

Muonic hydrogen and the Proton Radius Puzzle

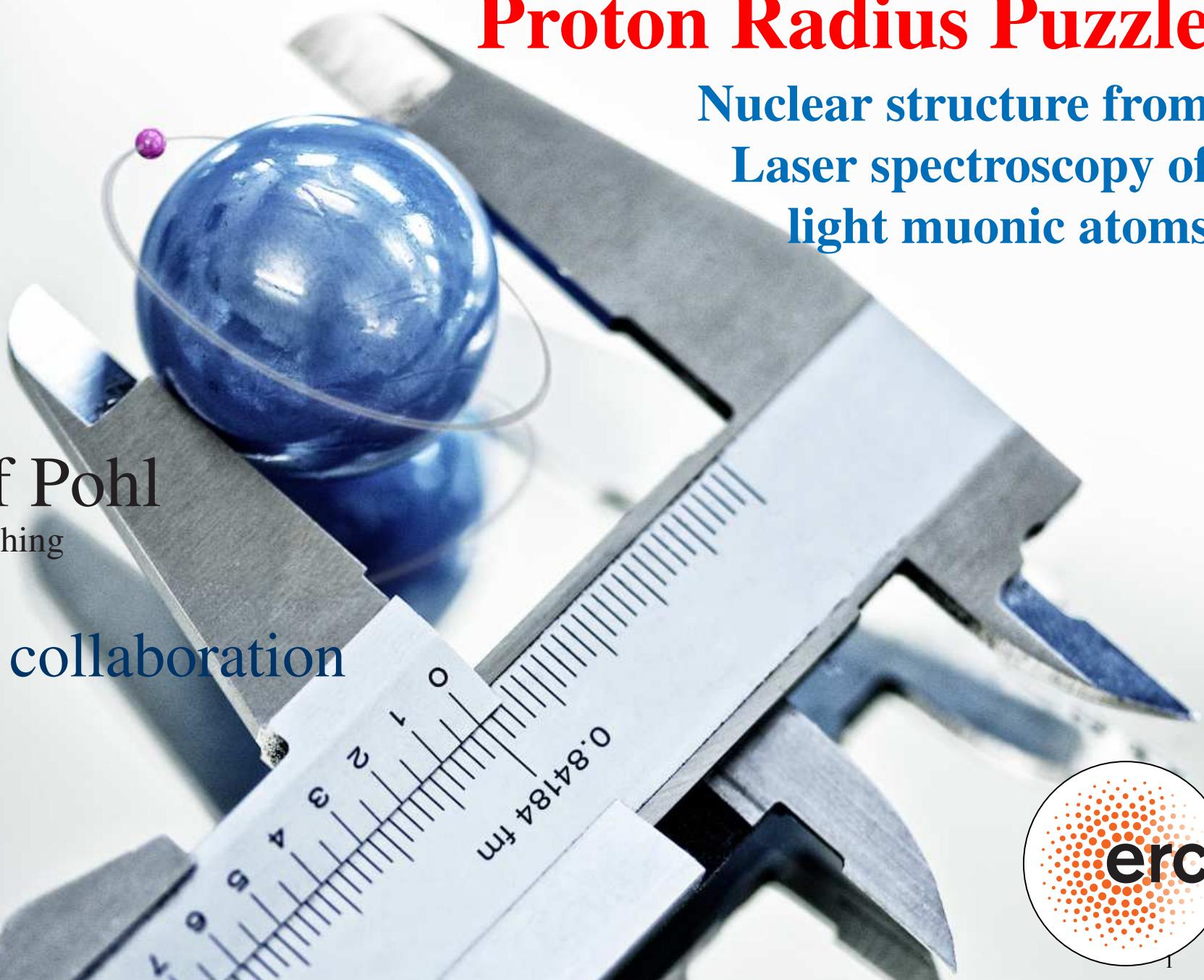
Nuclear structure from
Laser spectroscopy of
light muonic atoms

Randolf Pohl

MPQ, Garching

for the

CREMA collaboration



CREMA collaboration



Charge Radius Experiment with Muonic Atoms



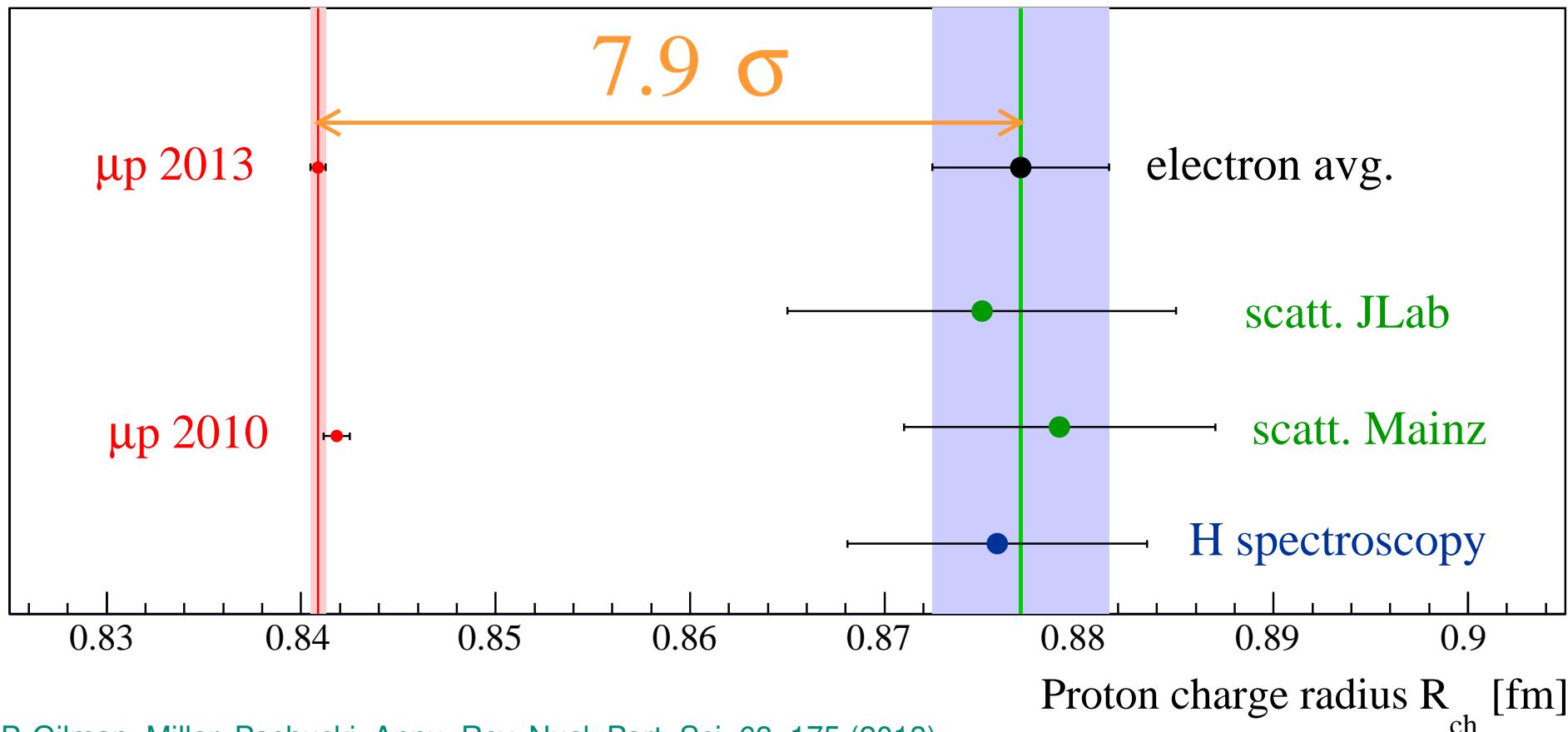
M. Diepold, B. Franke, J. Götzfried, T.W. Hänsch, J. Krauth, F. Mülhauser, T. Nebel, R. Pohl	MPQ, Garching, Germany
A. Antognini, K. Kirch, F. Kottmann , B. Naar, K. Schuhmann, D. Taquu	ETH Zürich, Switzerland
M. Hildebrandt, A. Knecht, A. Dax	PSI, Switzerland
F. Biraben, P. Indelicato, E.-O. Le Bigot, S. Galtier , L. Julien, F. Nez, C. Szabo-Foster	Labor. Kastler Brossel, Paris, France
F.D. Amaro, J.M.R. Cardoso, L.M.P. Fernandes , A.L. Gouveia, J.A.M. Lopez, C.M.B. Monteiro, J.M.F. dos Santos	Uni Coimbra, Portugal
D.S. Covita, J.F.C.A. Veloso	Uni Aveiro, Portugal
M. Abdou Ahmed, T. Graf, A. Voss, B. Weichert	IFSW, Uni Stuttgart, Germany
T.-L. Chen, C.-Y. Kao , Y.-W. Liu	Nat. Tsing Hua Uni, Hsinchu, Taiwan
P. Amaro, J.F.D.C. Machado, J.P. Santos	Uni Lisbon, Portugal
L. Ludhova, P.E. Knowles, L.A. Schaller	Uni Fribourg, Switzerland
A. Giesen	Dausinger & Giesen GmbH, Stuttgart, Germany
P. Rabinowitz	Uni Princeton, USA

The proton radius puzzle

The proton rms charge radius measured with

electrons: 0.8770 ± 0.0045 fm

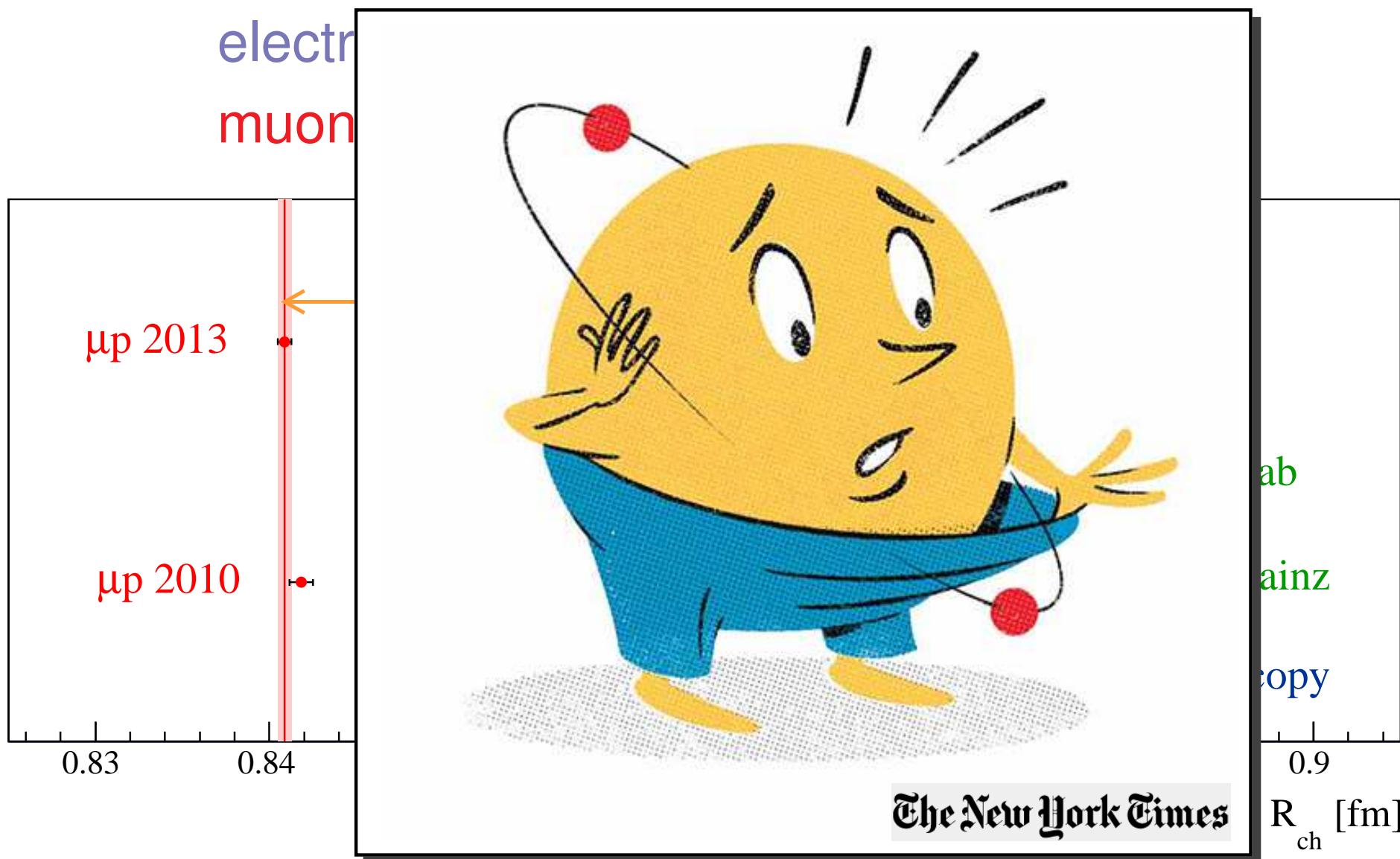
muons: 0.8409 ± 0.0004 fm



RP, Gilman, Miller, Pachucki, Annu. Rev. Nucl. Part. Sci. 63, 175 (2013).

The proton radius puzzle

The proton rms charge radius measured with

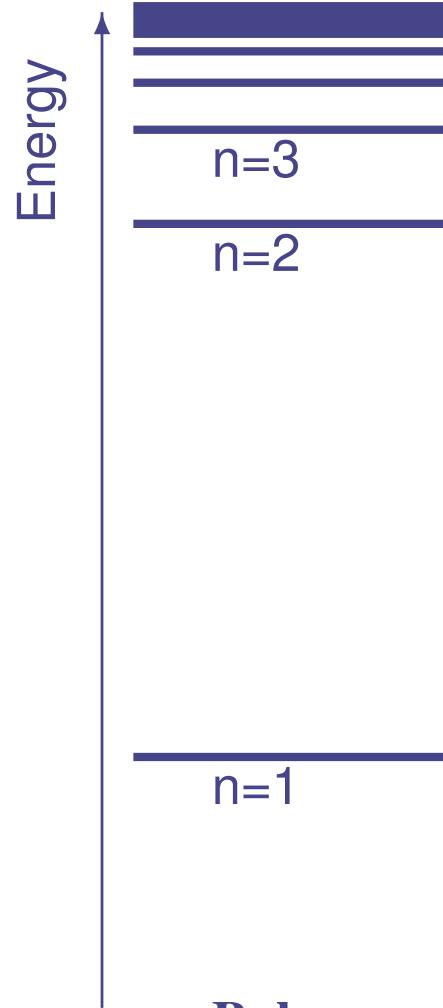


Outline



- Introduction:
 - How large is the proton?
 - Atomic vs. nuclear physics
- Muonic hydrogen:
 - Size does matter!
- Experiment:
 - Principle
 - Muon beam
 - Laser system
- The “Proton Radius Puzzle”
- New measurements:
 - Regular hydrogen
 - **Muonic deuterium**
 - **Muonic helium**

