$L_e - L_\mu - L_\tau$ gives approximate L_e symmetry after seesaw!

Broken $U(1)_{B+3(L_e-L_\mu-L_\tau)}$ (say $\varepsilon = 0.05$) gives **normal hierarchy**.¹⁴

- (Inverted hierarchy requires additional \mathbb{Z}_2 symmetry.)

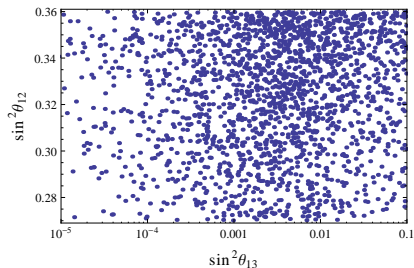
¹⁴J.H. and W. Rodejohann, PRD **85**, 113017 (2012) [arXiv:1203.3117].

Mixing Angles and Collider

- $U(1)_{B+3(L_e-L_\mu-L_\tau)}$ broken by scalar $S \sim 6$ in RHN sector:

$$S^* \bar{\nu}_{R,1}^c \nu_{R,1}, \quad S \bar{\nu}_{R,2}^c \nu_{R,2}, \quad S \bar{\nu}_{R,2}^c \nu_{R,3}, \quad S \bar{\nu}_{R,3}^c \nu_{R,3} \Rightarrow \Delta \mathcal{M}_R \sim \langle S \rangle.$$

- VEV $v_S \sim \varepsilon |\mathcal{M}_R|$ gives:



- μ and τ same $U(1)'$ charge: θ_{23} random (large...).
- LEP-II constraint on $U(1)_{B+3(L_e-L_\mu-L_\tau)}$: $v_S > 2.3 \text{ TeV}$, LHC prospects in [H. S. Lee and E. Ma, *PLB* 688 (2010)].

$$L_\mu - L_\tau$$

- Anomaly free in SM even without ν_R .¹⁵
- $\mathcal{M}^{L_\mu - L_\tau}$ invertible \Rightarrow Seesaw gives $L_\mu - L_\tau$ symmetric \mathcal{M}_ν .
- Add one or two scalars S that couple to $\bar{\nu}_{R,i}^c \nu_{R,j}$ and get a VEV.
- VEV fills zeros in \mathcal{M}_R and \mathcal{M}_ν and gives mass to Z' boson $M_{Z'}/g' \sim \langle S \rangle$.
- No Z' coupling to first generation \rightarrow “Weak” limits for heavy Z' :

$$M_{Z'}/g' > 550 \text{ GeV} \quad \text{at} \quad 95\% \text{ C.L.}$$

from trident production at CCFR $\nu_\mu N \rightarrow \nu_\mu N \rightarrow \nu_\mu N \mu^+ \mu^-$.¹⁶

- Light Z' (below 400 MeV) can resolve muon's magnetic moment anomaly.¹⁷

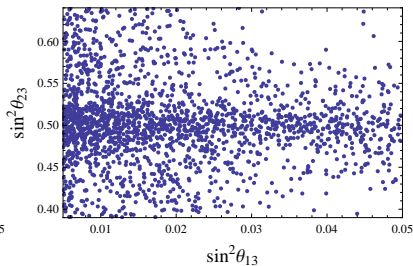
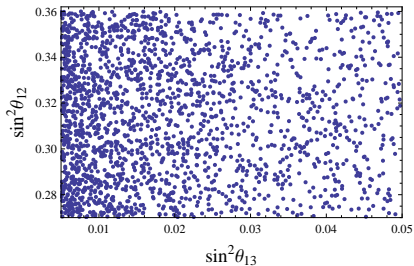
¹⁵Foot (1991), He, Joshi, Lew, Volkas (1991).

¹⁶Altmannshofer Gori, Pospelov, Yavin, PRD **89** (2014) [arXiv:1403.1269].

