



Cosmological constraints, and LHC signatures of a Z' mediator between dark matter and the SU(3) sector

Lucien Heurtier

Bruxelles, November 2015

Based on :

- E. Dudas, L.H., Y. Mambrini and B. Zaldivar, "Extra U(1), effective operators, anomalies and dark matter", Arxiv : 1307.0005
- O. Ducu, L.H., J. Maurer, "LHC signatures of a Z' mediator between dark matter and the SU(3) sector" ArXiv : 1509.05615

Outline

- Why a U(1)' symmetry?
- Introduction to an effective Z' model
- State of the art in the electroweak sector
- What about colour?
- Dark matter constraints
- LHC constraints
- New possible signatures at LHC?

◊ Common wisdom : The standard model is uncomplete..

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Need to parametize our lack of knowledge!

Why a U(1)' Symmetry?

Possible approach :

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- Motivate additional effective operators
- Try to understand a smart toy-model!

Simplest extension of SM ightarrow add a U(1)' symmetry

Question : Who is charged under what?



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Two options :

- Charged SM fermions
 - \longrightarrow FCNC constraints
 - $\longrightarrow B L$, $\alpha(B L) + \beta Y$ models heavy Z'
 - \longrightarrow Stringy light Z', anomaly cancellation a la Green-Schwarz

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• Uncharged SM fermions

- \longrightarrow Motivations from string theory (D-brane models)
- \longrightarrow Heavy States \rightsquigarrow effective higher-dimensional operators

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The little story of a little rayline



$$E_{\gamma} = m_{DM} \left(1 - \frac{m_Z^2}{4m_{DM}^2} \right) \tag{1.1}$$

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The little story of a little light ray

[Dudas et al., 2012]



The little story of a little light ray

Weniger, 2012



End of the story?...

- \hookrightarrow detected in other regions of the sky
- \hookrightarrow detector effects suspected...

◊ Look at other possible interactions : What about SU(3) channels?

Reminder Box



Introduction : The model

♦ Heavy intermediate states : heavy SM fermions

Heavy mass scale : breaking of the heavy U(1)' higgs sector

Stueckelberg realization

$$\Phi = rac{V + \phi}{\sqrt{2}} exp(ia_X/V) \longrightarrow \Phi = rac{V}{\sqrt{2}} exp(ia_X/V)$$

U(1)' transformations

$$\delta Z'_{\mu} = \partial_{\mu} \alpha$$
 , $\delta \theta_X = rac{g_X}{2} \alpha$ where $\theta_X \equiv rac{a_X}{V}$

Initial lagrangian

$$\begin{split} \mathcal{L} &= \mathcal{L}_{SM} + \frac{1}{2} (\partial_{\mu} a_{X} - M_{Z'} Z'_{\mu})^{2} - \frac{1}{4} F^{X}_{\mu\nu} F^{X \, \mu\nu} \\ &+ \bar{\Psi}^{i}_{L} \left(i \gamma^{\mu} D_{\mu} + \frac{g_{X}}{2} X^{i}_{L} \gamma^{\mu} Z'_{\mu} \right) \Psi^{i}_{L} \\ &+ \bar{\Psi}^{i}_{R} \left(i \gamma^{\mu} D_{\mu} + \frac{g_{X}}{2} X^{i}_{R} \gamma^{\mu} Z'_{\mu} \right) \Psi^{i}_{R} \\ &- \left(\bar{\Psi}^{i}_{L} M_{ij} e^{\frac{i a_{X} (X^{i}_{L} - X^{j}_{R})}{V}} \Psi^{i}_{R} + \text{h.c.} \right) \\ \end{split}$$
where
$$\begin{split} M_{Z'} \equiv g_{X} \frac{V}{2} \, . \end{split}$$

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 $\hookrightarrow \mathcal{L}$ anomaly-free & \mathcal{L}_{SM} neutral under $U(1)' \Rightarrow \Psi_M$ set anomaly-free

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 $\hookrightarrow \mathcal{L} \text{ anomaly-free } \& \ \mathcal{L}_{SM} \text{ neutral under } U(1)' \Rightarrow \Psi_M \text{ set} \\ \text{anomaly-free}$

 $\hookrightarrow \text{ Kinetic mixing term } \tfrac{\delta}{2} \ F_X^{\mu\nu} \ F_{\mu\nu}^Y \text{ is neglected } \underbrace{\mathbb{W}_{hy}}_{\leftarrow}$