Hydrogen

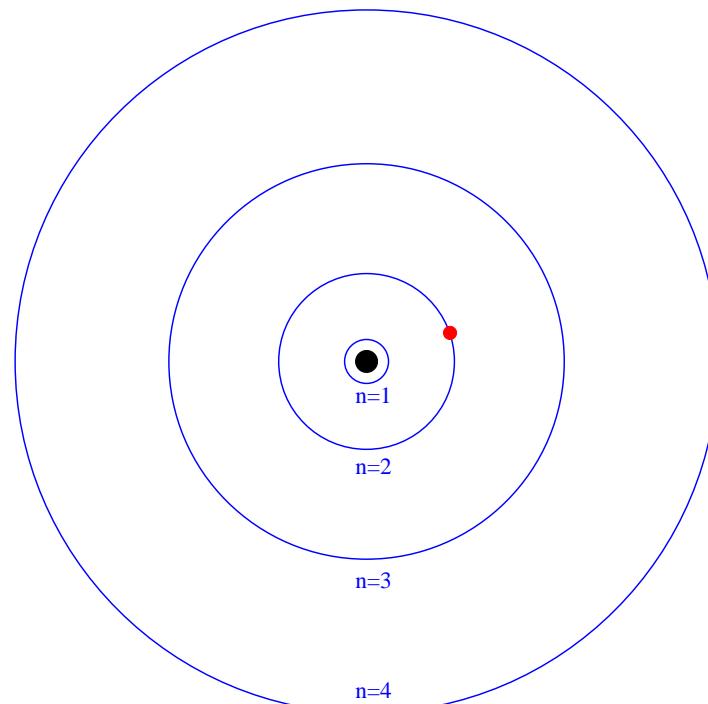


Bohr

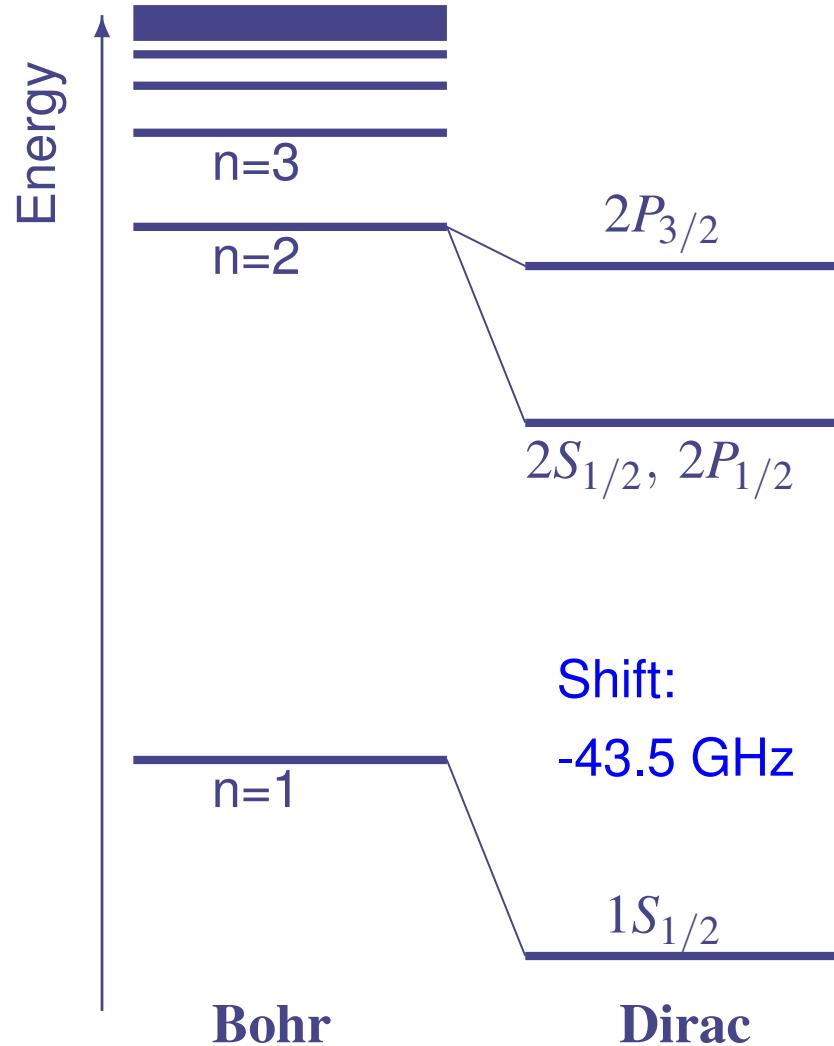
$$E = R_\infty / n^2$$

$$V \sim 1/r$$

Bohr model of the hydrogen atom



Hydrogen

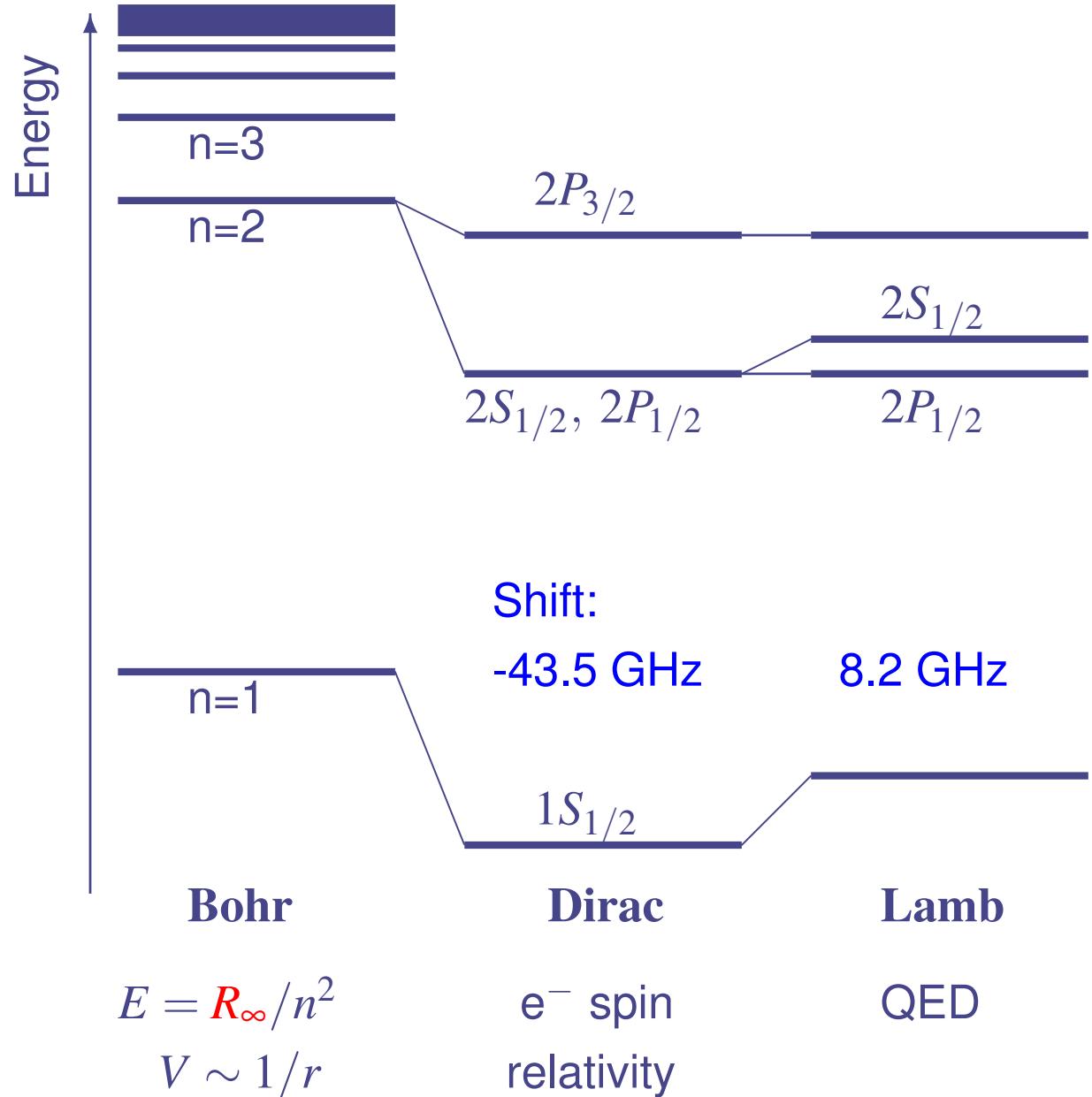


$$E = R_\infty / n^2$$

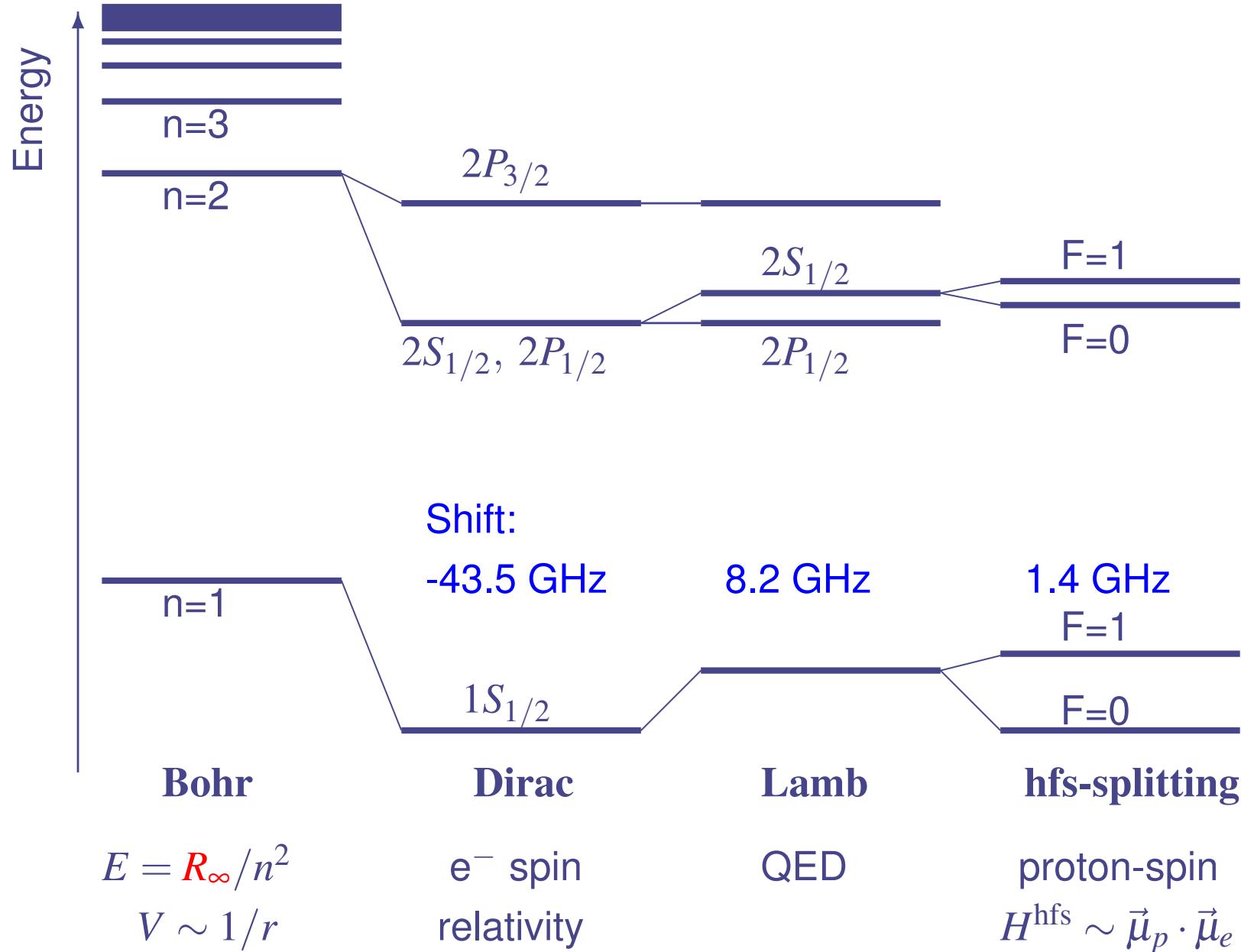
$$V \sim 1/r$$

e⁻ spin
relativity

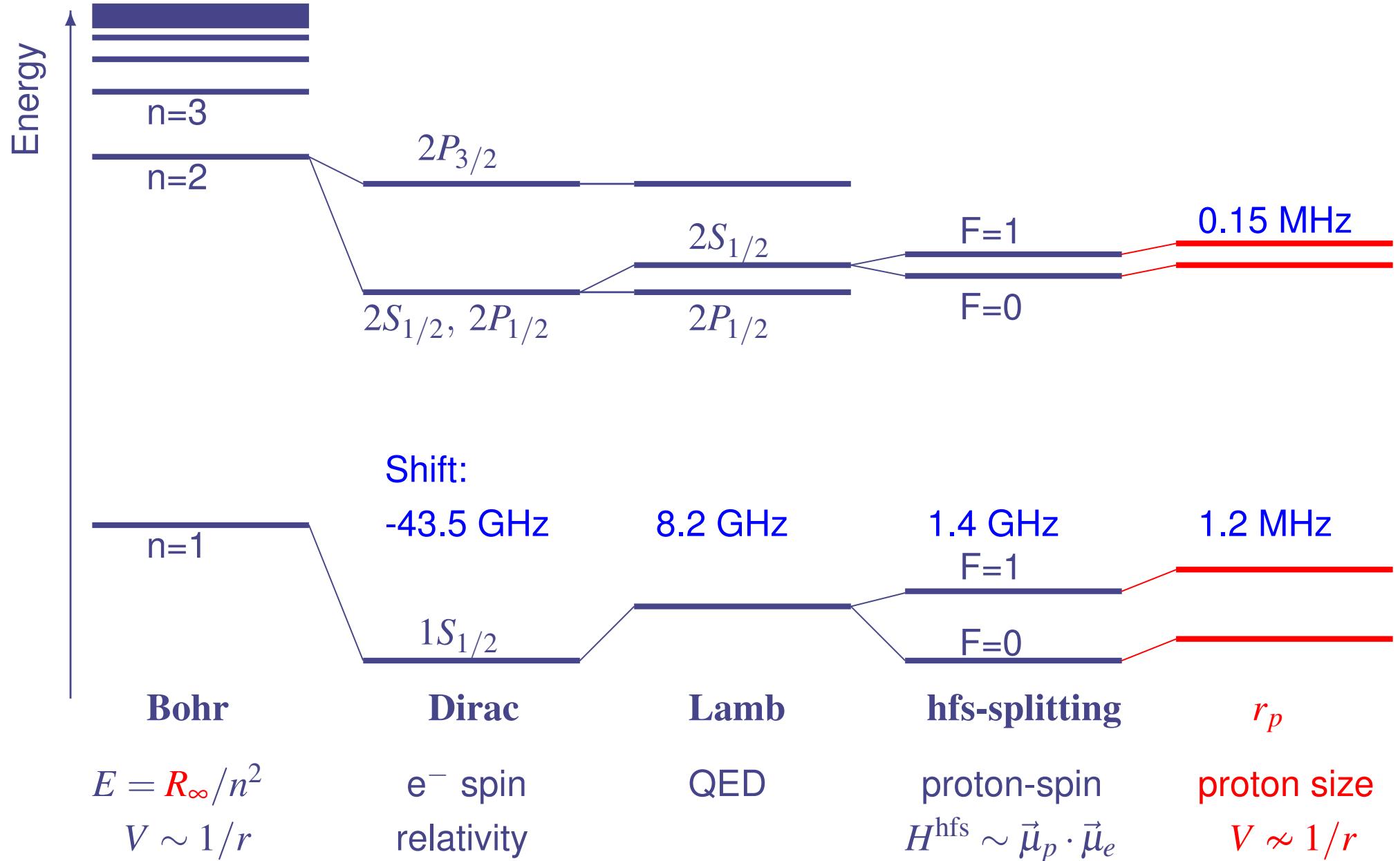
Hydrogen



Hydrogen

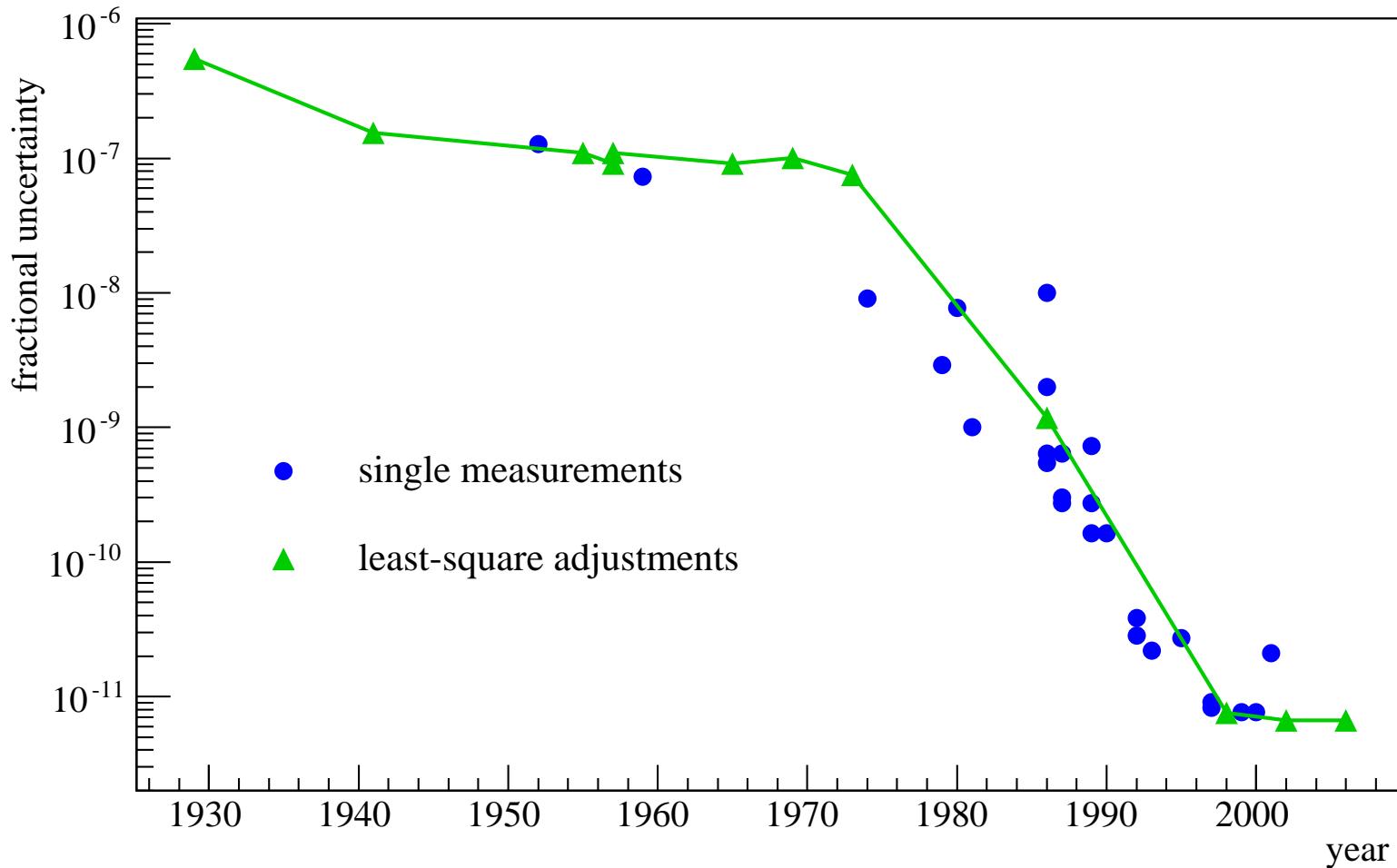


Hydrogen



The Rydberg constant

Accuracy of the Rydberg constant

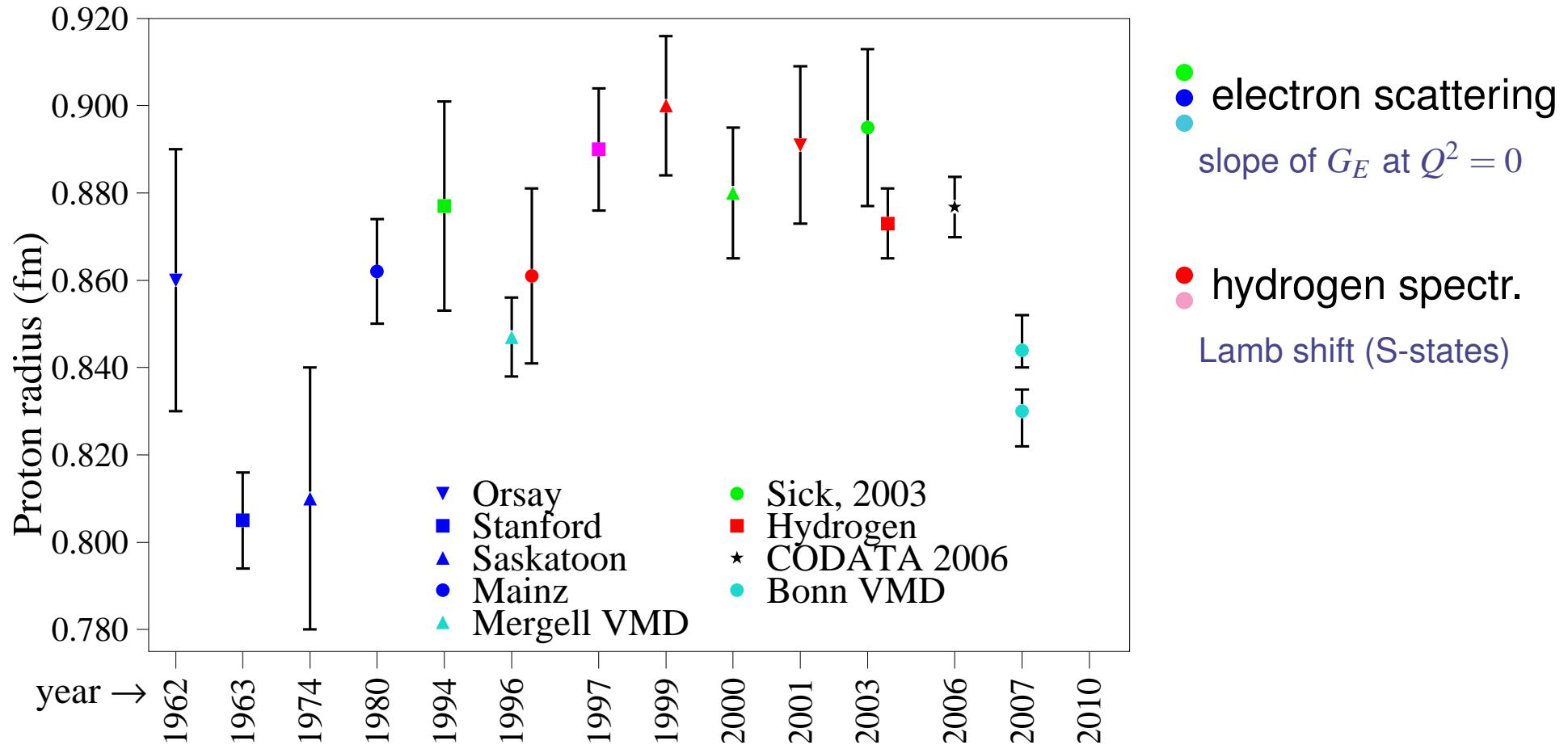


$$2010: R_\infty = 10973\,731.568\,539 \pm 0.000\,055 \text{ m}^{-1} (u_r = 5.0 \cdot 10^{-12})$$

is the **most accurately determined** fundamental constant.

Proton radius vs. time

The proton rms charge radius is not the most accurate quantity in the universe.

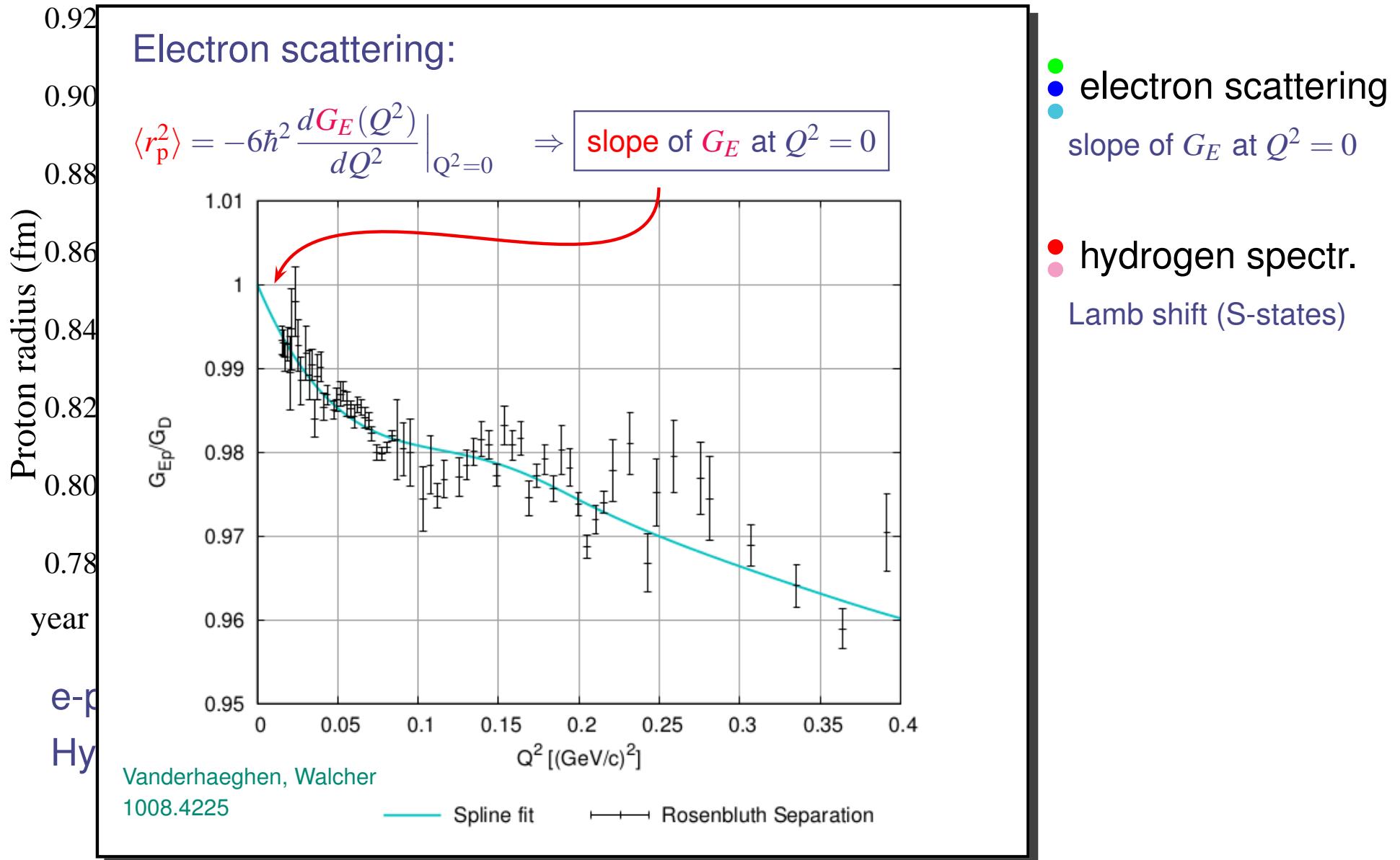


$$e\text{-}p \text{ scattering: } r_p = 0.895(18) \text{ fm } (u_r = 2 \%)$$

$$\text{Hydrogen: } r_p = 0.8760(78) \text{ fm } (u_r = 0.9 \%)$$

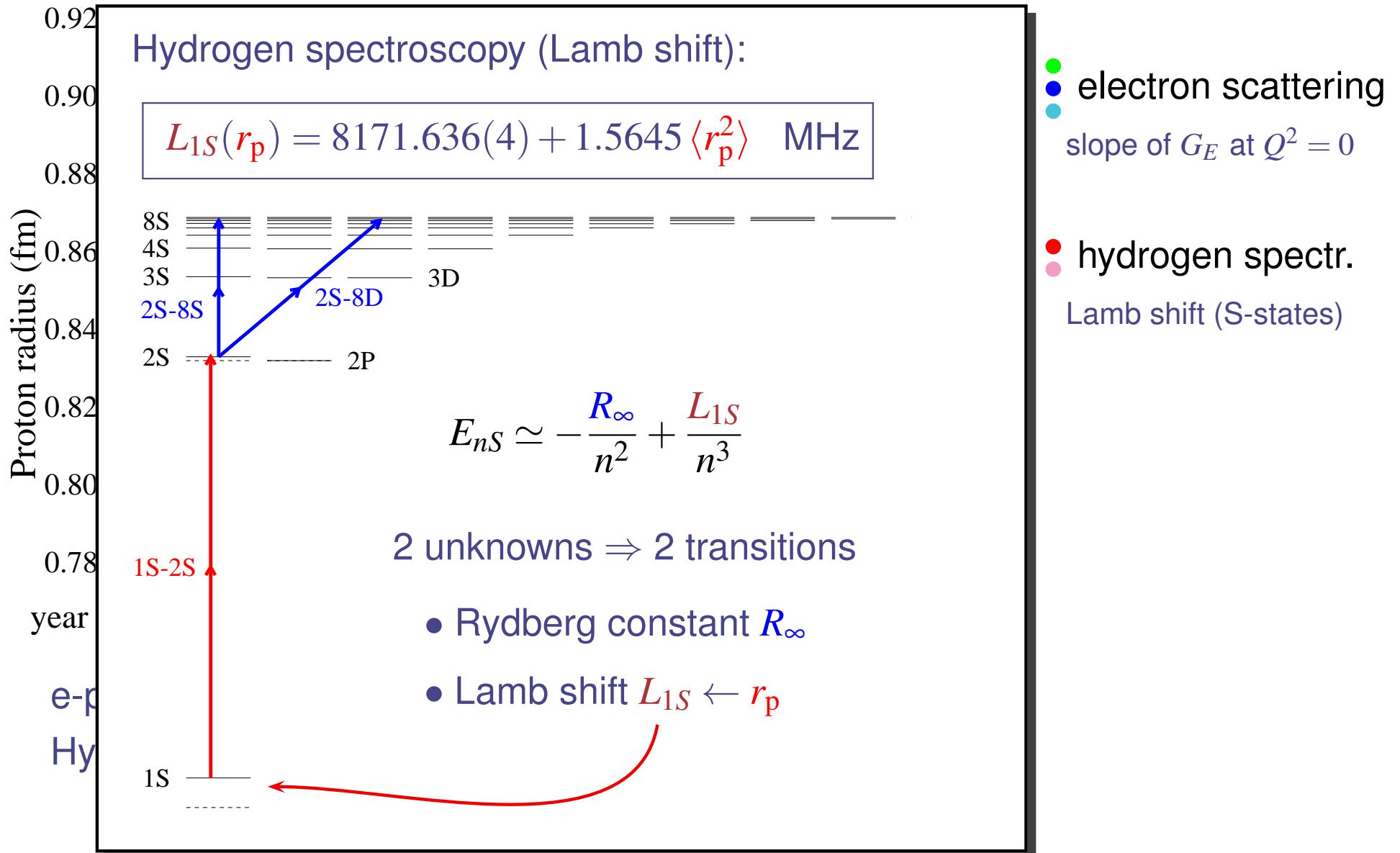
Proton radius vs. time

The proton rms charge radius is not the most accurate quantity in the universe.