¹⁷Altmannshofer Gori, Pospelov, Yavin, PRL **113** (2014) [arXiv:1406.2332].

$$L_\mu - L_\tau$$

Two scalars, $\varepsilon = v_S/|\mathcal{M}_R| = 0.02$:



$L_\mu - L_\tau$ and Lepton Flavor Violation

- LFV in charged leptons if we break $L_\mu - L_\tau$ with a scalar doublet.¹⁸
- Can source $h \rightarrow \mu\tau$.¹⁹

SM-like doublet Φ_2 , new doublet Φ_1 with $L_\mu - L_\tau$ charge -2 , and singlet S with $+1$:

$$V(\Phi_1, \Phi_2, S) = m_1^2 |\Phi_1|^2 + \frac{\lambda_1}{2} |\Phi_1|^4 - m_2^2 |\Phi_2|^2 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 \\ - \mu_S^2 |S|^2 + \frac{\lambda_S}{2} |S|^4 + \lambda_{\Phi_1 S} |\Phi_1|^2 |S|^2 + \lambda_{\Phi_2 S} |\Phi_2|^2 |S|^2 \\ - \delta S^2 \Phi_2^\dagger \Phi_1 + \text{h.c.}$$

S heavy and large VEV: 2HDM with softly broken $U(1)$:

$$V(\Phi_1, \Phi_2) \simeq m_1^2 |\Phi_1|^2 + \frac{\lambda_1}{2} |\Phi_1|^4 - m_2^2 |\Phi_2|^2 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 \\ - m_3^2 \Phi_2^\dagger \Phi_1 + \text{h.c.}$$

Small VEV for Φ_1 : $\langle \Phi_1 \rangle \simeq \langle \Phi_2 \rangle m_3^2 / m_1^2 \simeq \delta \langle \Phi_2 \rangle \langle S \rangle^2 / m_1^2$.

¹⁸J.H., Rodejohann, PRD **84** (2011) [arXiv:1107.5238].

¹⁹J.H., Holthausen, Rodejohann, Shimizu, arXiv:1411.XXXX.

Yukawa Structure

$$\begin{aligned}
-\mathcal{L}_Y &= \bar{L}_L Y_{\ell_1} \Phi_1 \ell_R + \bar{L}_L Y_{N_1} \tilde{\Phi}_1 N_R \\
&+ \bar{L}_L Y_{\ell_2} \Phi_2 \ell_R + \bar{L}_L Y_{N_2} \tilde{\Phi}_2 N_R + \bar{Q}_L Y_u \tilde{\Phi}_2 u_R + \bar{Q}_L Y_d \Phi_2 d_R \\
&+ \frac{1}{2} \bar{N}_R^c \mathcal{M}_N N_R + \frac{1}{2} \bar{N}_R^c Y_{S_1} S N_R + \frac{1}{2} \bar{N}_R^c Y_{S_2} \bar{S} N_R + \text{h.c.}
\end{aligned}$$

with matrices

$$\begin{aligned}
Y_{\ell_2} &= \text{diag}(y_e, y_\mu, y_\tau), & Y_{N_2} &= \text{diag}(y_1, y_2, y_3), \\
Y_{\ell_1} &= \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & \xi_{\tau\mu} & 0 \end{pmatrix}, & Y_{N_1} &= \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & \xi_{23} \\ 0 & 0 & 0 \end{pmatrix}.
\end{aligned}$$

$$\mathcal{M}_N = \begin{pmatrix} M_1 & & \\ & M_2 & \\ & & M_2 \end{pmatrix}, \quad Y_{S_1} = \begin{pmatrix} 0 & 0 & a_{13} \\ 0 & 0 & 0 \\ a_{13} & 0 & 0 \end{pmatrix}, \quad Y_{S_2} = \begin{pmatrix} 0 & a_{12} & 0 \\ a_{12} & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}.$$

Charged Lepton Masses

$$M_e = \frac{v}{\sqrt{2}} \begin{pmatrix} y_e s_\beta & & \\ & y_\mu s_\beta & \\ & \xi_{\tau\mu} c_\beta & y_\tau s_\beta \end{pmatrix} \equiv V_{eL} \text{diag}(m_e, m_\mu, m_\tau) V_{eR}^\dagger,$$

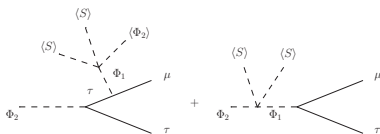
with

$$\frac{\tan \theta_L}{\tan \theta_R} = \frac{m_\mu}{m_\tau} \ll 1 \quad \text{and} \quad \sin \theta_R \simeq \frac{v}{m_\tau} \frac{\xi_{\tau\mu}}{\sqrt{2}} \cos \beta.$$

SM-like scalar h couples

$$y \simeq \underbrace{\text{diag}(m_e, m_\mu, m_\tau)}_{\text{type-I 2HDM}} \frac{c_\alpha}{v s_\beta} - s_R \frac{m_\tau}{v} \frac{\cos(\alpha - \beta)}{c_\beta s_\beta} \begin{pmatrix} 0 & & \\ -c_{RSL} & -s_{LSR} & \\ c_{LCR} & c_{LSR} & \end{pmatrix}.$$

Only LFV in μ - τ sector, quarks and electrons save!