Effective couplings



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Effective couplings



$$\mathcal{L}_{CP \text{ even}}^{(6)} = \frac{1}{M^2} \left\{ d_g \partial^\mu D_\mu \theta_X \mathcal{T}r(G\tilde{G}) + d'_g \partial^\mu D^\nu \theta_X \operatorname{Tr}(G_{\mu\rho} \tilde{G}^\rho_{\nu}) \right. \\ \left. + \left. e_g D^\mu \theta_X \operatorname{Tr}(G_{\nu\rho} \mathcal{D}_\mu \tilde{G}^{\rho\nu}) + e'_g D_\mu \theta_X \operatorname{Tr}(G_{\alpha\nu} \mathcal{D}^\nu \tilde{G}^{\mu\alpha}) \right\} \\ \left. + \left. \frac{1}{M^2} \left\{ D^\mu \theta_X \left[i(D^\nu H)^\dagger (c_1 \tilde{F}^\gamma_{\mu\nu} + 2c_2 \tilde{F}^W_{\mu\nu}) H + h.c. \right] \right. \\ \left. + \left. \partial^m D_m \theta_X (d_1 \mathcal{T} r(F^\gamma \tilde{F}^\gamma) + 2d_2 \mathcal{T} r(F^W \tilde{F}^W)) \right. \\ \left. + \left. d'_{ew} \partial^\mu D^\nu \theta_X \operatorname{Tr}(F_{\mu\rho} \tilde{F}^\rho_{\nu}) \right. \\ \left. + \left. e_{ew} D^\mu \theta_X \operatorname{Tr}(F_{\nu\rho} \mathcal{D}_\mu \tilde{F}^{\rho\nu}) + e'_{ew} D_\mu \theta_X \operatorname{Tr}(F_{\alpha\nu} \mathcal{D}^\nu \tilde{F}^{\mu\alpha}) \right\} \right\} (1.2)$$

-





couplings

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$$\mathcal{L}_{DM} = \bar{\psi}_L^{DM} \frac{1}{2} g_X X_L^{DM} \gamma^\mu Z'_\mu \psi_L^{DM} + \bar{\psi}_R^{DM} \frac{1}{2} g_X X_R^{DM} \gamma^\mu Z'_\mu \psi_R^{DM}$$

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DM annihilation into Gluons

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 \hookrightarrow Chiral dark matter :

$$\langle \sigma v \rangle_{s-ch.} \simeq \frac{d_g^2}{M^4} \frac{g_X^4 m_{\psi}^6 (X_L - X_R)^2}{\pi M_{Z'}^4} \left\{ \frac{2 \left(M_{Z'}^2 - 4 m_{\psi}^2 \right)^2}{\left(M_{Z'}^2 \Gamma^2 (Z') + \left(M_{Z'}^2 - 4 m_{\psi}^2 \right)^2 \right)} \right\}$$

$$\langle \sigma v
angle_{t-ch.} \simeq rac{g_X^4 \sqrt{m_\psi^2 - M_{Z'}^2}}{128 \pi^2 m_\psi M_{Z'}^2 \left(2m_\psi^2 - M_{Z'}^2
ight)^2} P_4\left(m_\psi^2, M_{Z'}^2, X_R^2, X_L^2
ight)$$

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DM annihilation into Gluons

Main features :

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Main features :

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 \hookrightarrow T-channel opening at $m_{\psi} = M_{Z'}$

 \hookrightarrow T-channel mostly sensible to g_X

A few parameters in this model : $M_{Z'}$, m_{ψ} , g_X , $\frac{d_g}{M^2}$, X_L , X_R .

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Experimental constraints :

- Relic abundance
- Indirect detection
- LHC mono-jets events

What about direct detection?



Direct detection?

• Integrating out Z' :

$$\frac{d_g}{M^2 M_{Z'}^2} \, \bar{\psi}^{DM} \gamma^{\mu} \left(\frac{X_R + X_L}{2} + \frac{X_R - X_L}{2} \gamma_5 \right) \psi^{DM} \mathcal{T}r \, \partial_{\mu} (G \tilde{G})$$

• Imposing CP invariance for strong interactions :

 $\langle N(p)|{
m Tr}\ G^{
u}_{\mu} \tilde{G}^{\lambda}_{
u}|N(p')
angle = A\epsilon^{\lambdalphaeta}_{\mu} p_{lpha} p'_{eta}$ where A invariant.

$$\Rightarrow \langle N(p) | \mathcal{T}r \; \partial_{\mu}(G \, \tilde{G}) | N(p') \rangle = 0$$

No constraint from direct detection.

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Relic abundance and indirect detection





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Relic abundance and indirect detection



Other curves

LHC constraints

Possible mono-jets final states



Figure : Dark matter production processes at the LHC (at partonic level), in association with 1 jet: $p \ p \rightarrow j \bar{\psi}_{DM} \psi_{DM}$.

LHC constraints

Using CMS data [[CMS Collaboration], CMS-PAS-EXO-12-048], $E_{CM} = 8$ TeV:



Figure : 90% CL lower bounds on the quantity M^2/d_g as a function of the dark matter mass, for $M_{Z'} = 100$ GeV (blue), 500 GeV (red) and 1 TeV (green). Based on the CMS analysis with collected data using a center-of-mass energy of 8 TeV and a luminosity of 19.5/fb.

Synthesis





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Comparison with EW sector





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Any signature? ...