Proton radius vs. time

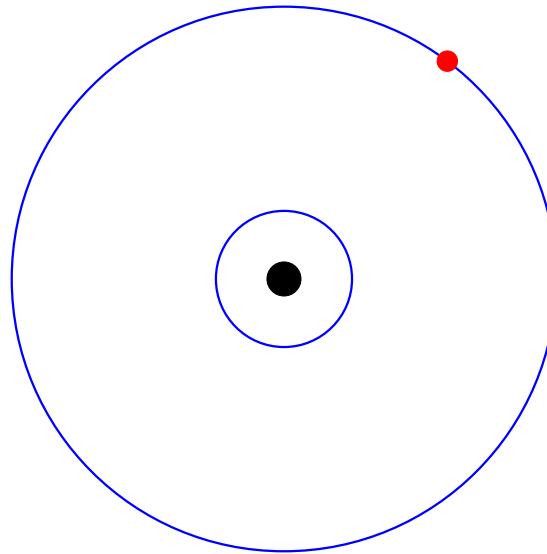
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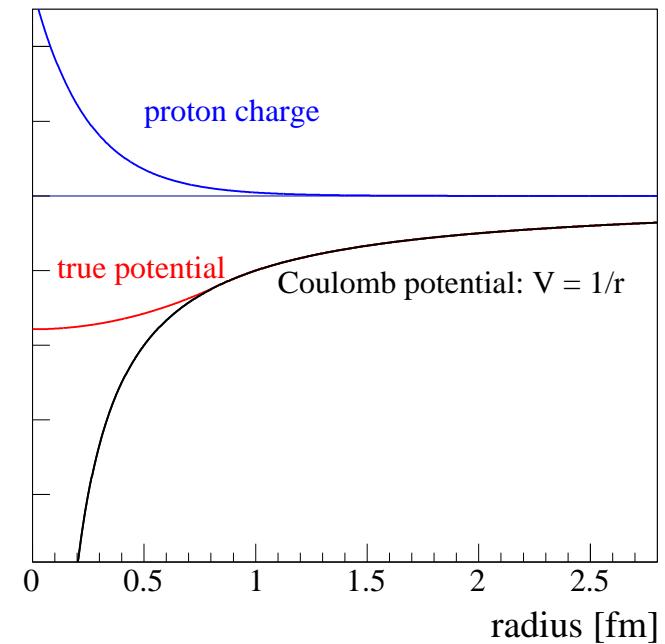
Atomic physics

Bohr model of the atom

- Electrons orbit the nucleus
“Planetary system”
- Hydrogen: 1 electron + 1 proton



Atomic physics



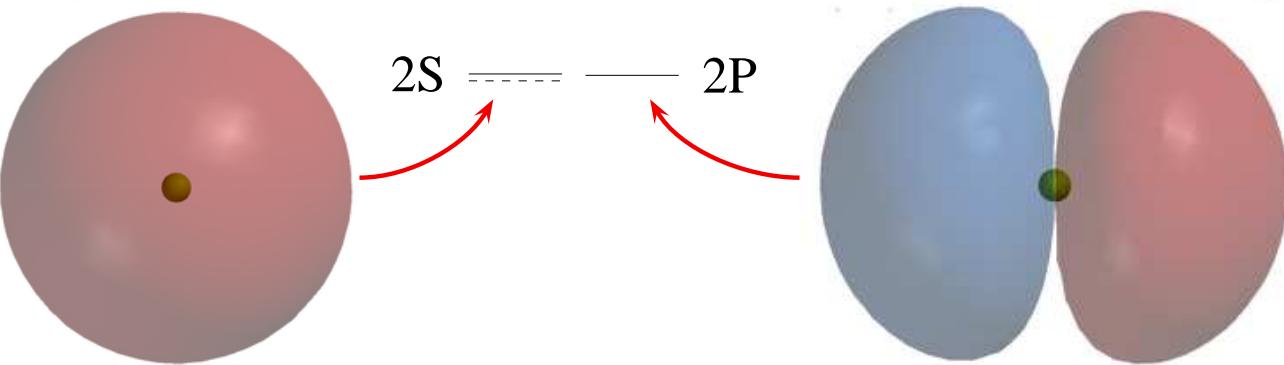
S states: max. at $r=0$

Electron sometimes **inside** the proton.

S states are **less bound**.

Shift ist proportional to the

size of the proton



P states: zero at $r=0$

Electron is **not** inside the proton.



Orbital pictures from Wikipedia

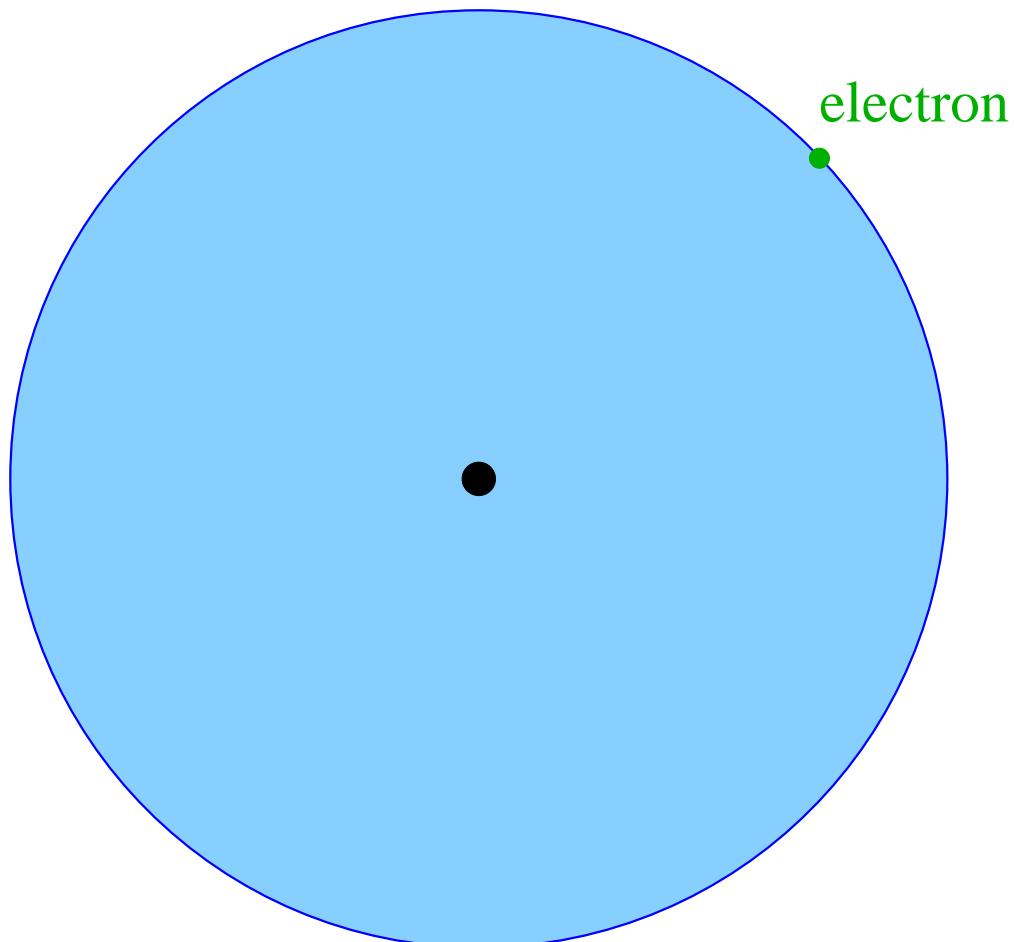
Muonic hydrogen

Regular hydrogen:

electron e^- + proton p

Muonic hydrogen:

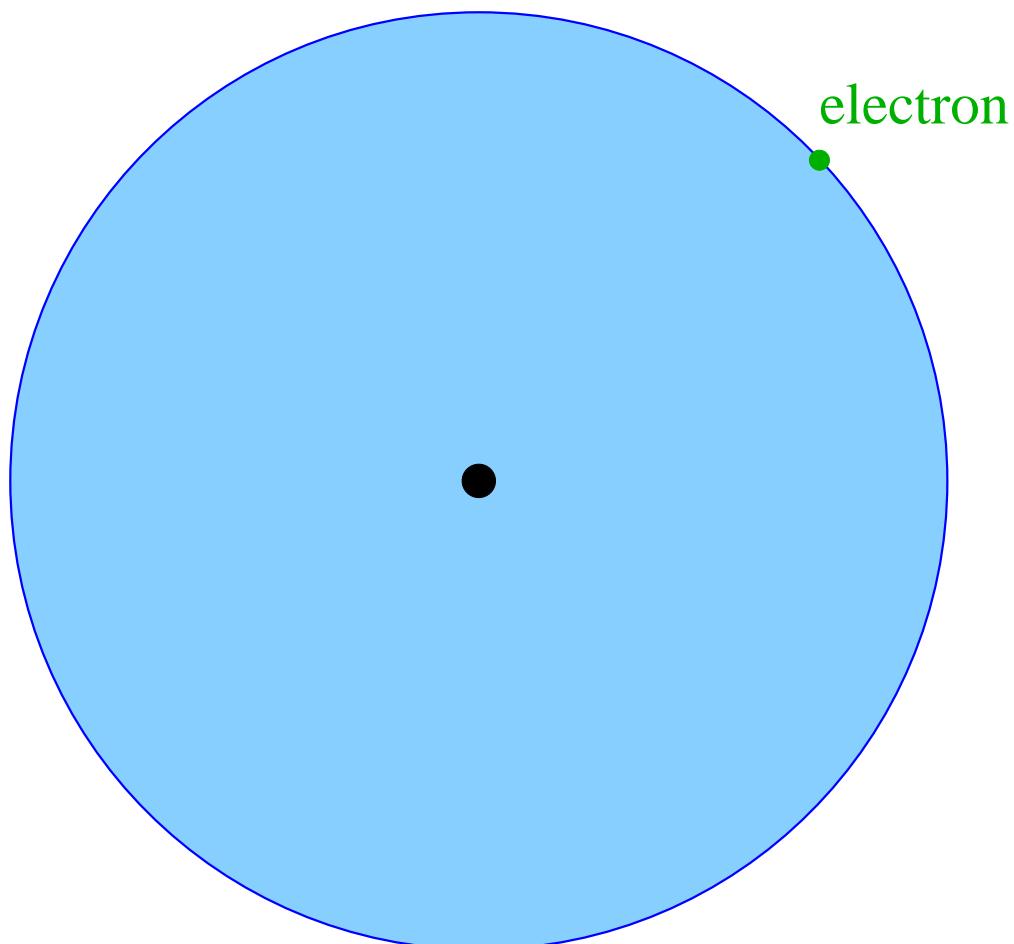
muon μ^- + proton p



Muonic hydrogen

Regular hydrogen:

electron e^- + proton p



Muonic hydrogen:

muon μ^- + proton p

Drei Generationen der Materie (Fermionen)			
I Masse → 2,4 MeV	II Ladung → $\frac{2}{3}$	III Spin → $\frac{1}{2}$	0 Name → γ
U up	C $\frac{2}{3}$	t $\frac{1}{2}$	Photon
d down	s $\frac{1}{2}$	b $\frac{1}{2}$	g Gluon
ν_e Elektron-Neutrino	ν_μ Myon-Neutrino	ν_τ Tau-Neutrino	Z^0 schwache Kraft
e Elektron	μ Myon	τ Tau	W^\pm schwache Kraft

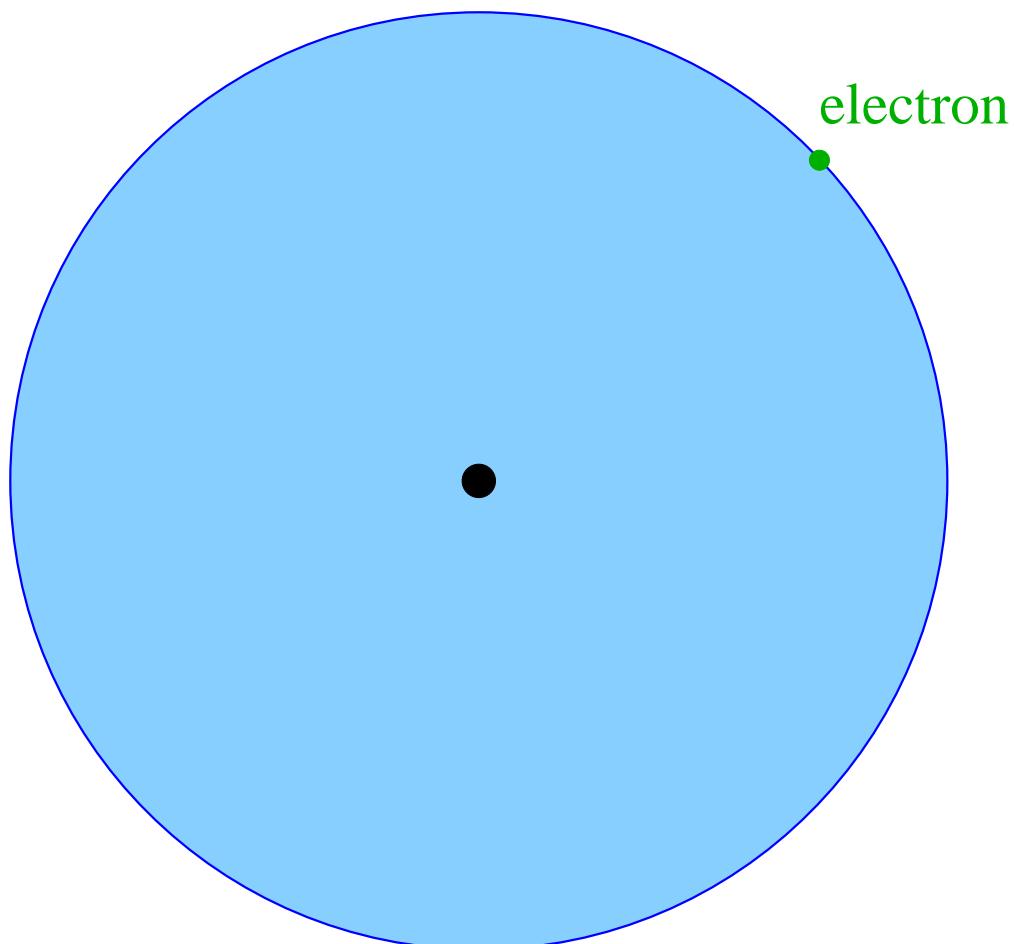
Quarks
Leptonen
Eichbosonen

from Wikipedia

Muonic hydrogen

Regular hydrogen:

electron e^- + proton p



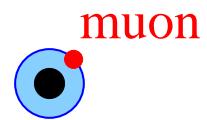
Muonic hydrogen:

muon μ^- + proton p

muon mass $m_\mu \approx 200 \times m_e$

Bohr radius $r_\mu \approx 1/200 \times r_e$

μ inside the proton: $200^3 \approx 10^7$



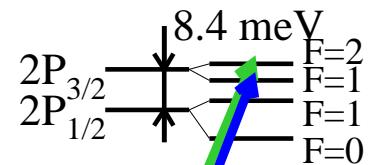
muon much more sensitive to r_p

Proton charge radius and muonic hydrogen

Lamb shift in μp [meV]:

$$\Delta E = 206.0668(25) - 5.2275(10) r_p^2 \text{ [meV]}$$

$\mu p(n=2)$ levels:



Proton size effect is **2%** of the μp Lamb shift

Measure to 10^{-5} \Rightarrow r_p to 0.05 %

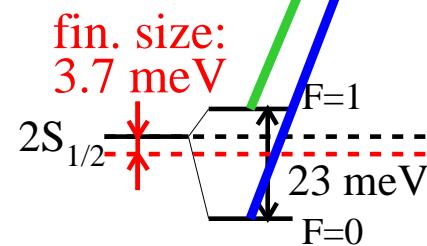
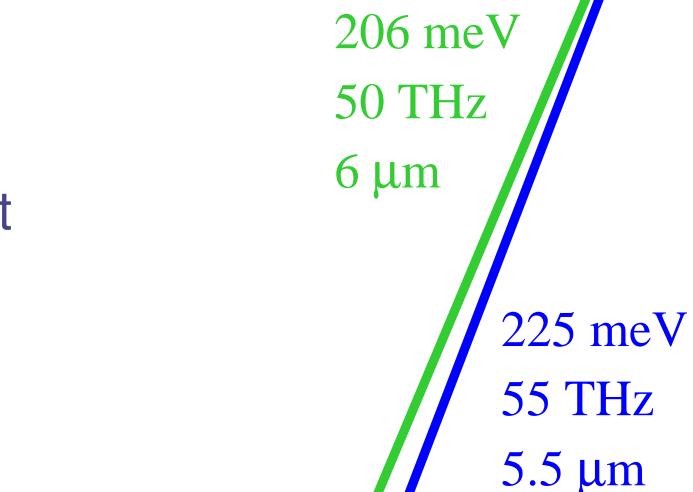
Experiment:

R. Pohl *et al.*, Nature 466, 213 (2010).

A. Antognini, RP *et al.*, Science 339, 417 (2013).

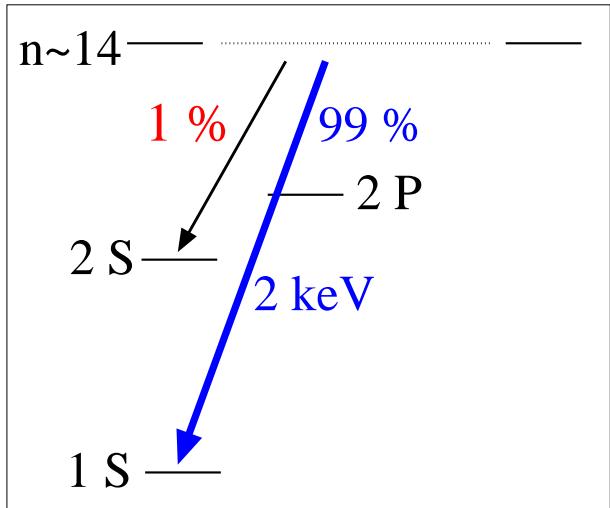
Theory summary:

A. Antognini, RP *et al.*, Ann. Phys. 331, 127 (2013).



μp Lamb shift experiment: Principle

“prompt” ($t \sim 0$)



μ^- stop in H_2 gas
 $\Rightarrow \mu p^*$ atoms formed ($n \sim 14$)

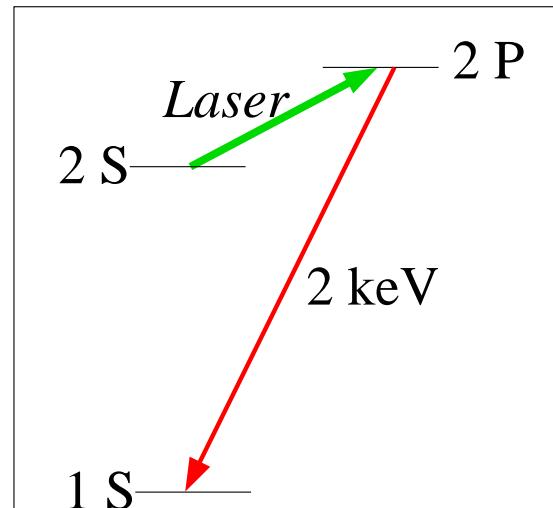
99%: cascade to $\mu p(1\text{S})$,
emitting **prompt** $K_\alpha, K_\beta \dots$

1%: long-lived $\mu p(2\text{S})$ atoms

lifetime $\tau_{2S} \approx 1\text{ }\mu\text{s}$ at 1 mbar H_2

RP *et. al.*, Phys. Rev. Lett. 97, 193402 (2006).

“delayed” ($t \sim 1\text{ }\mu\text{s}$)



fire **laser** ($\lambda \approx 6\text{ }\mu\text{m}$, $\Delta E \approx 0.2\text{ eV}$)

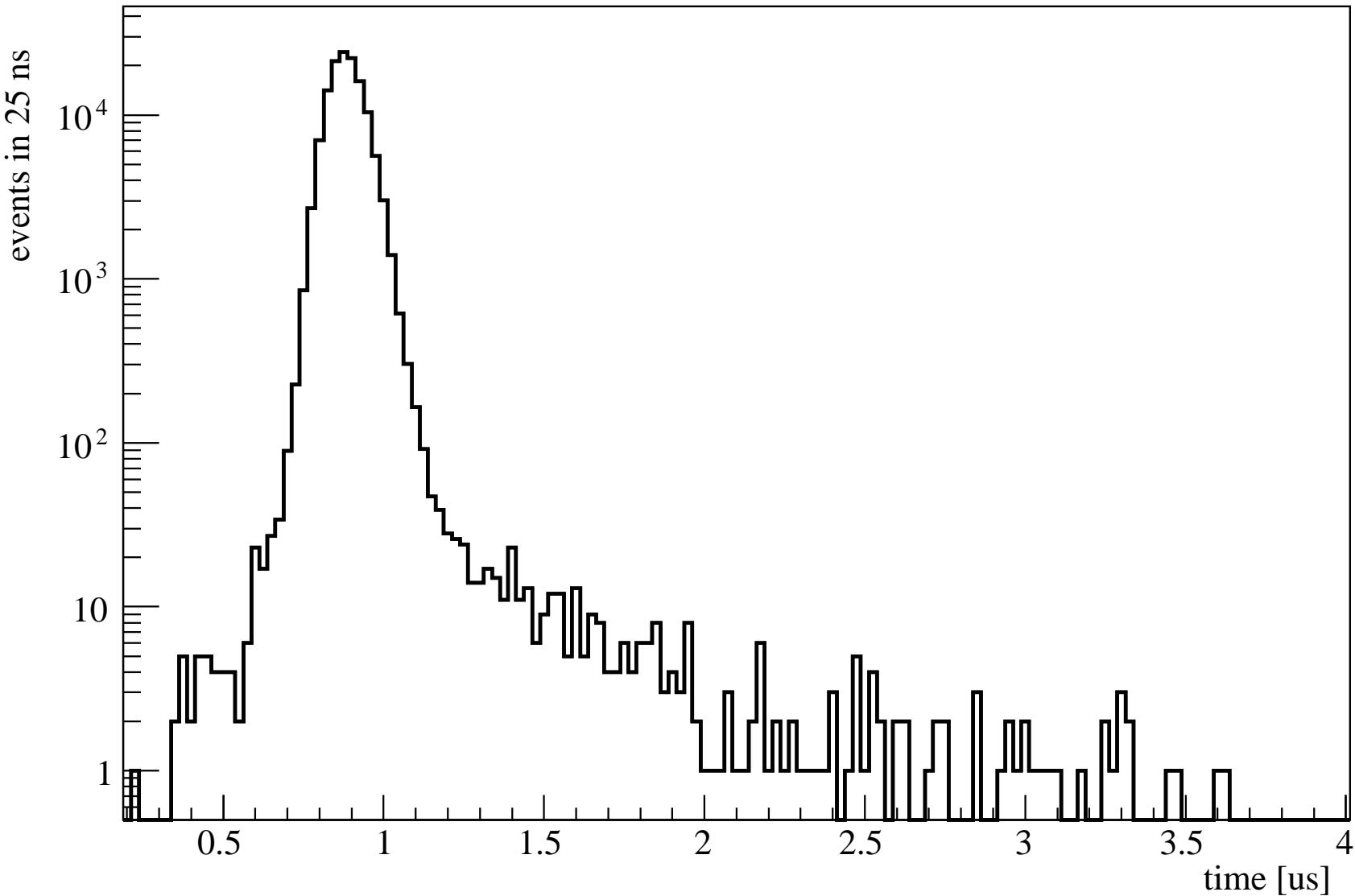
\Rightarrow induce $\mu p(2\text{S}) \rightarrow \mu p(2\text{P})$

\Rightarrow observe **delayed** K_α x-rays

\Rightarrow normalize $\frac{\text{delayed } K_\alpha}{\text{prompt } K_\alpha}$ x-rays