$h \rightarrow \mu\tau$


CMS 2.5σ excess in $h \rightarrow \mu\tau$ for²⁰

$$|y_{\tau\mu}^h| = \frac{m_\tau}{v} \left| \frac{\cos(\alpha - \beta)}{c_\beta s_\beta} c_{RCLSR} \right| \simeq 7 \times 10^{-3} \left| \frac{\cos(\alpha - \beta)}{s_\beta c_\beta} c_{RSR} \right| \stackrel{!}{\simeq} 3 \times 10^{-3}.$$

- Either $c_\beta, s_R \ll 1$ and $\xi_{\tau\mu} c_{\alpha-\beta} \simeq 4 \times 10^{-3}$,
- or larger s_R and correlations with $h \rightarrow \tau\tau, \mu\mu$:

$$\frac{\text{BR}(h \rightarrow \tau\tau)}{\text{BR}(h \rightarrow \tau\tau)|_{\text{SM}}} \simeq \left(\frac{c_\alpha}{s_\beta} - y_{\tau\mu}^h \frac{v}{m_\tau} t_R \right)^2 \simeq (1 \pm 0.4 |t_R|)^2,$$

compared to 0.78 ± 0.27 (CMS) or $1.4_{-0.4}^{+0.5}$ (ATLAS).

²⁰J.H., Holthausen, Rodejohann, Shimizu, arXiv:1411.XXXX.

One step further: texture zeros

- $U(1)_{B-L} \times U(1)_{L_e-L_\mu} \times U(1)_{L_\mu-L_\tau}$ subgroups forbid entries in \mathcal{M}_R
 \Rightarrow texture zeros!²¹
- Choose subgroup so that some entries are allowed, others filled by $\langle S \rangle$, e.g. $B - L_e + L_\mu - 3L_\tau$ with $Y'(S) = 2$:

$$\begin{aligned} \mathcal{M}_R &= M_0 \begin{pmatrix} 0 & \times & 0 \\ \cdot & 0 & 0 \\ \cdot & \cdot & 0 \end{pmatrix} + \langle S \rangle \begin{pmatrix} \times & 0 & \times \\ \cdot & \times & 0 \\ \cdot & \cdot & 0 \end{pmatrix} \\ &\sim \begin{pmatrix} \times & \times & \times \\ \cdot & \times & 0 \\ \cdot & \cdot & 0 \end{pmatrix} \sim \begin{pmatrix} 0 & 0 & \times \\ \cdot & \times & \times \\ \cdot & \cdot & \times \end{pmatrix}^{-1} \simeq \mathcal{M}_\nu^{-1}. \end{aligned}$$

- Dirac matrices diagonal by symmetry, so $\mathcal{M}_R \sim \mathcal{M}_\nu^{-1}$.
- Texture zeros imply testable correlations among neutrino parameters, *seven* out of 15 two-zero patterns currently viable.

²¹J.H., Araki, Kubo, JHEP **1207** (2012) [arXiv:1203.4951].

Simplest $U(1)'$ models with just one scalar

- With just one scalar S , we can get five of the seven valid patterns:²²

Symmetry generator Y'	$ Y'(S) $	Texture zeros in \mathcal{M}_R	Texture zeros in \mathcal{M}_ν
$L_\mu - L_\tau$	1	$(\mathcal{M}_R)_{33}, (\mathcal{M}_R)_{22}$ (\mathbf{C}^R)	–
$B - L_e + L_\mu - 3L_\tau$	2	$(\mathcal{M}_R)_{33}, (\mathcal{M}_R)_{13}$ (\mathbf{B}_4^R)	$(\mathcal{M}_\nu)_{12}, (\mathcal{M}_\nu)_{22}$ (\mathbf{B}_3^ν)
$B - L_e - 3L_\mu + L_\tau$	2	$(\mathcal{M}_R)_{22}, (\mathcal{M}_R)_{12}$ (\mathbf{B}_3^R)	$(\mathcal{M}_\nu)_{13}, (\mathcal{M}_\nu)_{33}$ (\mathbf{B}_4^ν)
$B + L_e - L_\mu - 3L_\tau$	2	$(\mathcal{M}_R)_{33}, (\mathcal{M}_R)_{23}$ (\mathbf{D}_2^R)	$(\mathcal{M}_\nu)_{12}, (\mathcal{M}_\nu)_{11}$ (\mathbf{A}_1^ν)
$B + L_e - 3L_\mu - L_\tau$	2	$(\mathcal{M}_R)_{22}, (\mathcal{M}_R)_{23}$ (\mathbf{D}_1^R)	$(\mathcal{M}_\nu)_{13}, (\mathcal{M}_\nu)_{11}$ (\mathbf{A}_2^ν)