Interesting channels : multi-tops production



- $Z' \rightarrow GG$ forbidden by Landau-Yang
- Need (e.g.) ISR to feel the resonance
- Off-shell contributions in the *tttt* channel

Interesting channels : multi-tops production

1/ Tri-jets invariant mass :

- ISR+ $Z'
 ightarrow q ar{q} \, G$ (Br \sim 100 %)
- Studies of resonances : mainly di-jets or pair production
- Yet, at 7TeV : $\frac{d\sigma}{d\Omega}(m_{jjj})$: [Khachatryan et al. (CMS) arXiv:1412.1633]
- \hookrightarrow Upper limit on $\frac{d_g}{M^2}$

Tri-jets invariant mass

- Reproduce CMS cuts : $p_T > 100 {
 m GeV}$, |y| < 3.0
- Dissociate $|y|_{max} < 1$ and $1 \leqslant |y|_{max} \leqslant 2$
- Using Madgraph, CTEQ6L1, Pythia to MC, pdf and hadronisation



Figure : Three-jet invariant mass spectrum for QCD (left) and Z' signal models of various masses (right).

Tri-jets invariant mass



- Light Z' : peak smeared \rightarrow ISR selected in the tri-jets ...
- + : Populates high energetic bins
- + : QCD background is lower there
- - : Interpretation of the signal rendered less trivial..
- Exclusion limits on Z' at 7 TeV ightarrow upper limits on d_g/M^2

tītī production

• A promising channel : $t\bar{t}t\bar{t}$

	SM	Z' 300 ${ m GeV}$	$500{ m GeV}$	$800{ m GeV}$	$1.6 \mathrm{TeV}$	$3{ m TeV}$
8TeV	~ 1.3 fb	2.8 pb	0.36 pb	55 fb	5.9 fb	0.28 fb
13TeV	9.2 fb	0.57 μ b	74 pb	11 pb	1.2 pb	57 fb

- Very small coupling in the SM
- Landau-Yang suppression → off-shell contributions
 → no dependance on the Z' width
- Interferences SM-Z' negligible (<5%)
- CMS bound : $\sigma(t\bar{t}t\bar{t}) < 32 {
 m fb}$ at 8TeV

[Khachatryan et al.[CMS Collaboration] arXiv:1409.7339]

Constraints of LHC, run 1



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From exclusion limits to projections

- LHC run 2 : up to $100 fb^{-1}$ at 13 TeV
- Potential of discovery for this model?
- Tri jets : MC simulation of the background for pp → jjj up to m_{Z'} = 5TeV → Overestimation of the background compared to CMS at

high E : more conservative in our case

• Four-tops : at 13 TeV :

$$\sigma_{SM}(t\bar{t}t\bar{t}) \rightarrow imes 7$$

 $\sigma_{Z'}(t\bar{t}t\bar{t}) \rightarrow imes 200 !$

Results



• Model very much constrained from different perspectives

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- Microscopic computations of effective coupling to be extended to other interactions
- Possible predictions for the next runs of the LHC...

The End

Thank you!

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Constraints on kinetic mixing

If not neglected \longrightarrow new diagrams



$$\langle \sigma v \rangle_{GG} \simeq \frac{d_g^2}{M^4} \frac{2g_X^4}{\pi} \frac{m_{\psi}^6}{M_{Z'}^4} \,.$$
 (5.1)

 \rightarrow [X. Chu, Y. Mambrini, J. Quevillon and B. Zaldivar, arXiv:1306.4677 [hep-ph]

$$\begin{split} \langle \sigma v \rangle_{\delta} &\simeq \frac{16}{\pi} g_X^2 g^2 \delta^2 \frac{m_{\psi}^2}{M_{Z'}^4} \qquad , \qquad m_{\psi} < M_Z \\ \langle \sigma v \rangle_{\delta} &\simeq \frac{g_X^2 g^2 \delta^2 M_Z^4}{\pi m_{\psi}^2 M_{Z'}^4} \qquad , \qquad m_{\psi} > M_Z. \end{split}$$

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(5.2)

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Constraints on kinetic mixing

Kinetic mixing competes with other effective operators if

$$\delta \gtrsim \frac{d_g}{M^2} \frac{g_X}{2\sqrt{2}g} m_{\psi}^2 \qquad , \qquad m_{\psi} < M_Z$$

$$\delta \gtrsim \frac{d_g}{M^2} \frac{\sqrt{2}g_X}{g} \frac{m_{\psi}^4}{M_Z^2} \qquad , \qquad m_{\psi} > M_Z \qquad (5.3)$$

 \hookrightarrow For $m_\psi=$ 200 GeV : $rac{d_g}{M^2}\lesssim 10^{-4} imes \delta$ GeV $^{-2}$

Constraints on kinetic mixing



 $\hookrightarrow \delta \gtrsim$ 0.8 excluded by LEP experiments...

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Image: A matrix and a matrix