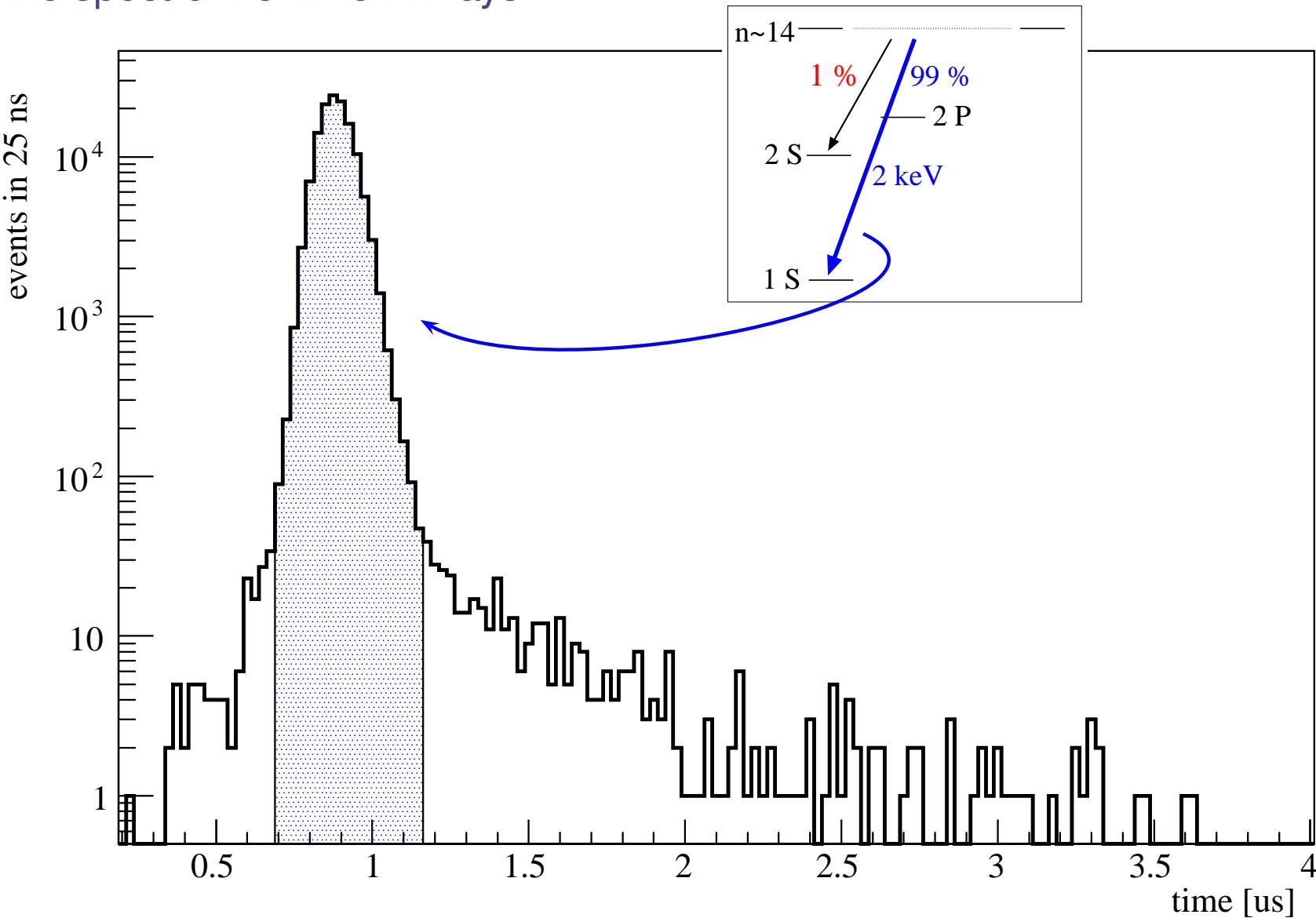
μ p Lamb shift experiment: Principle

time spectrum of 2 keV x-rays (\sim 13 hours of data @ 1 laser wavelength)



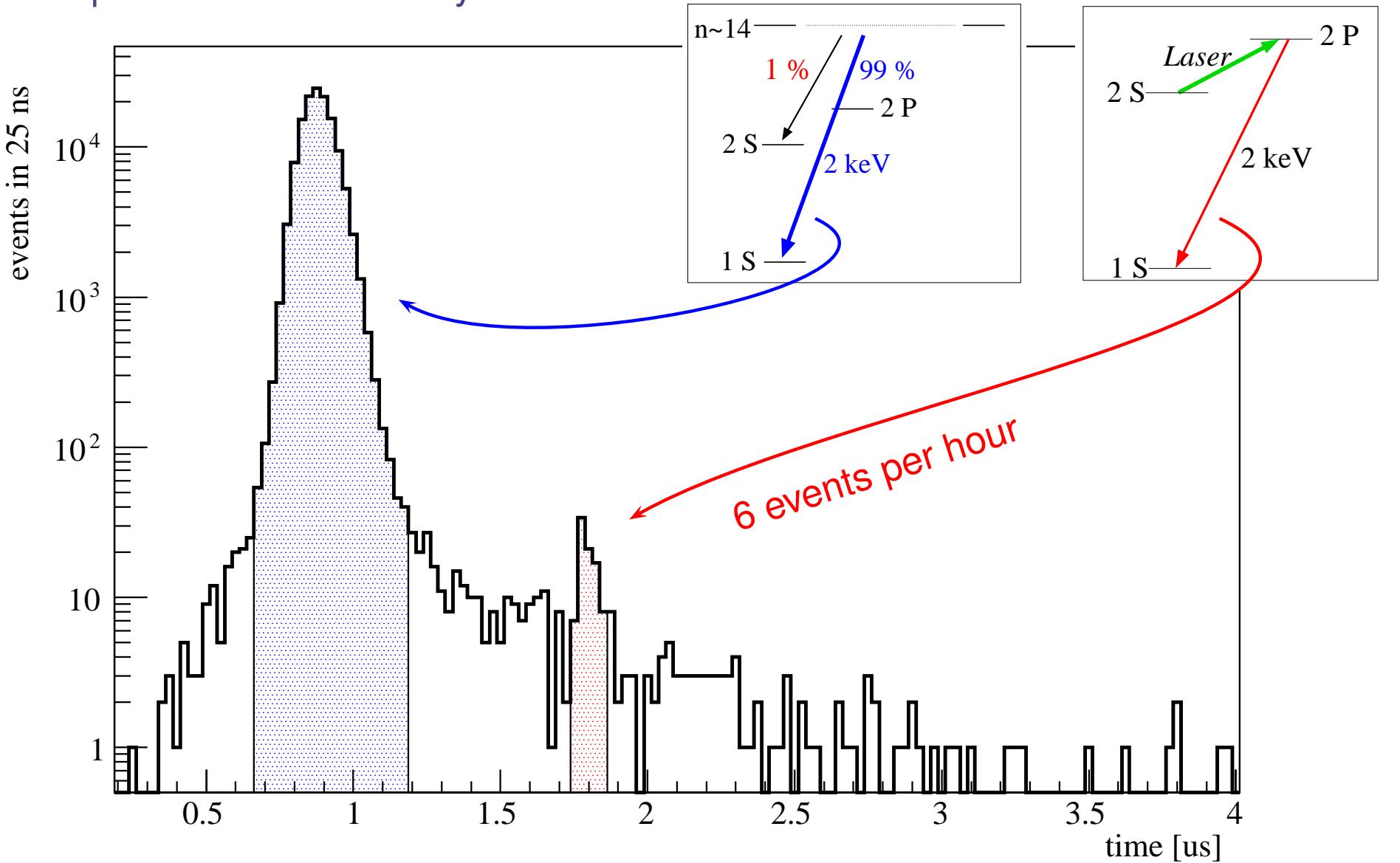
μ p Lamb shift experiment: Principle

time spectrum of 2 keV x-rays



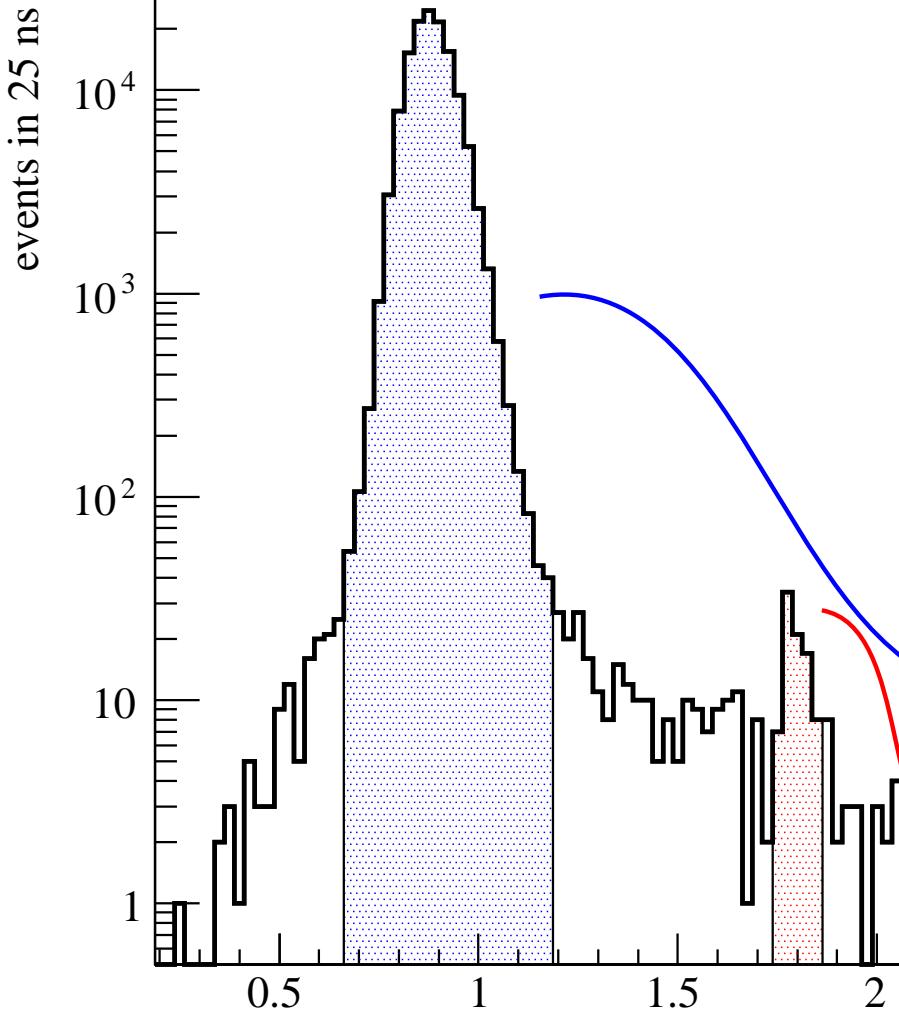
μ p Lamb shift experiment: Principle

time spectrum of 2 keV x-rays

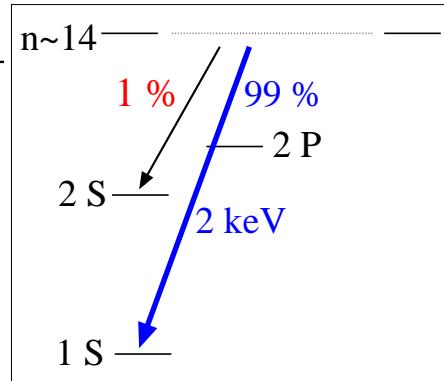


μ p Lamb shift experiment: Principle

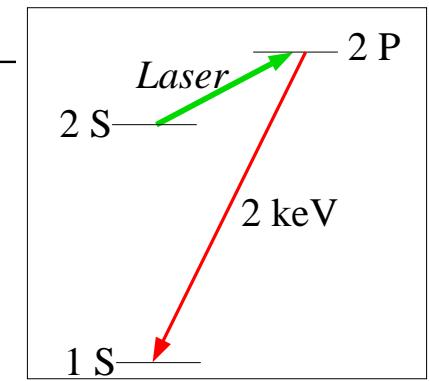
time spectrum of 2 keV x-rays



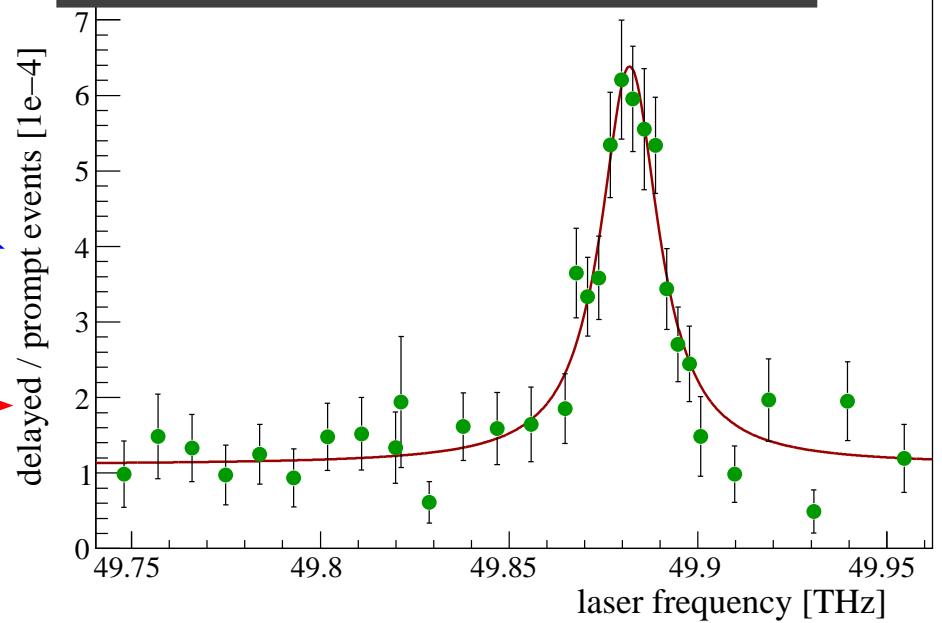
"prompt" ($t \sim 0$)



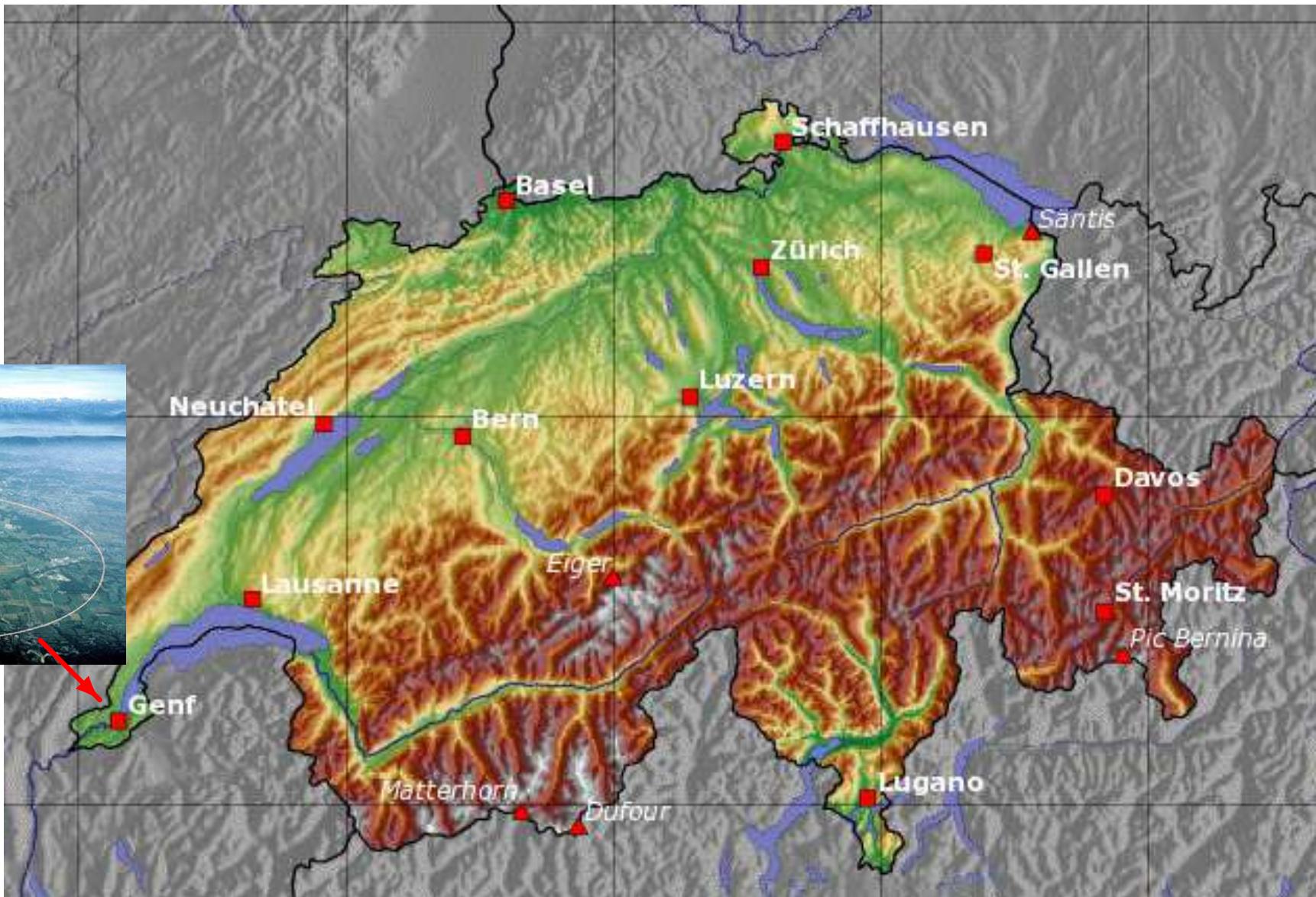
"delayed" ($t \sim 1 \mu\text{s}$)



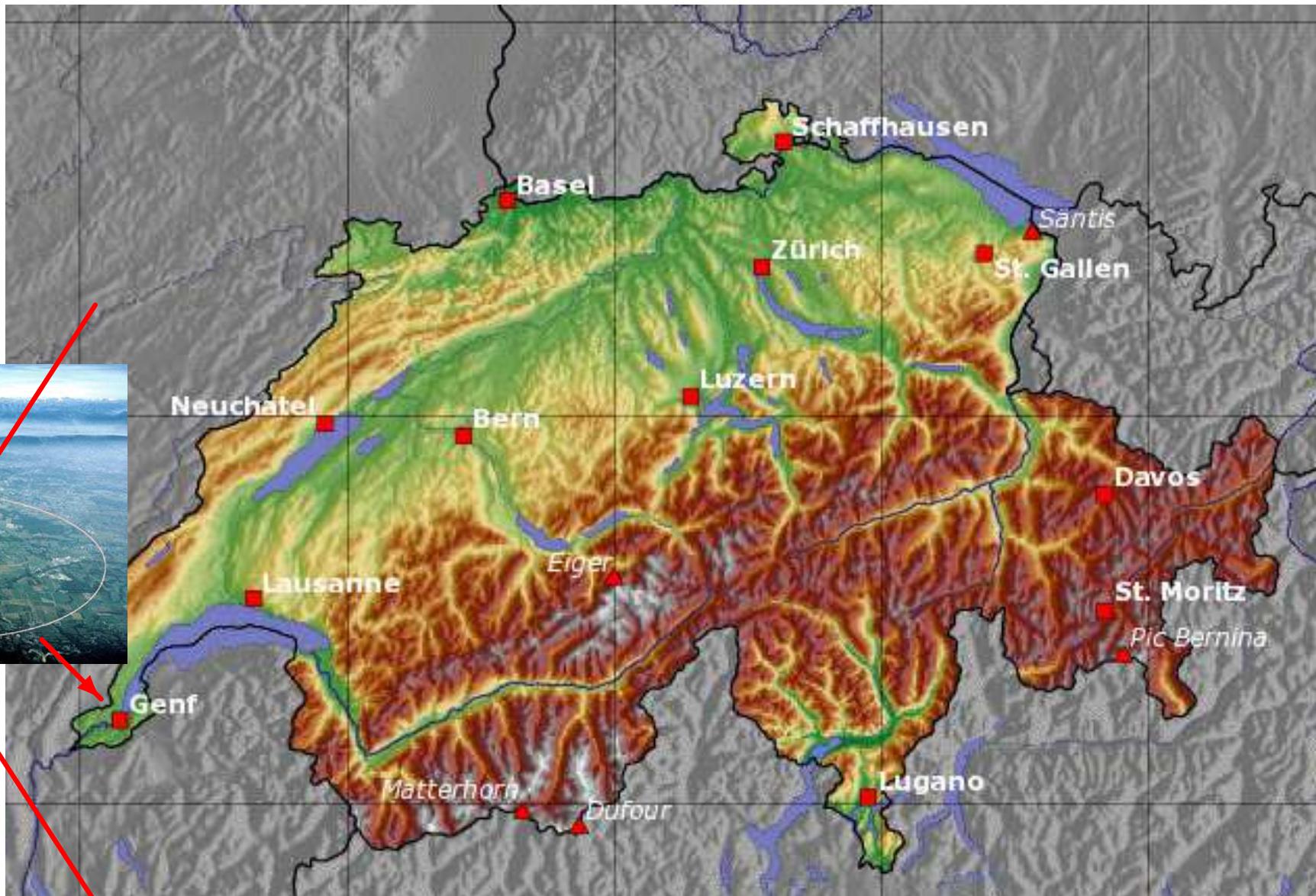
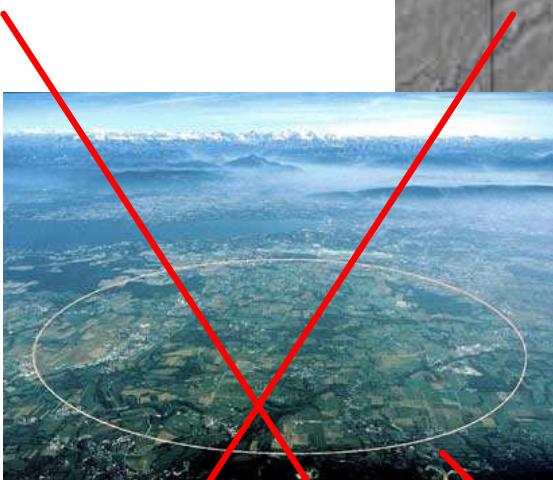
normalize $\frac{\text{delayed } K_{\alpha}}{\text{prompt } K_{\alpha}}$ \Rightarrow Resonance