- Many patterns are hard to distinguish via neutrino experiments, e.g. \mathbf{D}_1^R and \mathbf{D}_2^R , but the symmetries $B + L_e - 3L_\mu - L_\tau$ and $B + L_e - L_\mu - 3L_\tau$ are very different

⇒ new possibilities to disentangle texture zeros.

- More scalars or discrete \mathbb{Z}_N subgroups can generate other allowed patterns.

²²J.H., Araki, Kubo, JHEP **1207** (2012) [arXiv:1203.4951].

Flavored Summary

- $SM+3\nu_R$ has anomaly free local $U(1)_{B-L} \times U(1)_{L_e-L_\mu} \times U(1)_{L_\mu-L_\tau}$.

Can use subgroups to influence

- Neutrino hierarchies:
 - $U(1)_{B+3(L_e-L_\mu-L_\tau)}$ for normal hierarchy,
 - $(U(1)_{B+3(L_e-L_\mu-L_\tau)} \times \mathbb{Z}_2)$ for inverted hierarchy,
 - $U(1)_{L_\mu-L_\tau}$ for quasi-degenerate.
- Texture zeros in \mathcal{M}_ν or \mathcal{M}_ν^{-1} .
- Specific LFV modes, e.g. $h \rightarrow \mu\tau$ via $L_\mu - L_\tau$.
- (Z' pheno on top: muon's magnetic moment, leptophilic DM, ...)

Very simple models, surprisingly potent framework!

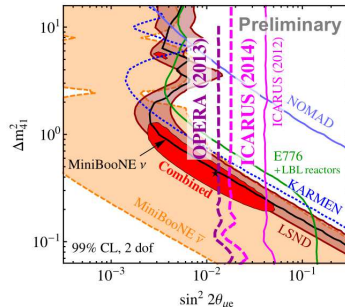
Dark Symmetries and Light Sterile Neutrinos

Neutrinos and *dark* gauge symmetries

$$\underbrace{U(1)_{B-L}}_{\text{unflavored}} \times \overbrace{U(1)_{L_e-L_\mu} \times U(1)_{L_\mu-L_\tau}}^{\text{flavored}} \underbrace{\quad}_{\text{dark}}.$$

- LSND, MiniBooNE: ν_S with eV mass and mixing $U_{as} \sim 0.1$?
- Tension appearance vs. disappearance...
- Tension with cosmology...

[Kopp, Neutrino 2014]



If we ever observe a sterile neutrino, it's lighter than “expected” (10^9 GeV). Why?

How to make ν_s light?

Isn't new physics always at TeV?

- Use seesaw partners ν_R as steriles: eV-seesaw

$$\mathcal{M} = \begin{pmatrix} 0 & m_D \\ m_D^T & M_R \end{pmatrix}$$

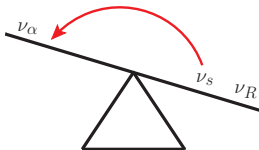
with $m_D \sim 0.1 \text{ eV}$, $M_R \sim 1 \text{ eV}$. [de Gouvêa, *PRD* (2005)]

- Active–sterile mixing automatically large:
 $U_{as} \sim m_D/M_R \sim \sqrt{m_\nu/m_s} \sim 0.1$.
- Minimal 3 + 2 scheme: two ν_R at eV scale, works fine.
[Donini, Schwetz et al., *JHEP* (2012)]
- Just throw in random $\mathcal{O}(1)$ couplings: sterile neutrino anarchy.
[JH, Rodejohann, *PRD* (2013)]

\Rightarrow The “heavy” eV-scale suppresses the “light” 0.1 eV?