Swiss muons



Swiss muons

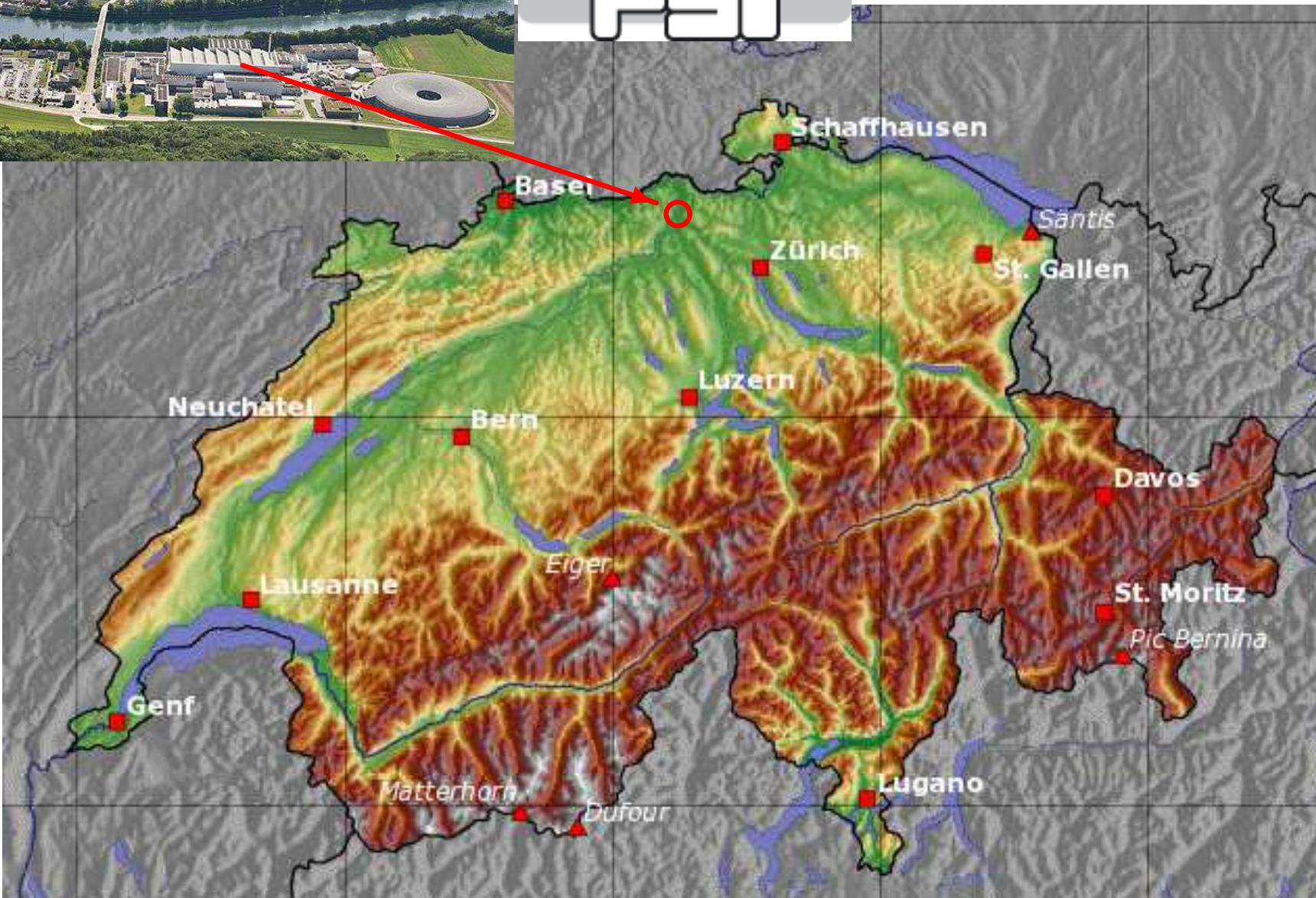


Swiss muons

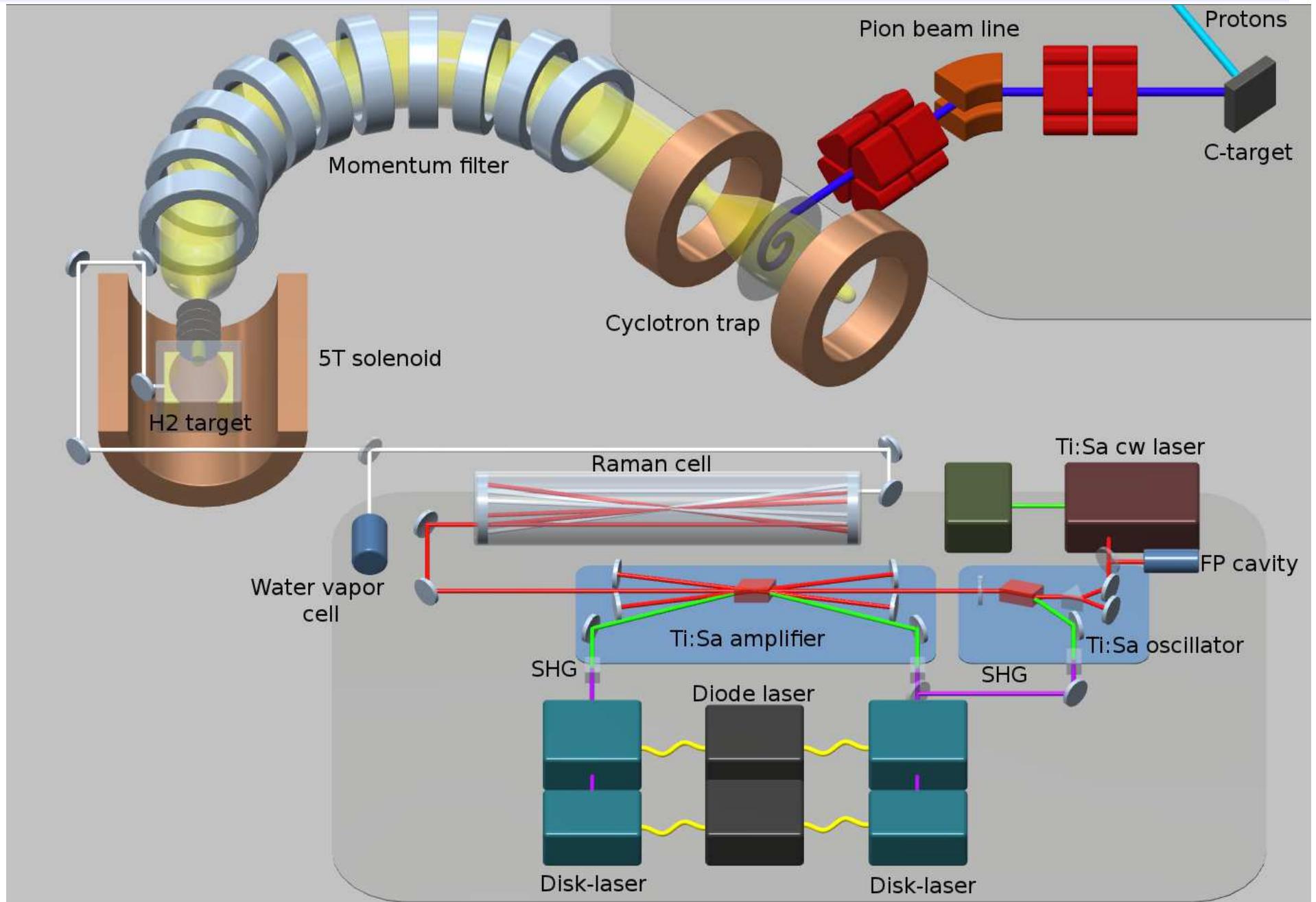


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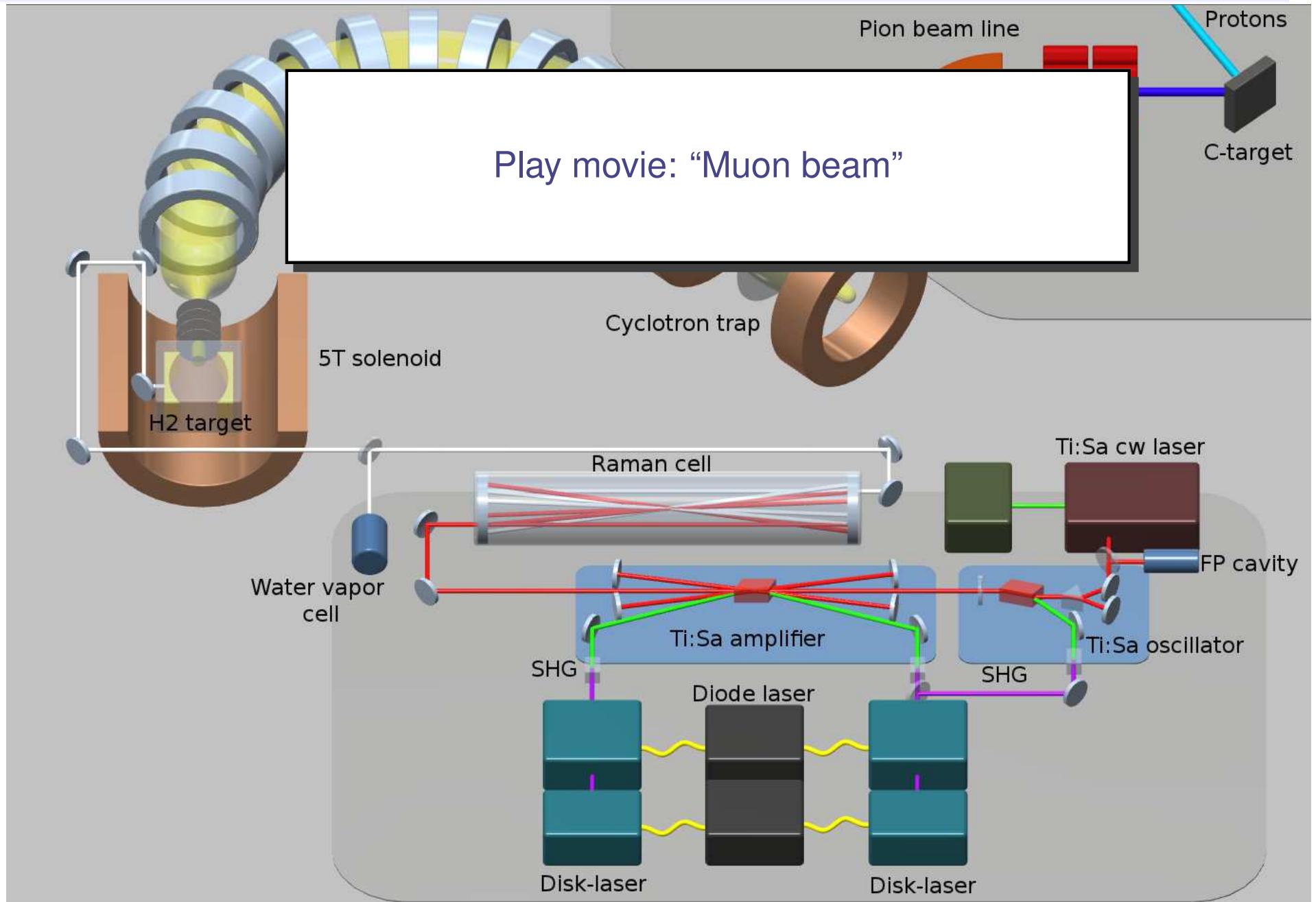
PSI



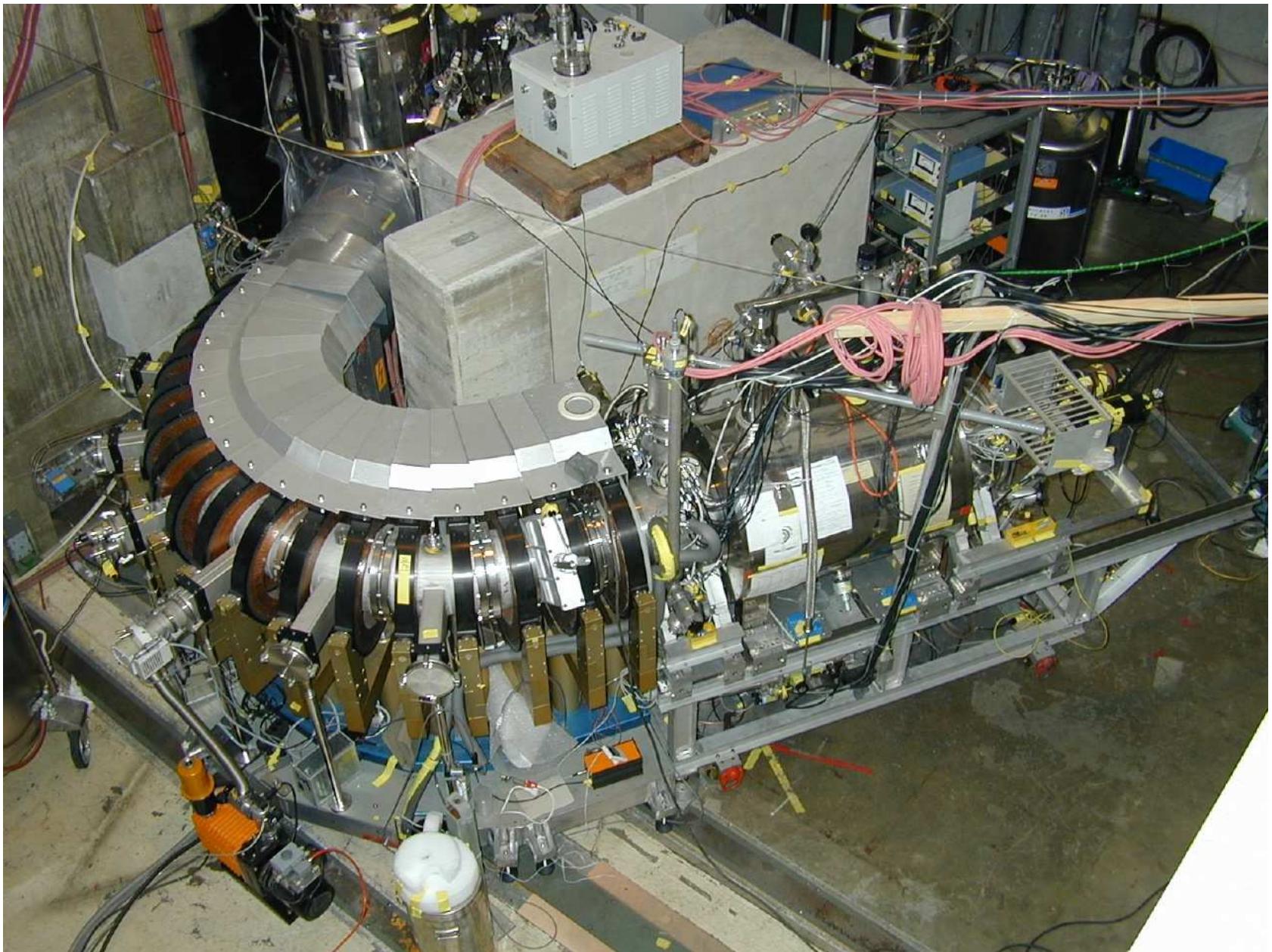
Setup



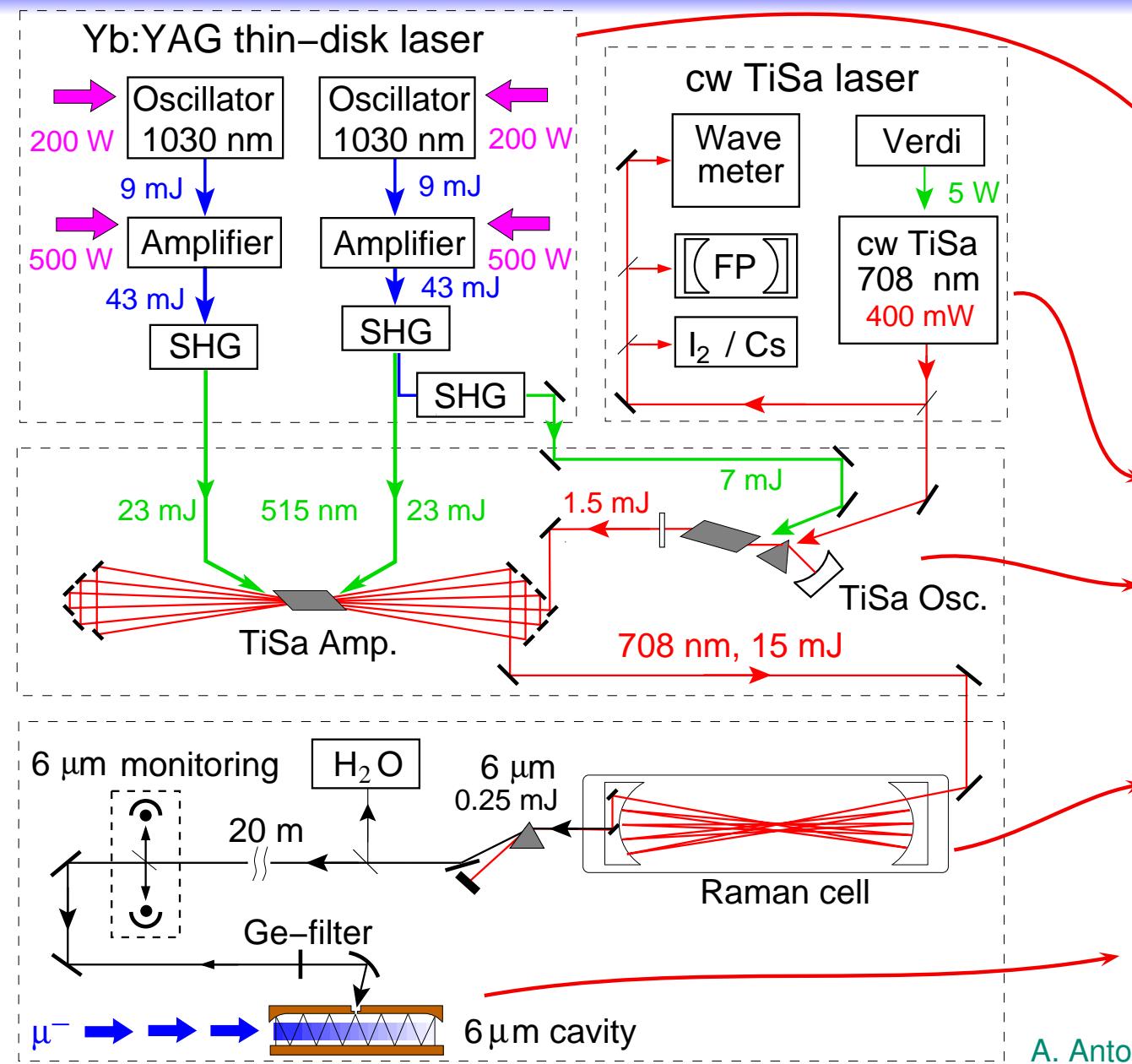
Setup



Muon beam line



The laser system

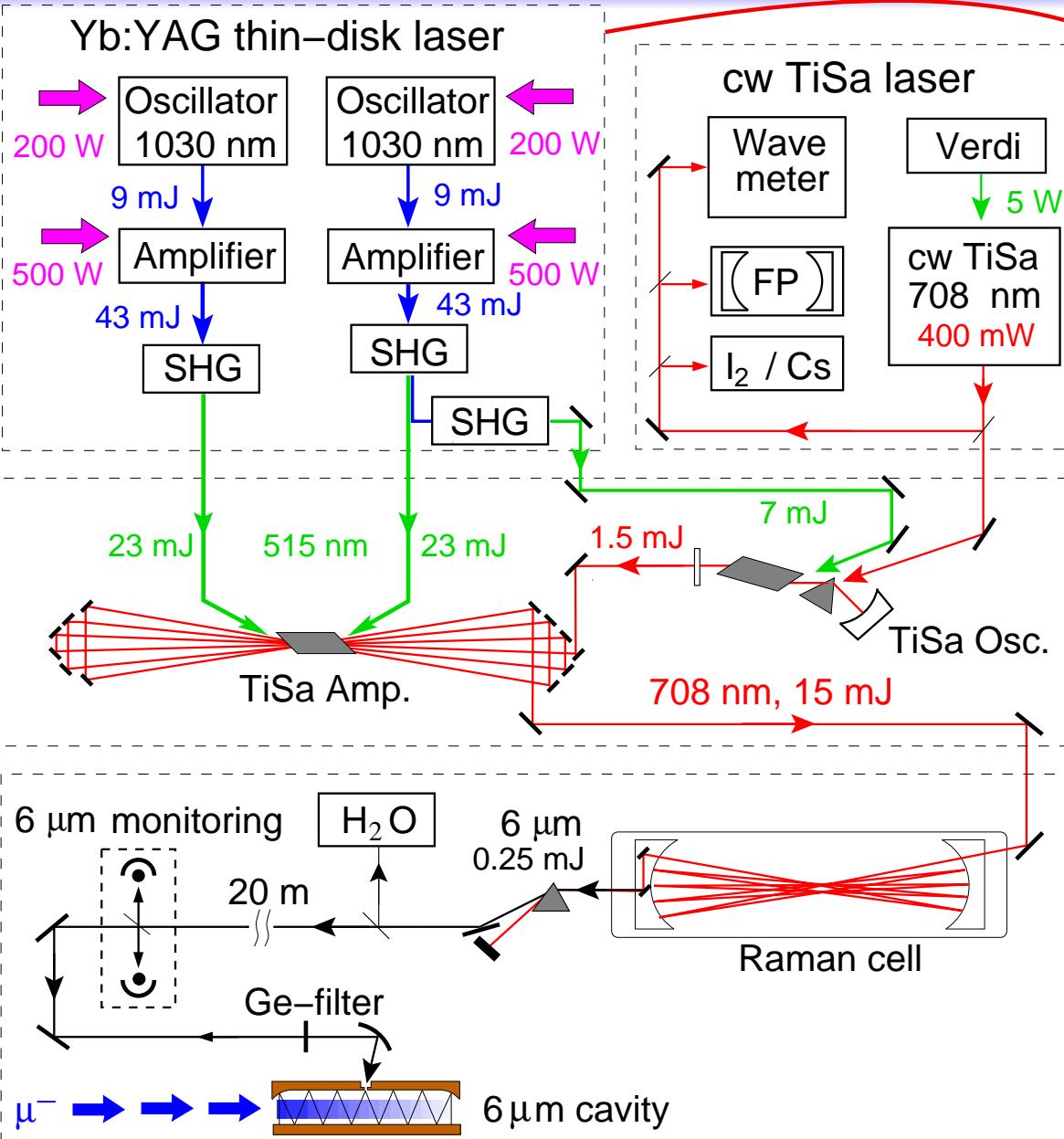


Main components:

- Thin-disk laser
fast response to detected μ^-
- Frequency doubling
- TiSa laser:
frequency stabilized cw laser
injection seeded oscillator
multipass amplifier
- Raman cell
3 Stokes: $708 \text{ nm} \rightarrow 6 \mu\text{m}$
 λ calibration @ $6 \mu\text{m}$
- Target cavity

A. Antognini, RP et. al., Opt. Comm. 253, 362 (2005).

The laser system



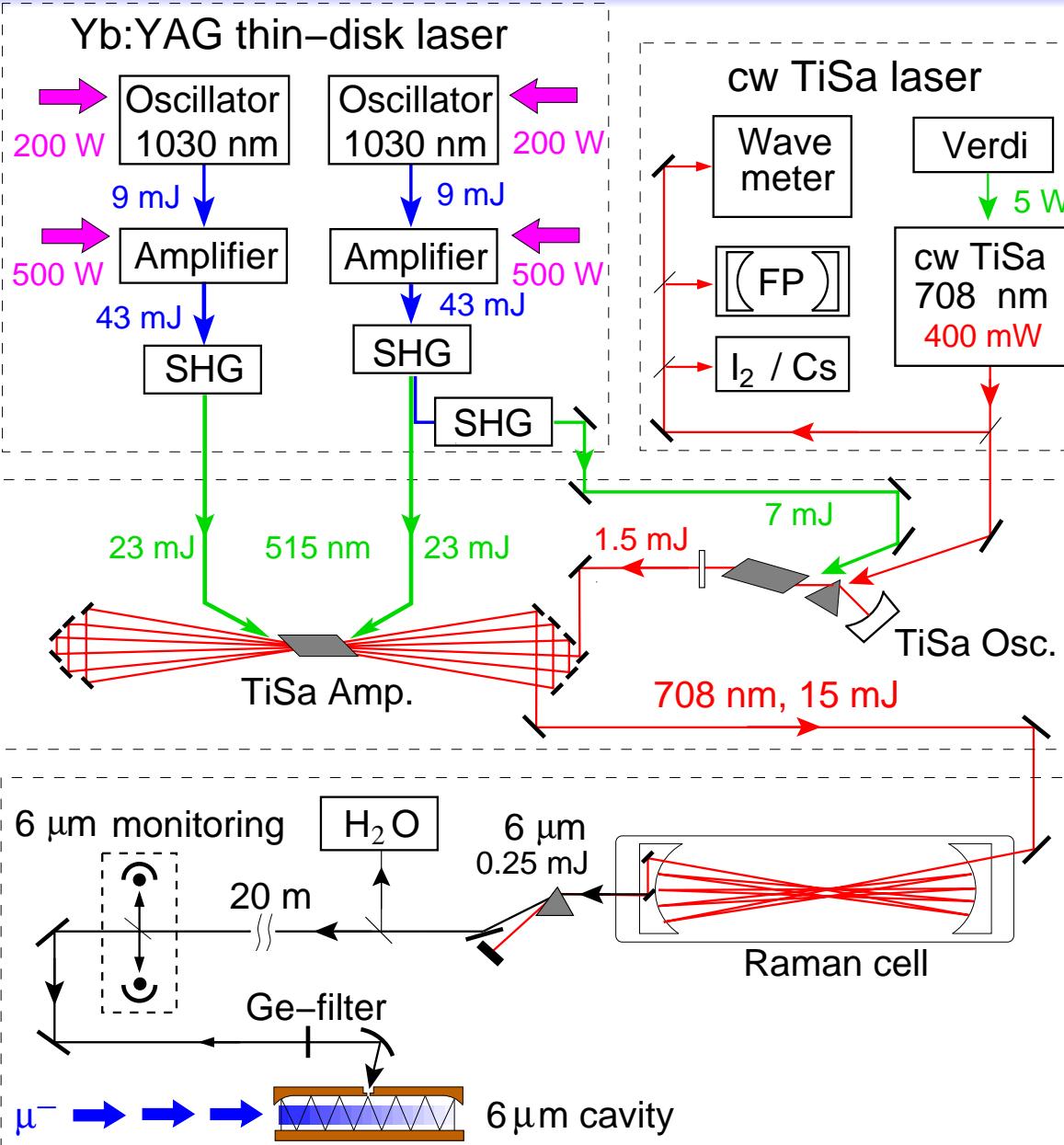
Thin-disk laser

- Large pulse energy: 85 (160) mJ
- Short trigger-to-pulse delay: $\lesssim 400$ ns
- Random trigger
- Pulse-to-pulse delays down to 2 ms
(rep. rate $\gtrsim 500$ Hz)