How to make ν_s light? II

- Put ν_s on the other side of the seesaw:



- Suppressed *BY* seesaw: need additional right-handed singlet S and mass matrix for $(\nu_\alpha, \nu_{R,j}^c, S^c)$

$$\mathcal{M}_{\text{MES}} = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & M_R & m_S \\ 0 & m_S^T & 0 \end{pmatrix}.$$

Minimal Extended Seesaw (MES) [Chun, Joshipura, Smirnov, *PLB* (1995), Babu, Seidl, *PRD,PLB* (2004), Barry, Rodejohann, Zhang, *JHEP* (2011), Zhang, *PLB* (2012)]

- Works also for $3 + 2$, $3 + 3, \dots$, just add more singlets.

Minimal extended seesaw

$$\mathcal{M}_{\text{MES}} = \begin{pmatrix} 0^{3 \times 3} & m_D & 0 \\ m_D^T & M_R^{3 \times 3} & m_S \\ 0 & m_S^T & 0^{1 \times 1} \end{pmatrix}$$

Assume $M_R \gg m_D, m_S$, usual seesaw:

$$\mathcal{M}_\nu^{4 \times 4} \simeq - \begin{pmatrix} (m_D M_R^{-1} m_D^T)^{3 \times 3} & m_D M_R^{-1} m_S \\ m_S^T M_R^{-1} m_D^T & (m_S^T M_R^{-1} m_S)^{1 \times 1} \end{pmatrix}.$$

- all masses suppressed by seesaw scale $M_R \sim 2 \times 10^{14}$ GeV. ✓
- sterile mass $m_4 \sim 1$ eV for $m_S \sim 5\text{--}10 m_D$.
- active–sterile mixing $U_{as} = \mathcal{O}(m_D/m_S)$ automatically right. ✓

⇒ SBL sterile neutrinos. ✓

Great, but how to get MES structure?

How to get MES

Need

$$\bar{L}\langle H\rangle\nu_R,$$

$$m_S\bar{S}^c\nu_R,$$

$$M_R\bar{\nu}_R^c\nu_R$$

and forbid couplings

$$\bar{L}\langle H\rangle S,$$

$$\bar{S}^c S.$$

- Flavor symmetry $A_4 \otimes \mathbb{Z}_4$ (messy...). [Zhang, *PLB* (2012)]
- Abelian gauge symmetry $U(1)'$: simple, but need additional fermions to cancel anomalies. [Babu, Seidl, *PLB* (2004)]
 - Cancel anomalies, make new fermions massive, and not disturb MES structure? With few scalars? **Yes!**

Magic numbers

	$\nu_{R,1}$	$\nu_{R,2}$	$\nu_{R,3}$	S_1	S_2	S_3	S_4	S_5	S_6	S_7	ϕ
Y'	0	0	0	11	-5	-6	1	-12	2	9	11

Mass matrix has nice block structure:

$$\mathcal{M} = \begin{pmatrix} (\mathcal{M}_{\text{MES}})_{7 \times 7} & 0 \\ 0 & (\mathcal{M}_S)_{6 \times 6} \end{pmatrix}$$

with

$$\mathcal{M}_S = \begin{pmatrix} 0 & y_1 \langle \phi \rangle & 0 & 0 & 0 & 0 \\ y_1 \langle \phi \rangle & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & y_2 \langle \phi \rangle & 0 & 0 \\ 0 & 0 & y_2 \langle \phi \rangle & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & y_3 \langle \phi \rangle \\ 0 & 0 & 0 & 0 & y_3 \langle \phi \rangle & 0 \end{pmatrix}.$$

$\Rightarrow S_1$ gives MES, $S_{2,3,4,5,6,7}$ decouple and form 3 Dirac fermions $\Psi_{1,2,3}$!

More numbers

- Happy “accident”: ϕ breaks $U(1)'$ to \mathbb{Z}_{11} .
 \Rightarrow all three Ψ_j stable!
- Active–sterile mixing $V_{4j} \sim \mathcal{O}(m_D/m_S) \stackrel{!}{=} \mathcal{O}(0.1)$.
- For $\mathcal{O}(1)$ Yukawas $\Rightarrow U(1)'$ breaking at $\langle \phi \rangle \sim 10 \langle H \rangle \sim \text{TeV}$.
 \Rightarrow masses for Z' , $\text{Re}(\phi)$, $\Psi_{1,2,3}$ around 100 GeV–TeV.

\Rightarrow Multicomponent stable dark matter.

Breakdown of neutral fermions:

$$\underbrace{\nu_e, \nu_\mu, \nu_\tau, S_1, \overbrace{\nu_{R,1}, \nu_{R,2}, \nu_{R,3}}^{\text{seesaw/leptogenesis}}}_{(3+1) \text{ MES}}, \underbrace{\overbrace{S_2, S_3}^{\Psi_1}, \overbrace{S_4, S_5}^{\Psi_2}, \overbrace{S_6, S_7}^{\Psi_3}}_{\text{DM}}$$

Dark matter interactions

Lagrangian:

$$\sum_j \left[i \bar{\Psi}_j \gamma^\mu \partial_\mu \Psi_j - M_j \left(1 + \frac{\text{Re}(\phi)}{\langle \text{Re}(\phi) \rangle} \right) \bar{\Psi}_j \Psi_j + \frac{g'}{2} Z'_\mu \bar{\Psi}_j \gamma^\mu (g_j^V + g_j^A \gamma_5) \Psi_j \right]$$

with $g_1^V = 1$, $g_2^V = 13$, $g_3^V = -7$, $g_1^A = -11$, $g_2^A = -11$, $g_3^A = 11$.

Connection to the Standard Model just like all other $U(1)_{\text{DM}}$ models:

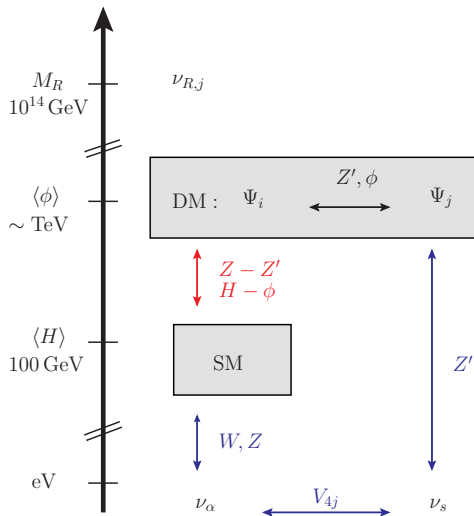
- Scalar mixing (Higgs portal): $\mathcal{L} \supset \delta |H|^2 |\phi|^2$
 $\Rightarrow \Psi_j$ couple to Brout–Englert–Higgs boson.
- Vector mixing (kinetic-mixing portal): $\mathcal{L} \supset \sin \xi F_Y^{\mu\nu} F'_{\mu\nu}$
 $\Rightarrow \Psi_j$ couple to Z boson.

New:

- Fermion mixing (neutrino portal):

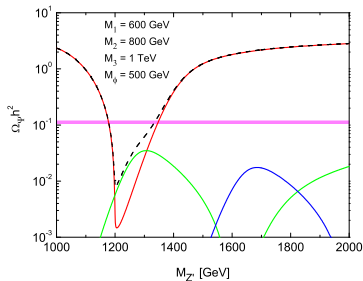
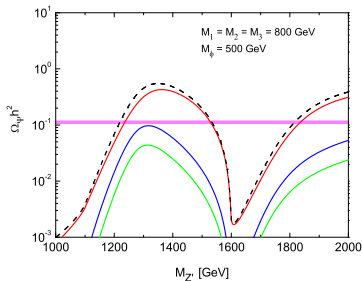
$$\mathcal{L} \supset \frac{11g'}{2} Z'_\mu \sum_{i,j=1}^4 V_{4i}^* V_{4j} (\bar{\nu}_i \gamma^\mu \gamma_5 \nu_j + \bar{\nu}_i \gamma^\mu \nu_j) .$$

Neutrino portal



Relic density via neutrino portal

- Relic density via annihilation $\Psi\Psi \rightarrow Z' \rightarrow \nu_s\nu_s$ into sterile neutrinos.



- Direct detection is loop-suppressed: $\sim \Delta m_{41}^2 / (100 \text{ GeV})^2 \sim 10^{-22}$.
- Indirect detection: $\text{BR}(\Psi\Psi \rightarrow \nu\nu) \simeq 100\%$ gives monochromatic neutrinos from Galactic halo. Too small for IceCube...
- Including Higgs portal and kinetic-mixing portal gives the usual measurable effects.

Dark Summary

- Additional right-handed neutrinos with exotic charges under a broken $U(1)'$ can generate structure in neutral fermions.
- Here: generate seesaw-suppressed sterile neutrino.
- Magic numbers: necessary anomaly-cancelling fermions form multicomponent DM.
- Gauge interactions open new SM–DM portal through sterile neutrinos.