- Each single μ^- triggers the laser system
- 2S lifetime $\approx 1 \mu\text{s} \rightarrow$ short laser delay

A. Antognini, RP *et. al.*,
IEEE J. Quant. Electr. 45, 993 (2009).

The laser system



MOPA TiSa laser:

cw laser, frequency stabilized

- referenced to a stable FP cavity
- FP cavity calibrated with I₂, Rb, Cs lines

$$v_{\text{FP}} = N \cdot FSR$$

$$FSR = 1497.344(6) \text{ MHz}$$

$v_{\text{TiSa}}^{\text{cw}}$ absolutely known to 30 MHz

$$\Gamma_{2P-2S} = 18.6 \text{ GHz}$$

Seeded oscillator

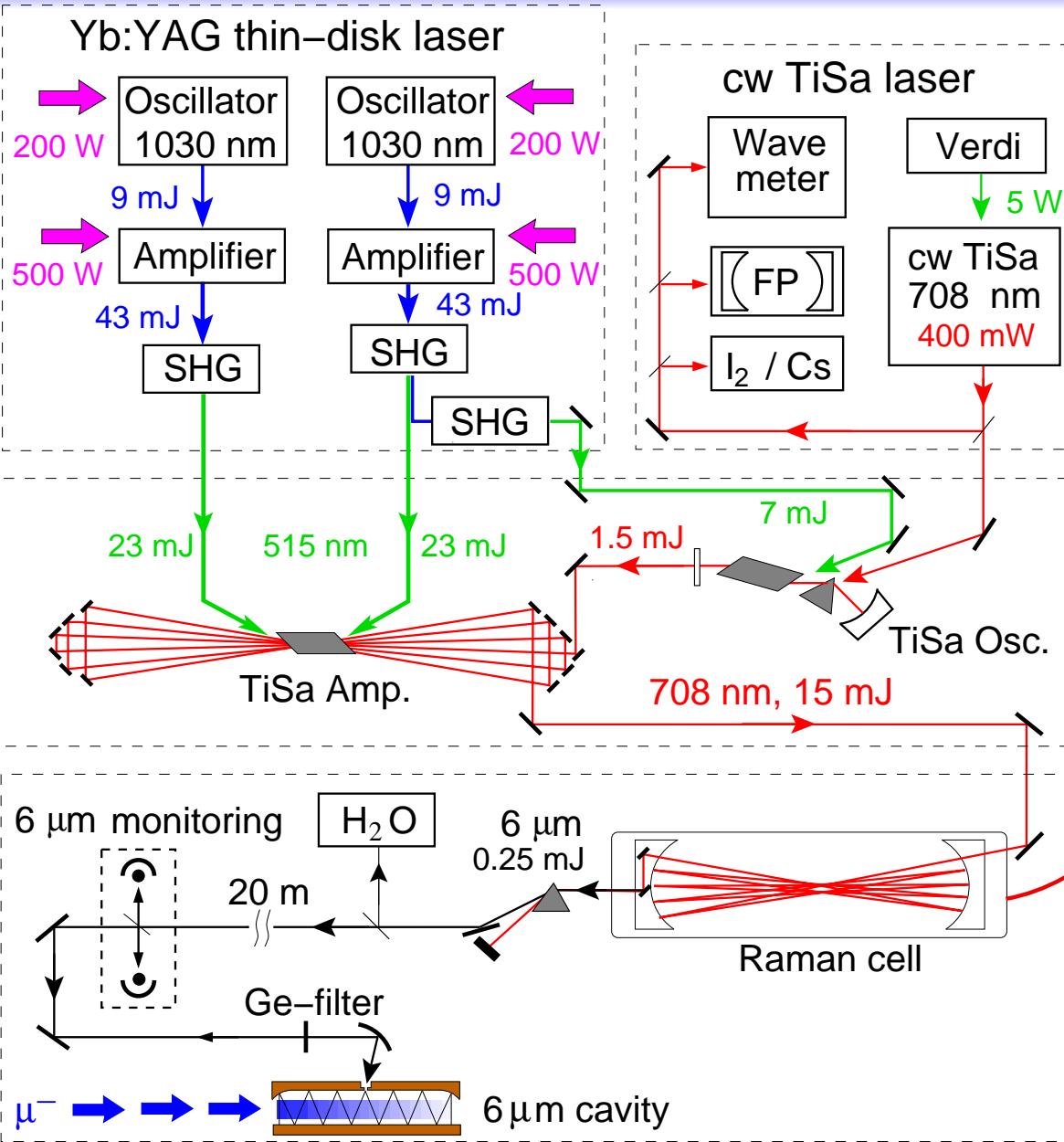
$$\rightarrow v_{\text{TiSa}}^{\text{pulsed}} = v_{\text{TiSa}}^{\text{cw}}$$

(frequency chirp ≤ 200 MHz)

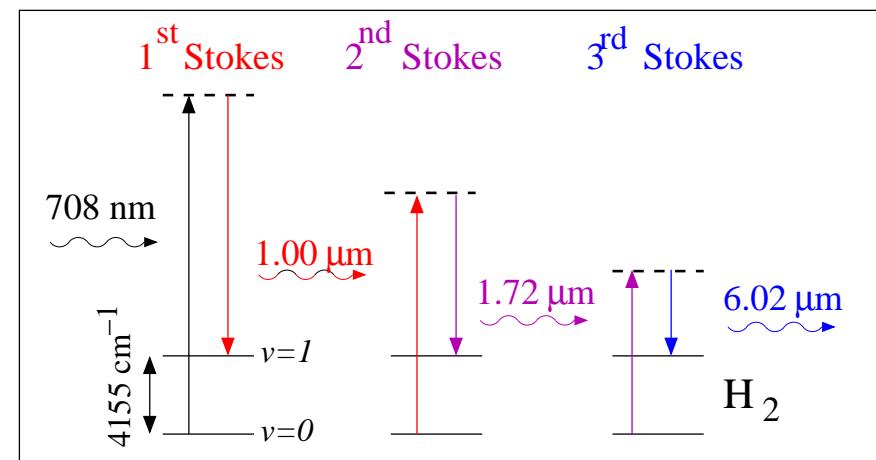
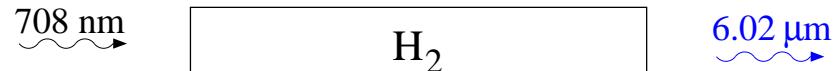
Multipass amplifier (2f- configuration)

gain=10

The laser system



Raman cell:

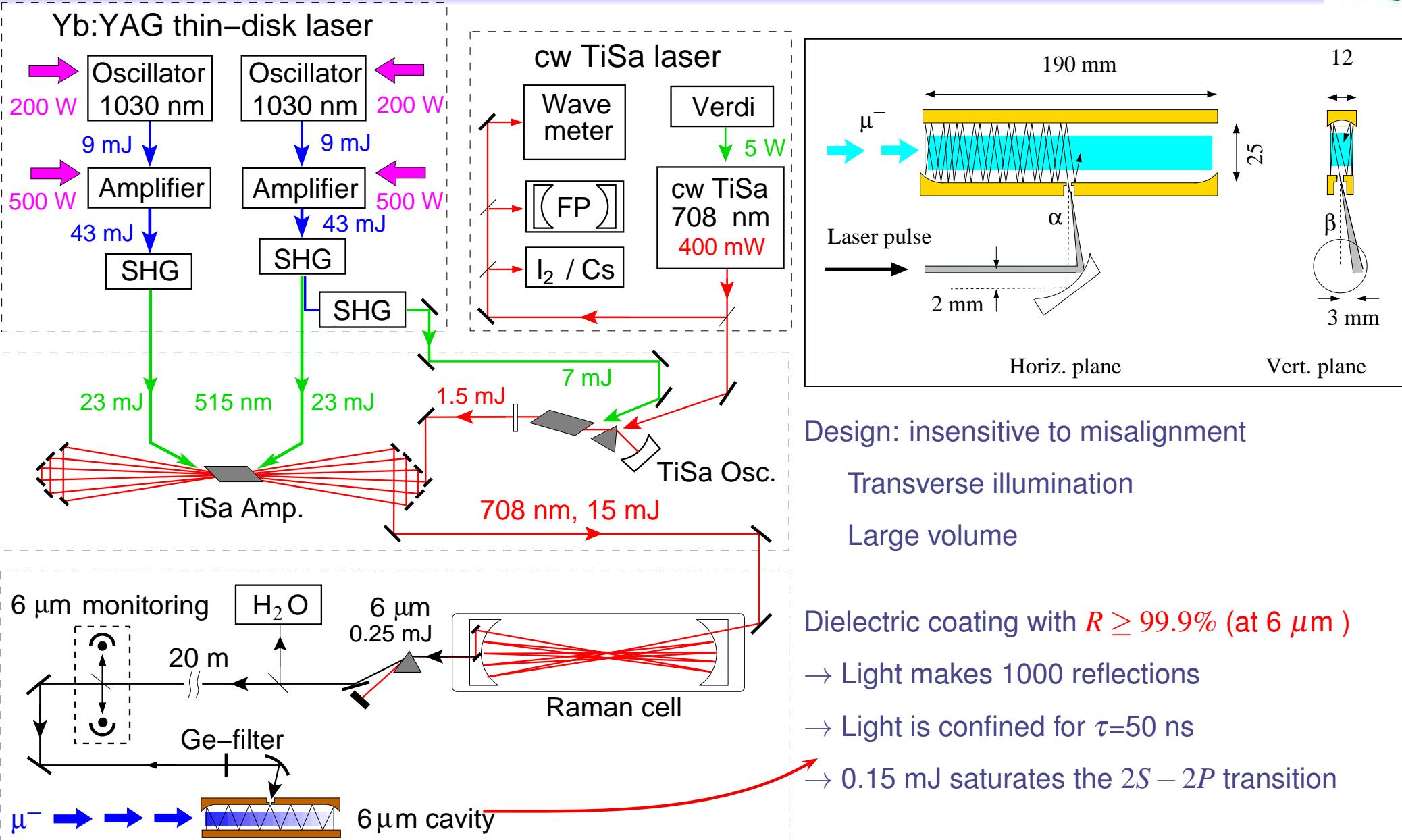


$$\nu^{6\mu\text{m}} = \nu^{708\text{nm}} - 3 \cdot \hbar \omega_{\text{vib}}$$

tunable
 $\omega_{\text{vib}}(p, T) = \text{const}$

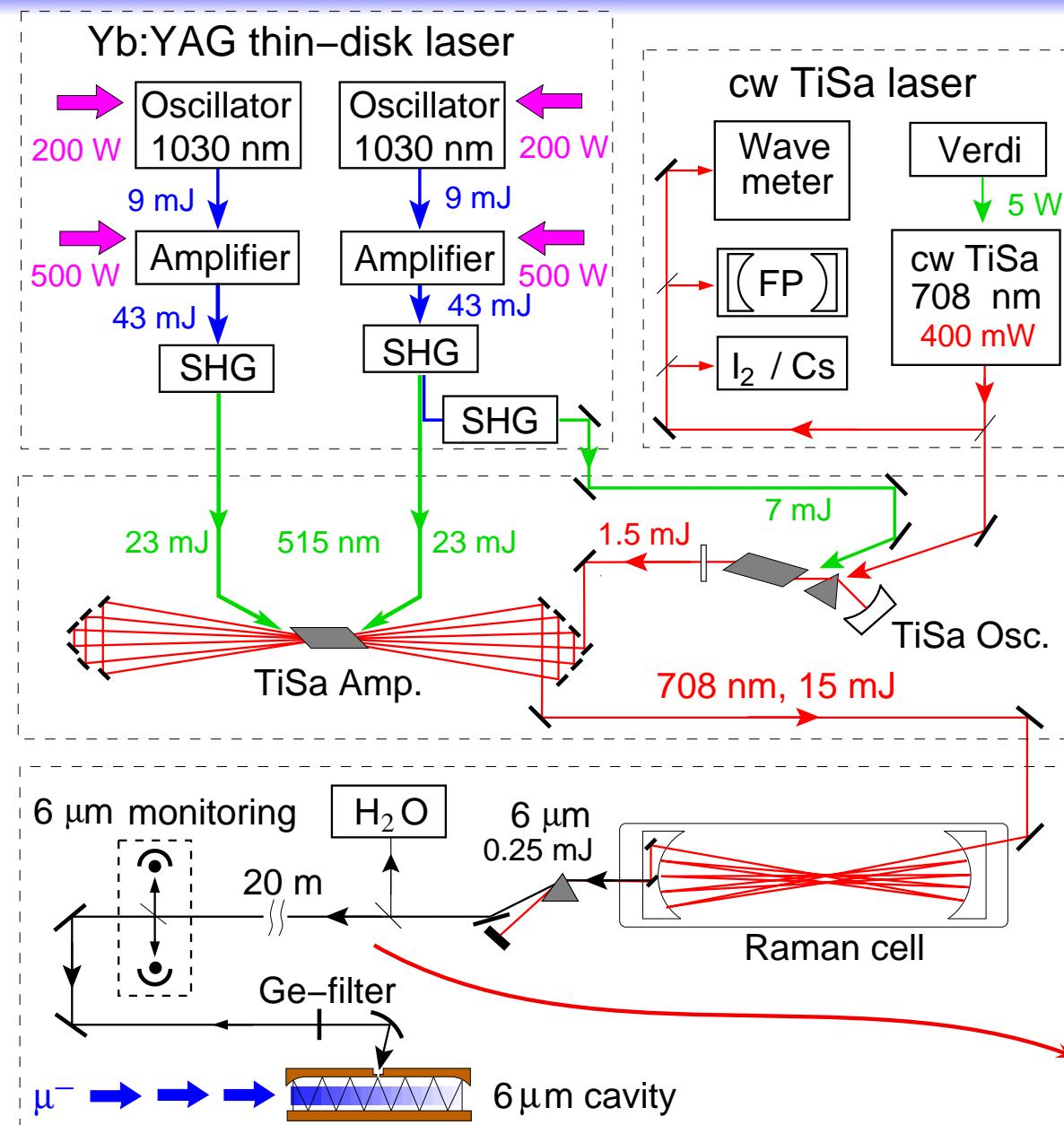
P. Rabinowitz *et. al.*, IEEE J. QE 22, 797 (1986)

The laser system

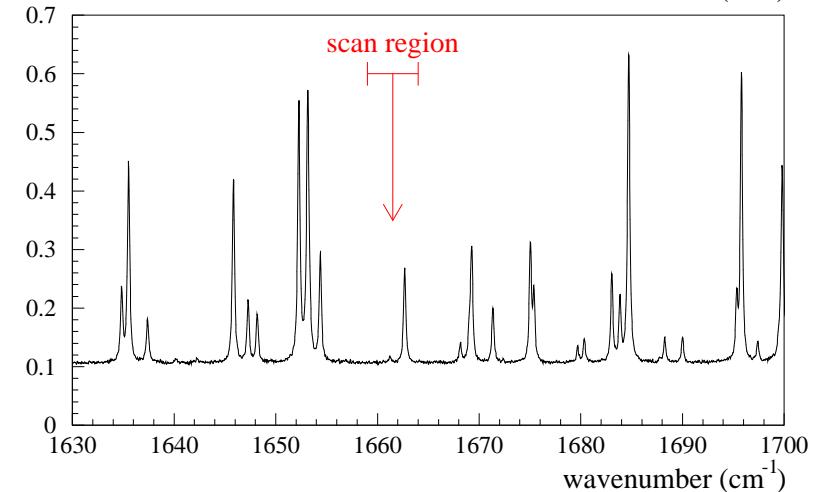
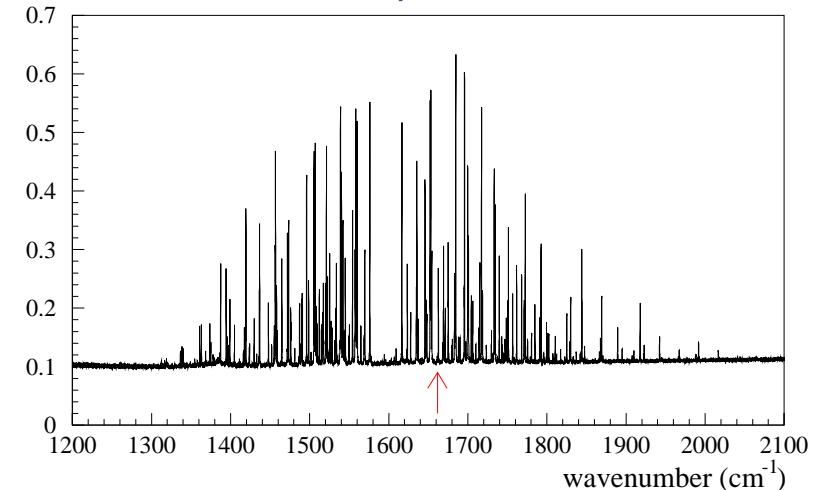


J. Vogelsang, RP et. al., Opt. Expr. 22, 13050 (2014)

The laser system

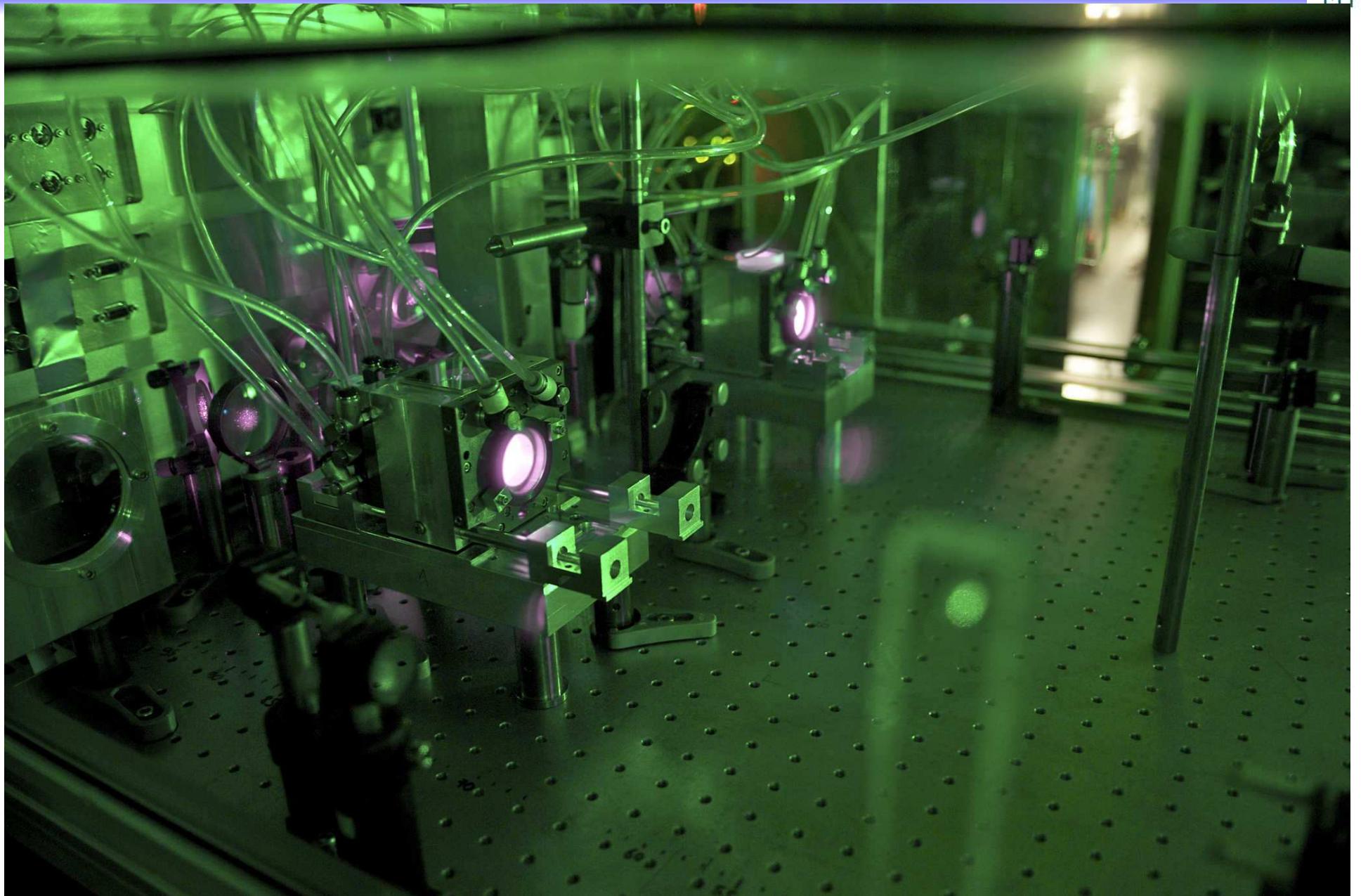


Water absorption

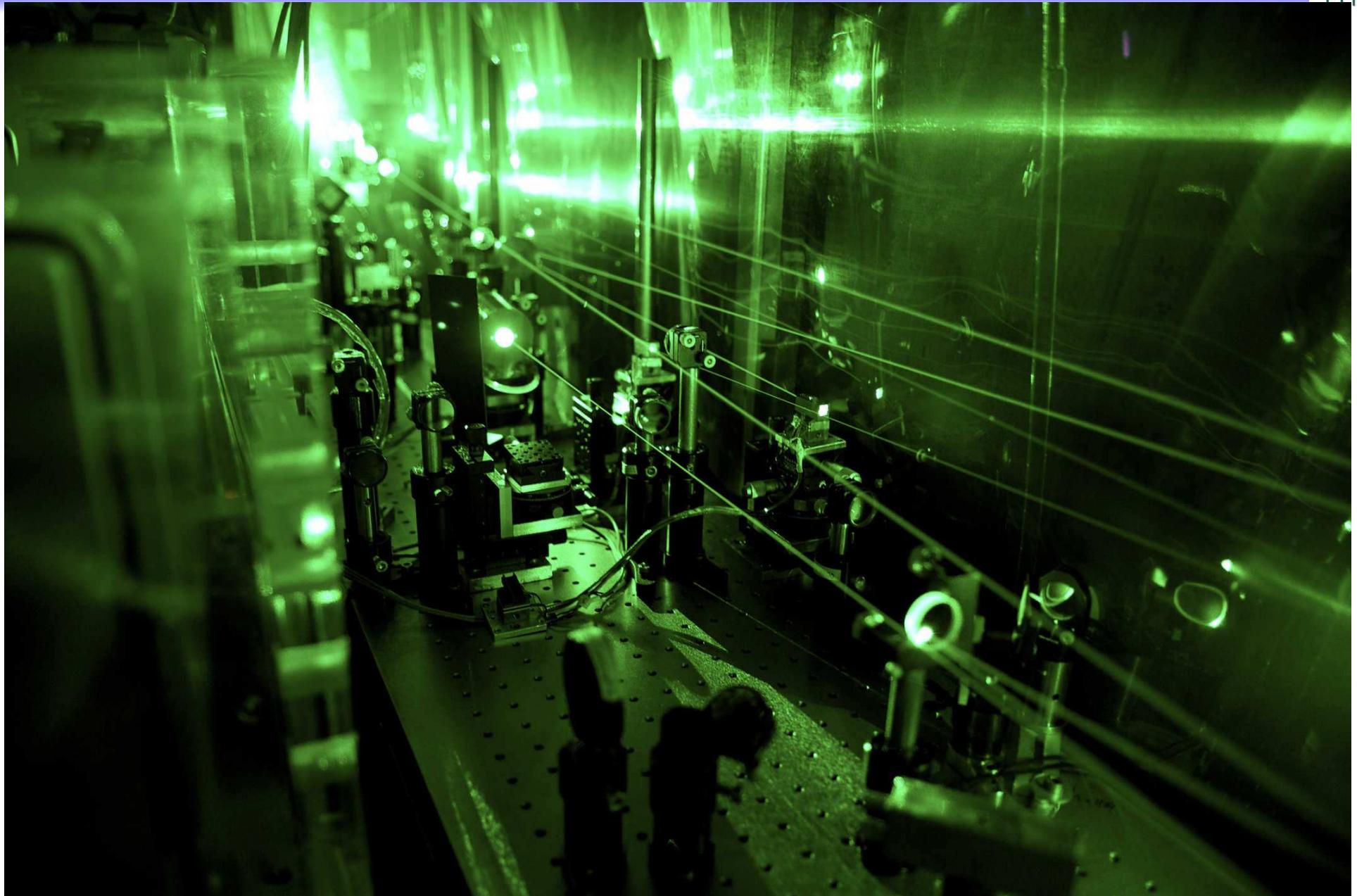


- Vacuum tube for 6 μm beam transport.
- Direct frequency calibration at 6 μm .