⇒ Huge unexplored playground!

Other charges: $3 + 2$, $3 + 3$, Majorana DM, unstable DM, ...

Conclusion

- Abelian gauge symmetries $U(1)'$ versatile framework.
- Simple, minimalistic, renormalizable.
- SM-motivated symmetries

$$\underbrace{U(1)_{B-L}}_{\text{unflavored}} \times \overbrace{U(1)_{L_e-L_\mu} \times U(1)_{L_\mu-L_\tau}}^{\text{flavored}} \underbrace{\quad}_{\text{dark}} .$$

connected to neutrino properties:

- $B - L$ for Majorana vs. Dirac and leptogenesis.
- $B - L$ only possible unbroken symmetry acting on SM particles.
- $L_\mu - L_\tau$, $B + 3(L_e - L_\mu - L_\tau)$, ... for hierarchies, mixing angles, texture zeros, LFV, $h \rightarrow \mu\tau$, muon's magnetic moment, R -parity, ...
- Dark $U(1)'$ for sterile neutrino pheno, dark matter stability and abundance, ...

Conclusion

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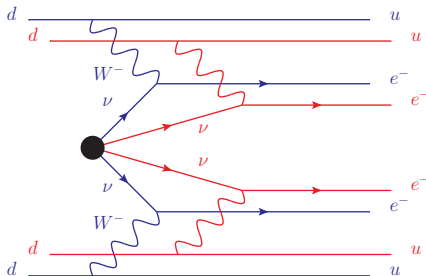
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- Dark $U(1)'$ for sterile neutrino pheno, dark matter stability and abundance, ...

Merci!

How to check for $\Delta L = 4$?

- **Neutrinoless quadruple beta decay**²³ $(A, Z) \rightarrow (A, Z + 4) + 4 e^-$
e.g. via $\mathcal{O}_{\Delta L=4} = (\bar{\nu}_L^c \nu_L)^2 / \Lambda^2$:

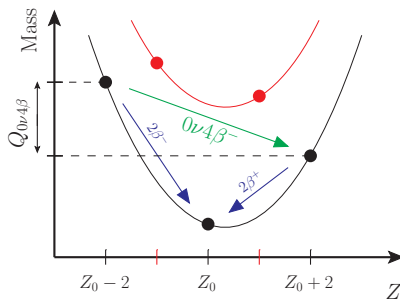


- Collider process $e^- e^- \rightarrow W^- W^- W^- W^- \ell^+ \ell^+$.
- Rare meson decays etc.?

²³J.H. and W. Rodejohann, EPL **103**, 32001 (2013) [arXiv:1306.0580].

Candidate Nuclei for $0\nu 4\beta$

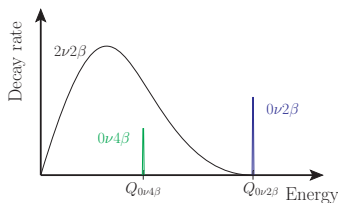
	$Q_{0\nu 4\beta}$	Other decays	NA/%
${}^{96}_{40}\text{Zr} \rightarrow {}^{96}_{44}\text{Ru}$	0.629 MeV	$\tau_{1/2}^{2\nu 2\beta} \simeq 2 \times 10^{19} \text{ y}$	2.8
${}^{136}_{54}\text{Xe} \rightarrow {}^{136}_{58}\text{Ce}$	0.044 MeV	$\tau_{1/2}^{2\nu 2\beta} \simeq 2 \times 10^{21} \text{ y}$	8.9
${}^{150}_{60}\text{Nd} \rightarrow {}^{150}_{64}\text{Gd}$	2.079 MeV	$\tau_{1/2}^{2\nu 2\beta} \simeq 7 \times 10^{18} \text{ y}$	5.6



Best Candidate: Neodymium ^{150}Nd

Decay channels:

- $^{150}_{60}\text{Nd} \rightarrow ^{150}_{62}\text{Sm}$ via $2\nu 2\beta$ ($\tau_{1/2}^{2\nu 2\beta} \simeq 7 \times 10^{18}$ y): the two electrons have a continuous energy spectrum and total energy $E_{e,1} + E_{e,2} < 3.371$ MeV.
- $^{150}_{60}\text{Nd} \rightarrow ^{150}_{64}\text{Gd}$ via $0\nu 4\beta$. Four electrons with continuous energy spectrum and summed energy $Q_{0\nu 4\beta} = 2.079$ MeV are emitted. In this special case, the daughter nucleus is α -unstable with half-life $\tau_{1/2}^{\alpha}(^{150}_{64}\text{Gd} \rightarrow ^{146}_{62}\text{Sm}) \simeq 2 \times 10^6$ y.



$0\nu 4\beta$ kinematically allowed, but expected rates unobservable.

Texture Zeros

- Take \mathcal{M}_ν and set two independent entries to zero \Rightarrow four constraints on the nine low-energy parameters (m_1, m_2, m_3) , $(\theta_{23}, \theta_{12}, \theta_{13})$ and (δ, α, β) (CP violating phases)
- 15 two-zero textures possible, only 7 allowed at 3σ : [H. Fritzsch et al, *JHEP 1109 (2011)*]

$$\mathbf{A}_1^\nu : \begin{pmatrix} 0 & 0 & \times \\ 0 & \times & \times \\ \times & \times & \times \end{pmatrix}, \quad \mathbf{A}_2^\nu : \begin{pmatrix} 0 & \times & 0 \\ \times & \times & \times \\ 0 & \times & \times \end{pmatrix}, \quad \mathbf{B}_1^\nu : \begin{pmatrix} \times & \times & 0 \\ \times & 0 & \times \\ 0 & \times & \times \end{pmatrix}, \quad \mathbf{B}_2^\nu : \begin{pmatrix} \times & 0 & \times \\ 0 & \times & \times \\ \times & \times & 0 \end{pmatrix},$$

$$\mathbf{B}_3^\nu : \begin{pmatrix} \times & 0 & \times \\ 0 & 0 & \times \\ \times & \times & \times \end{pmatrix}, \quad \mathbf{B}_4^\nu : \begin{pmatrix} \times & \times & 0 \\ \times & \times & \times \\ 0 & \times & 0 \end{pmatrix}, \quad \mathbf{C}^\nu : \begin{pmatrix} \times & \times & \times \\ \times & 0 & \times \\ \times & \times & 0 \end{pmatrix}.$$

Vanishing Minors

- Same idea, but with \mathcal{M}_ν^{-1} instead of \mathcal{M}_ν .
- Seven patterns for \mathcal{M}_ν^{-1} allowed:

$$\mathbf{D}_1^R : \begin{pmatrix} \times & \times & \times \\ \cdot & 0 & 0 \\ \cdot & \cdot & \times \end{pmatrix}, \quad \mathbf{D}_2^R : \begin{pmatrix} \times & \times & \times \\ \cdot & \times & 0 \\ \cdot & \cdot & 0 \end{pmatrix}, \quad \mathbf{B}_3^R : \begin{pmatrix} \times & 0 & \times \\ \cdot & 0 & \times \\ \cdot & \cdot & \times \end{pmatrix}, \quad \mathbf{B}_4^R : \begin{pmatrix} \times & \times & 0 \\ \cdot & \times & \times \\ \cdot & \cdot & 0 \end{pmatrix},$$

$$\mathbf{B}_1^R : \begin{pmatrix} \times & \times & 0 \\ \cdot & 0 & \times \\ \cdot & \cdot & \times \end{pmatrix}, \quad \mathbf{B}_2^R : \begin{pmatrix} \times & 0 & \times \\ \cdot & \times & \times \\ \cdot & \cdot & 0 \end{pmatrix}, \quad \mathbf{C}^R : \begin{pmatrix} \times & \times & \times \\ \cdot & 0 & \times \\ \cdot & \cdot & 0 \end{pmatrix}.$$

- Two-zero texture in \mathcal{M}_ν^{-1} corresponds to two vanishing minors in \mathcal{M}_ν . E.g.

$$\mathcal{M}^{-1} = \begin{pmatrix} \times & \times & 0 \\ \times & 0 & \times \\ 0 & \times & \times \end{pmatrix} \Rightarrow \begin{vmatrix} \mathcal{M}_{11} & \mathcal{M}_{13} \\ \mathcal{M}_{31} & \mathcal{M}_{33} \end{vmatrix} = 0 = \begin{vmatrix} \mathcal{M}_{21} & \mathcal{M}_{22} \\ \mathcal{M}_{31} & \mathcal{M}_{32} \end{vmatrix}$$