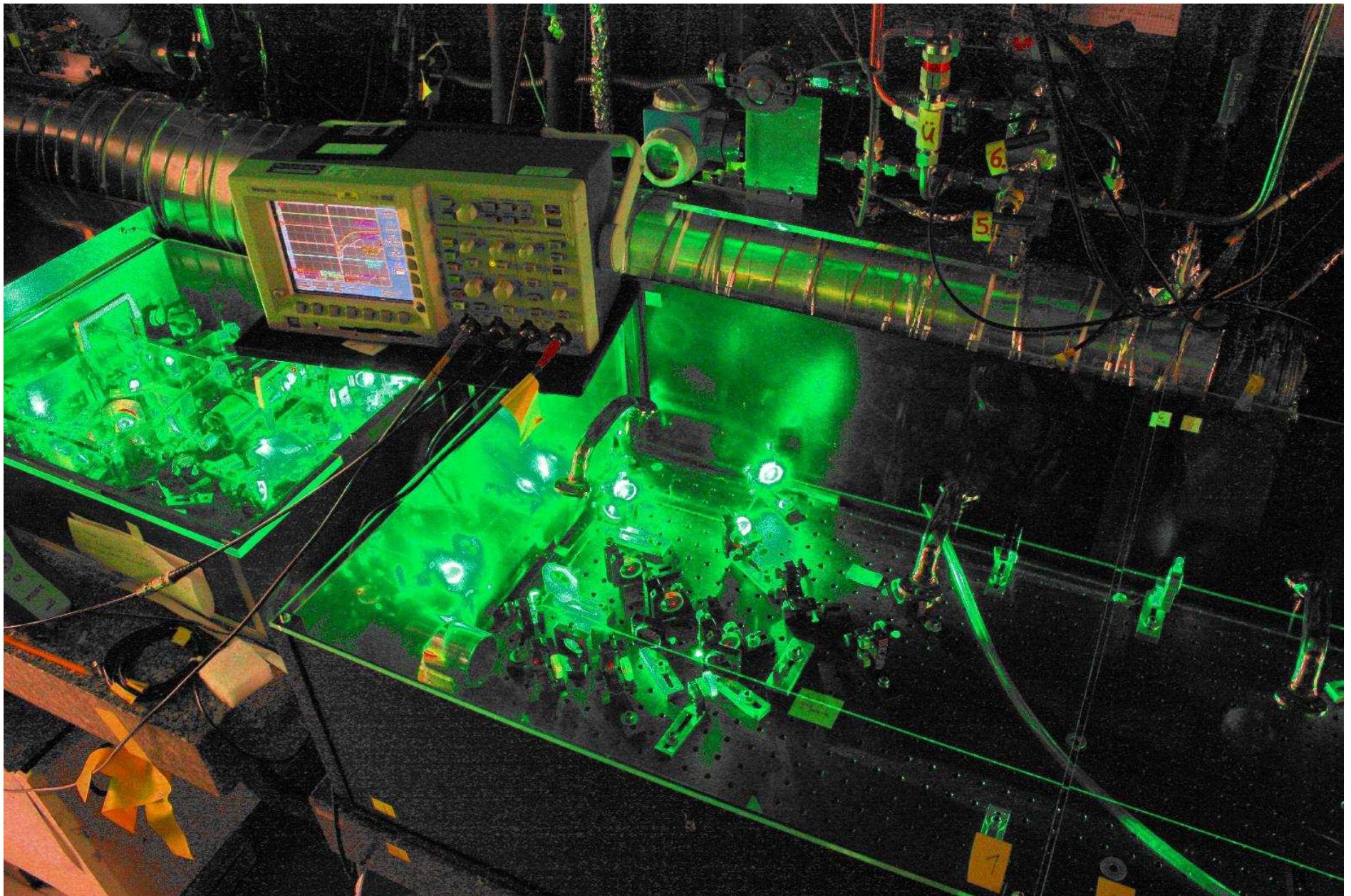
Disk amplifier laser heads



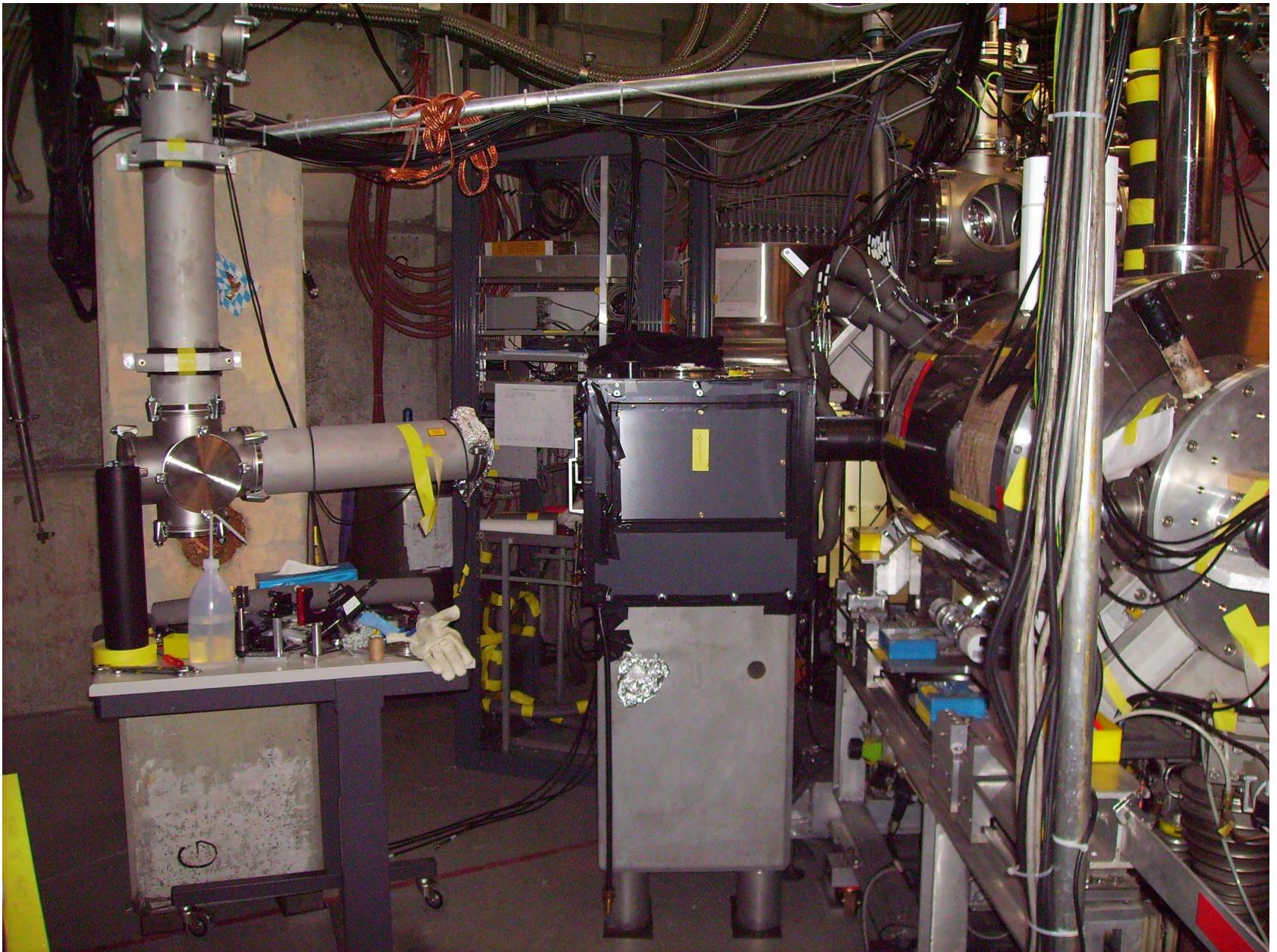
Disk laser doubling stages



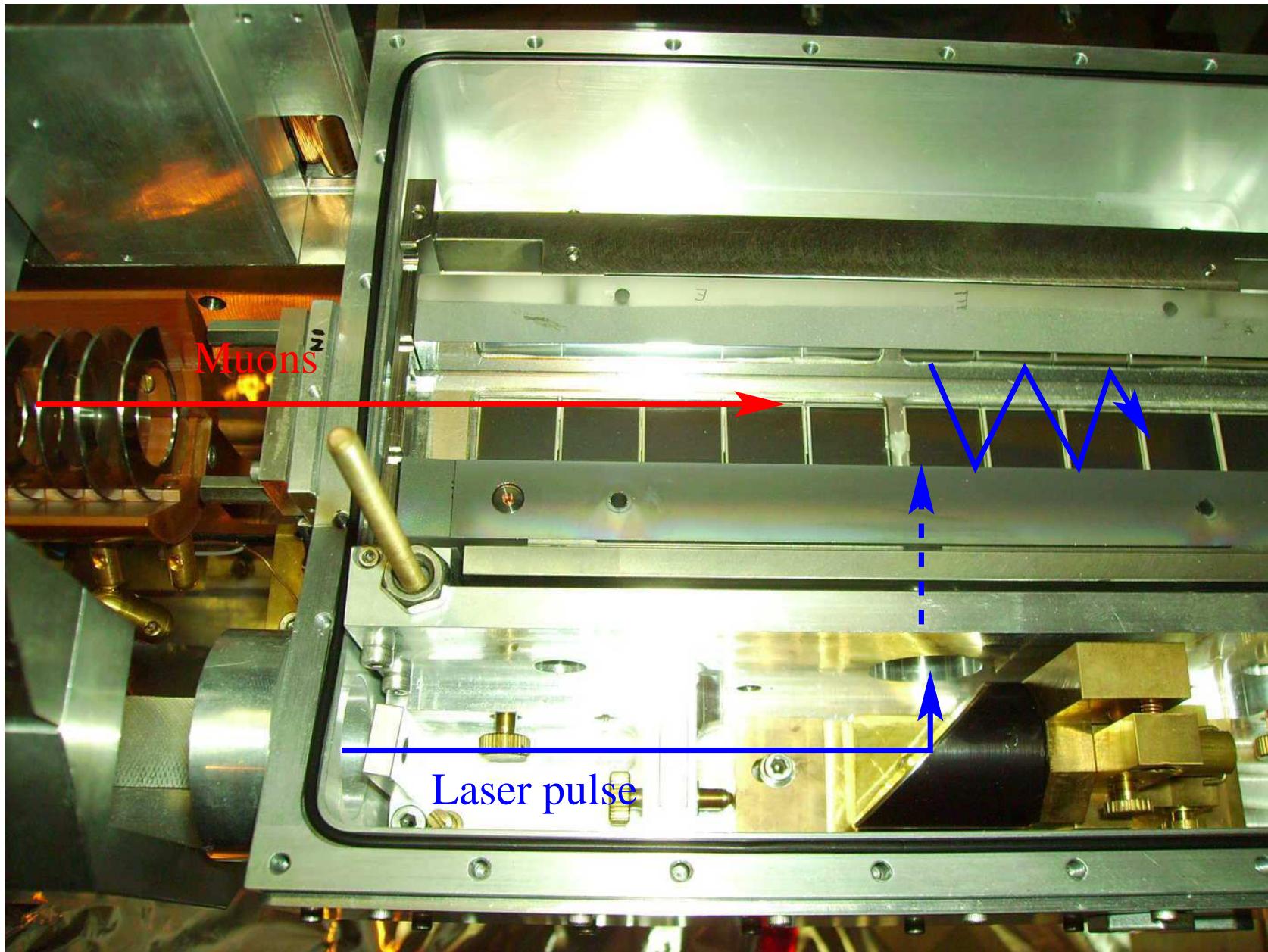
TiSa lasers and Raman cell



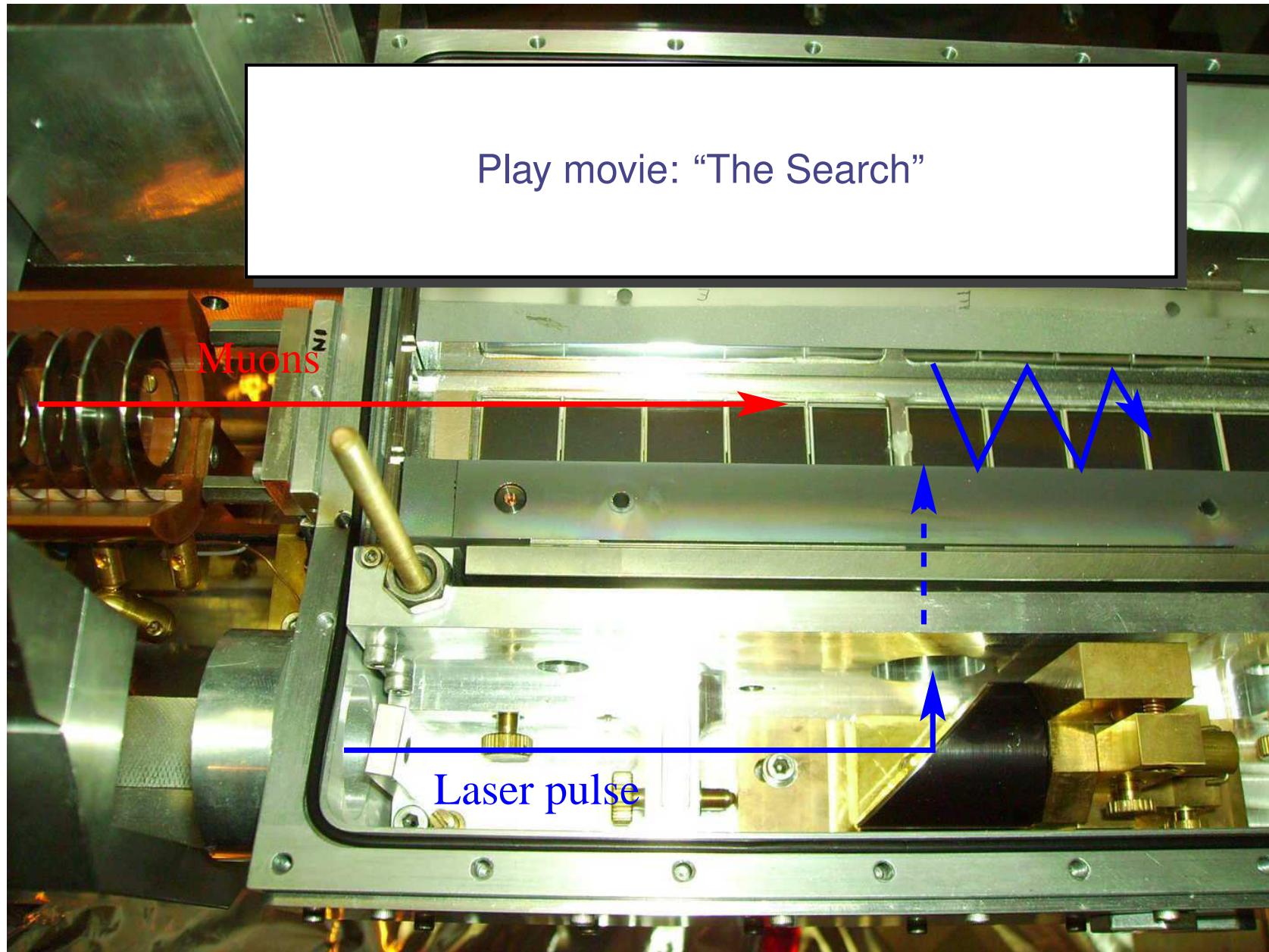
Laser beam tube



Target, cavity and detectors



Target, cavity and detectors



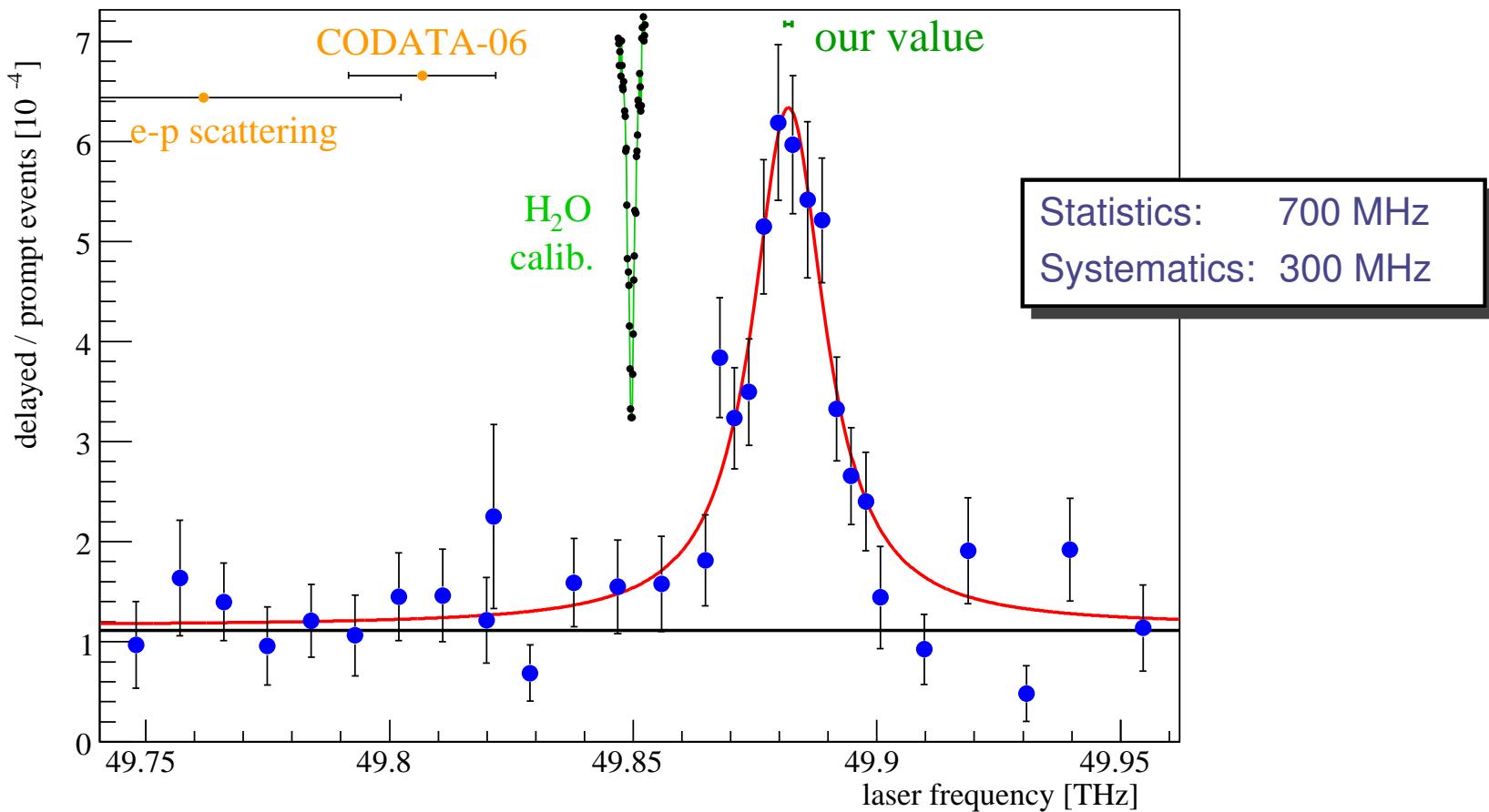
Yeah!



The resonance: discrepancy, sys., stat.

Water-line/laser wavelength:
300 MHz uncertainty

$\Delta\nu$ water-line to resonance:
200 kHz uncertainty

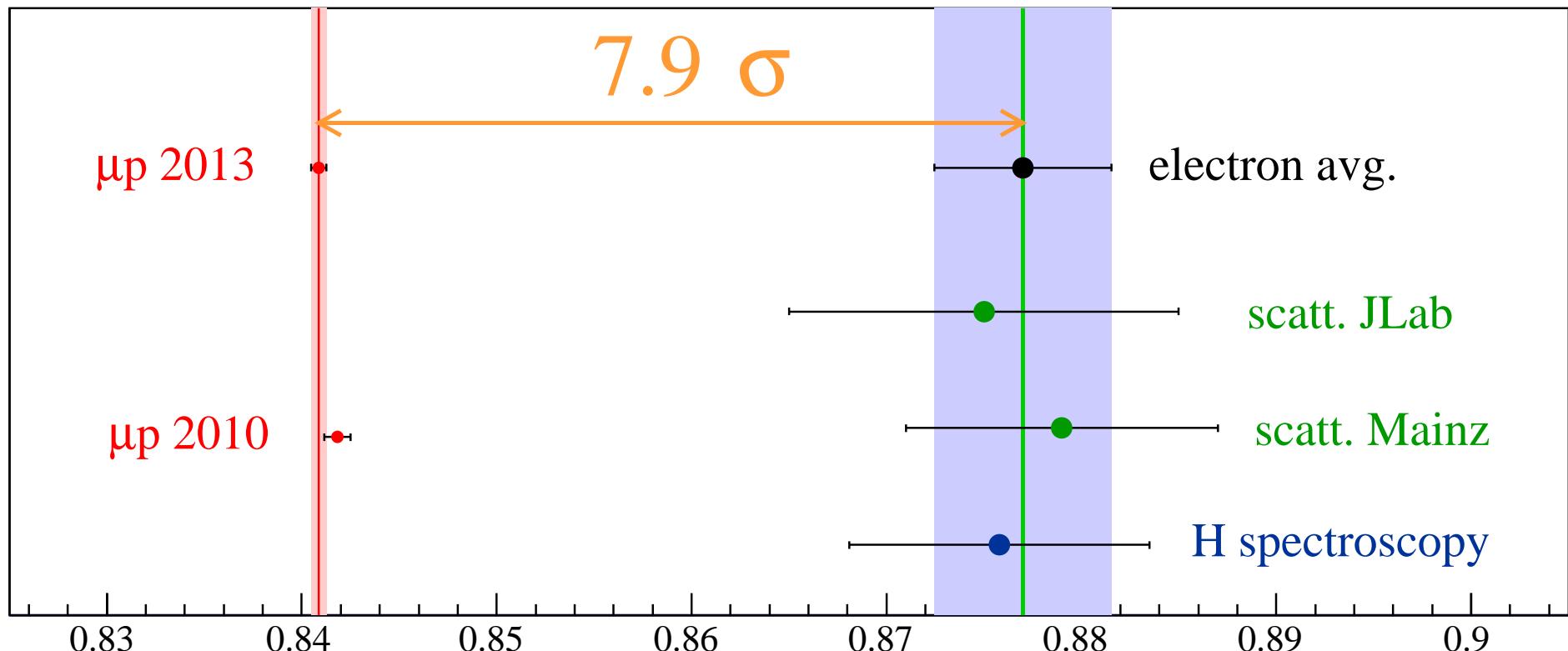


Discrepancy:
 $5.0\sigma \leftrightarrow 75 \text{ GHz} \leftrightarrow \delta\nu/\nu = 1.5 \times 10^{-3}$

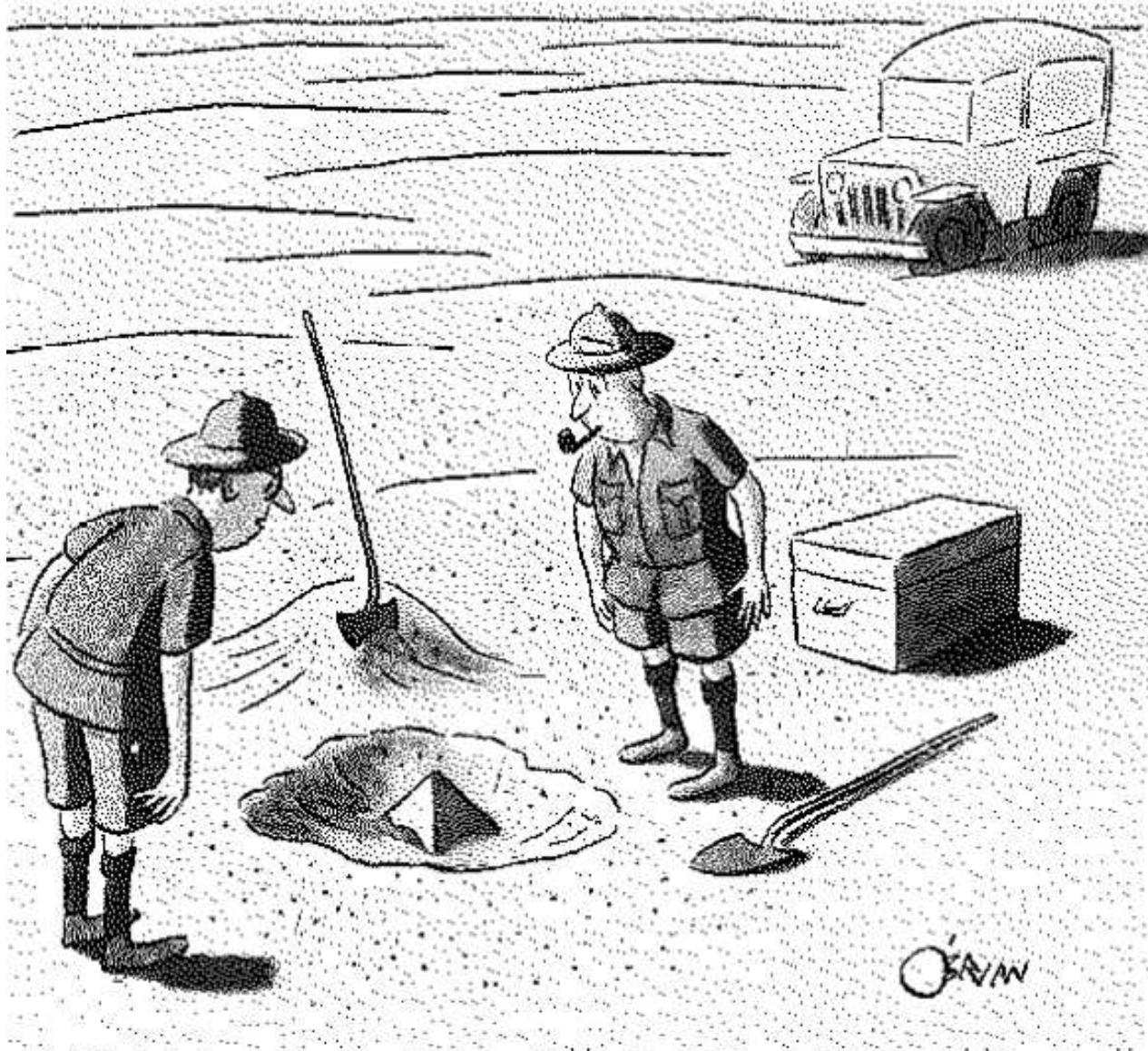
R. Pohl *et al.*, Nature 466, 213 (2010).
A. Antognini, RP *et al.*, Science 339, 417 (2013).

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muons: 0.8409 ± 0.0004 fm



R. Pohl *et al.*, Nature 466, 213 (2010).
A. Antognini *et al.*, Science 339, 417 (2013).



"This could be the discovery of the century. Depending, of course, on how far down it goes."

Muons in the news



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AAPPS Bulletin

Volume 23 Number 2 APRIL 2013

Proton Size Puzzle Reinforced

The diagram illustrates a proton beam line and an experimental setup. The beam line starts with a proton beam line leading to a C-target. Above the beam line is a Momentum filter and a Cyclotron trap. Below the beam line is a Raman cell and a Ti:Sa cw laser. The experimental setup includes a Ti:Sa amplifier, a Dioda laser, and a SHG (Second Harmonic Generation) module. A Water vapor cell is also shown. The entire setup is labeled with various components: Momentum filter, Cyclotron trap, Proton beam line, C-target, Raman cell, Ti:Sa cw laser, Ti:Sa amplifier, Dioda laser, SHG, and Water vapor cell.

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- Neutrino Oscillation and Mixing
- Status and Prospect of Telescope Array Experiment

Activities and Research News

- Proton Size Puzzle Reinforced
- Asia Pacific School/Workshop on Gravitation and Cosmology 2013

Institutes in Asia Pacific

- Department of Physics, Yonsei University
- Department of Physics at Korea University

Muons in the news



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Muons in the news



J. Bernauer, RP

Muons in the news



J. Bernauer, RP

What may be wrong?

$$\tilde{L}_{\mu p}^{\text{theo.}}(r_p^{\text{CODATA}}) - \tilde{L}_{\mu p}^{\text{exp.}} = \begin{cases} 75 \text{ GHz} \\ 0.31 \text{ meV} \\ 0.15 \% \end{cases}$$

μp theory wrong?
 μp experiment wrong?
 H theory wrong?
 H experiments wrong? $\rightarrow R_\infty$ wrong?
 AND e-p scattering exp. wrong?
 Standard Model wrong?!?

RP, R. Gilman, G.A. Miller, K. Pachucki, "Muonic hydrogen and the proton radius puzzle",
 Annu. Rev. Nucl. Part. Sci. **63**, 175 (2013) (arXiv 1301.0905)

What may be wrong?

$$\tilde{L}_{\mu p}^{\text{theo.}}(r_p^{\text{CODATA}}) - \tilde{L}_{\mu p}^{\text{exp.}} = \begin{cases} 75 \text{ GHz} \\ 0.31 \text{ meV} \\ 0.15 \% \end{cases}$$

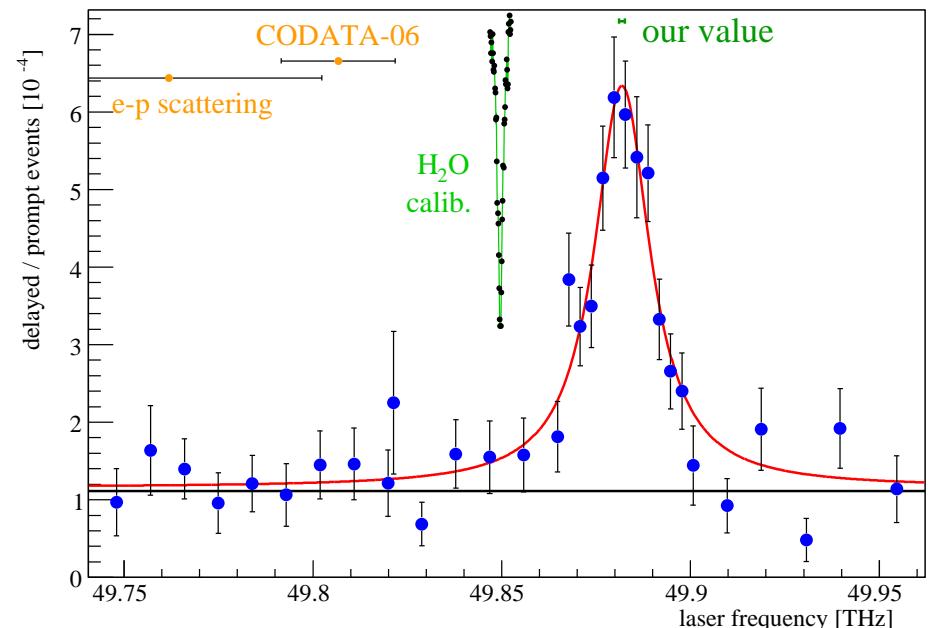
μp experiment wrong?

- Frequency mistake by 75 GHz ($\Leftrightarrow 0.15\%$)?

That is $> 100 \delta(\mu p)$! $\sigma_{\text{tot}} = 650 \text{ MHz}$, [$570 \text{ MHz}_{\text{stat}}$, $300 \text{ MHz}_{\text{syst}}$]

4 line widths ! $\Gamma = 19 \text{ GHz}$

2 resonances in μp give the same r_p



What may be wrong?

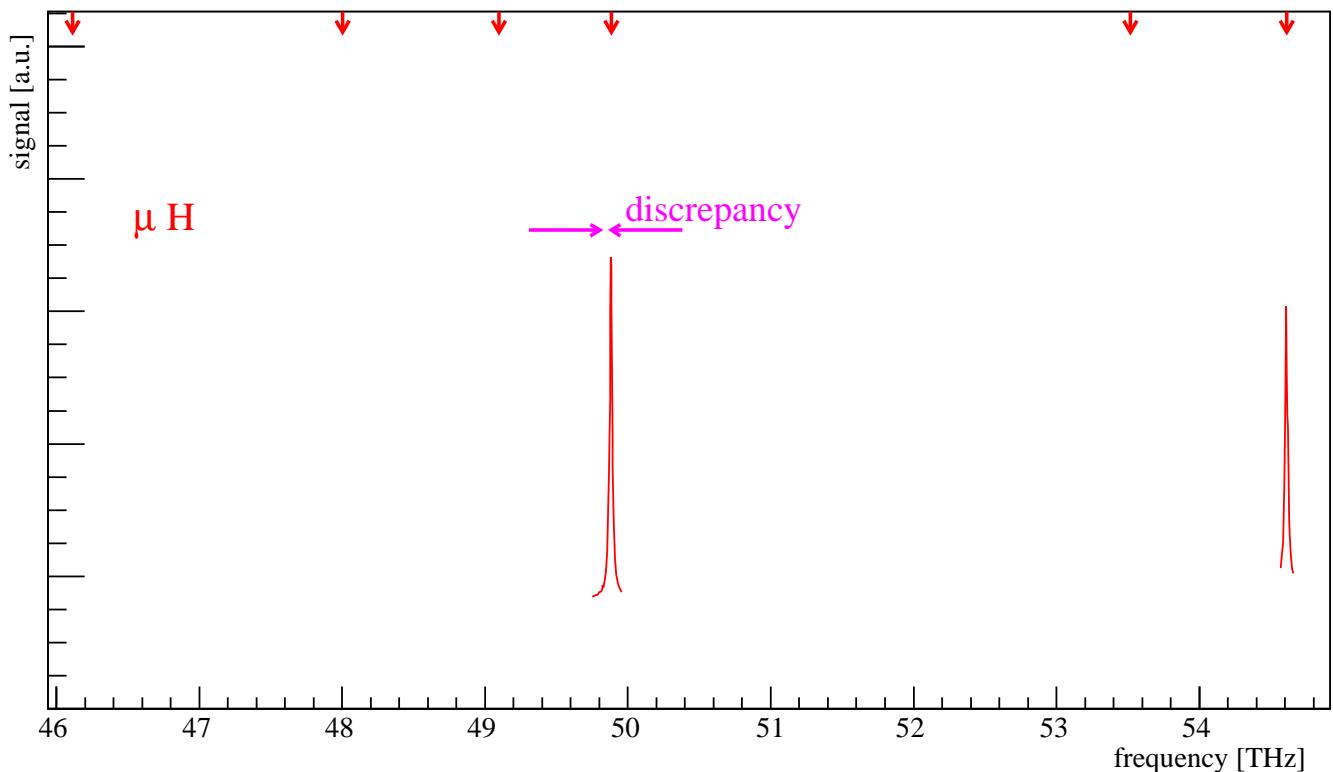
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μp experiment wrong?

- Frequency mistake by 75 GHz ($\Leftrightarrow 0.15\%$)?
- Wrong transition?

FS, HFS huge.

Next transition:
 $\sim 1 \text{ THz}$ away.



What may be wrong?

$$\tilde{L}_{\mu p}^{\text{theo.}}(r_p^{\text{CODATA}}) - \tilde{L}_{\mu p}^{\text{exp.}} = \begin{cases} 75 \text{ GHz} \\ 0.31 \text{ meV} \\ 0.15 \% \end{cases}$$

μp experiment wrong?

- Frequency mistake by 75 GHz ($\Leftrightarrow 0.15\%$)?
- Wrong transition?
- Systematic error?

Laser frequency (H ₂ O calibration)	300 MHz
intrinsic H ₂ O uncertainty	2 MHz
AC and DC stark shift	< 1 MHz
Zeeman shift (5 Tesla)	< 30 MHz
Doppler shift	< 1 MHz
Collisional shift	2 MHz
	300 MHz

μp atom is small and not easily perturbed by external fields.

What may be wrong?

$$\tilde{L}_{\mu p}^{\text{theo.}}(r_p^{\text{CODATA}}) - \tilde{L}_{\mu p}^{\text{exp.}} = \begin{cases} 75 \text{ GHz} \\ 0.31 \text{ meV} \\ 0.15 \% \end{cases}$$

μp experiment wrong?

- Frequency mistake by 75 GHz ($\Leftrightarrow 0.15\%$)?
- Wrong transition?
- Systematic error?
- Molecular effects?

$p \mu e$ molecular ion? U.D. Jentschura, Annals of Physics 326, 516 (2011).

Does not exist! J.-P. Karr, L. Hilico, PRL 109, 103401 (2012).
 M. Umair, S. Jonsell, J. Phys. B 47, 175003 (2014).

Experimentally:

- only 1 line observed ($> 80\%$ population)
- expected width
- $p p \mu$ ion short-lived R. Pohl *et al.*, PRL 97, 193402 (2006).

What may be wrong?

$$\tilde{L}_{\mu p}^{\text{theo.}}(r_p^{\text{CODATA}}) - \tilde{L}_{\mu p}^{\text{exp.}} = \begin{cases} 75 \text{ GHz} \\ 0.31 \text{ meV} \\ 0.15 \% \end{cases}$$

μp experiment wrong?

- Frequency mistake by 75 GHz ($\Leftrightarrow 0.15\%$)?
- Wrong transition?
- Systematic error?
- Molecular effects?
- Gas impurities? M. Diepold, RP *et al.*, PRA 88, 042520 (2013).

Target gas contained 0.55(5) % air (leak).

Back-of-the-envelope calculation:

$$\text{collision rate } \lambda \approx 6 \cdot 10^3 \text{ s}^{-1}$$

$$2S \text{ lifetime } \tau(2S) = 1 \mu\text{s}$$

\Rightarrow Less than 1% of all $\mu p(2S)$ atoms see any N_2

What may be wrong?

$$\tilde{L}_{\mu p}^{\text{theo.}}(r_p^{\text{CODATA}}) - \tilde{L}_{\mu p}^{\text{exp.}} = \begin{cases} 75 \text{ GHz} \\ 0.31 \text{ meV} \\ 0.15 \% \end{cases}$$

μp experiment wrong?

- Frequency mistake by 75 GHz ($\Leftrightarrow 0.15\%$)?
- Wrong transition?
- Systematic error?
- Molecular effects?
- Gas impurities?

μp experiment probably not wrong by 100σ

What may be wrong?

$$\tilde{L}_{\mu p}^{\text{theo.}}(r_p^{\text{CODATA}}) - \tilde{L}_{\mu p}^{\text{exp.}} = \begin{cases} 75 \text{ GHz} \\ 0.31 \text{ meV} \\ 0.15 \% \end{cases}$$

μp theory wrong?

Discrepancy = 0.31 meV
 Theory uncert. = 0.0025 meV
 $\implies 120\delta(\text{theory})$ deviation

double-checked by many groups

5th largest term!

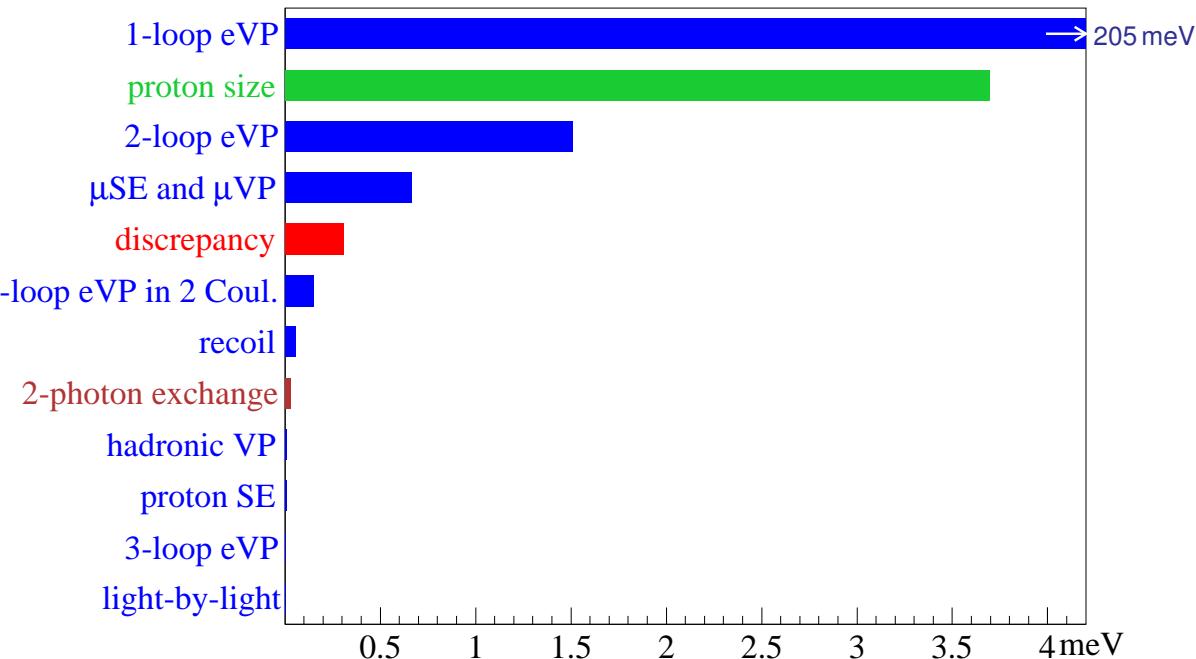
Theory summary:

A. Antognini, RP *et al.*

Annals of Physics 331, 127 (2013)

$$\Delta E = 206.0668(25) - 5.2275(10) r_p^2 \text{ [meV]}$$

Some contributions to the μp Lamb shift



What may be wrong?

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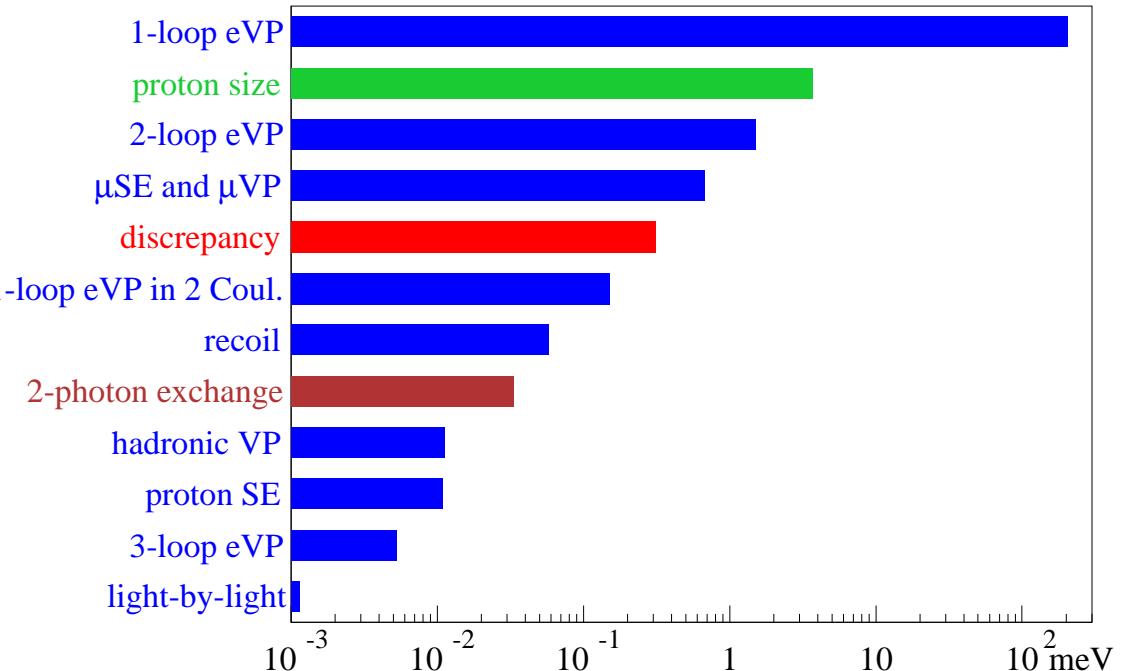
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 Theory uncert. = 0.0025 meV
 $\implies 120\delta(\text{theory})$ deviation

$$\Delta E = 206.0668(25) - 5.2275(10) r_p^2 \text{ [meV]}$$

μp theory probably not wrong by 100 σ

Lamb shift in μp 1: r_p independent

Table 1

All known radius-*independent* contributions to the Lamb shift in μp from different authors, and the one we selected. Values are in meV. The entry # in the first column refers to Table 1 in Ref. [13]. The “finite-size to relativistic recoil correction” (entry #18 in [13]), which depends on the proton structure, has been shifted to Table 2, together with the small terms #26 and #27, and the proton polarizability term #25. SE: self-energy, VP: vacuum polarization, LBL: light-by-light scattering, Rel: relativistic, NR: non-relativistic, RC: recoil correction.

#	Contribution	Pachucki [10,11]	Nature [13]	Borie-v6 [79]	Indelicato [80]	Our choice	Ref.
1	NR one-loop electron VP (eVP)	205.0074					
2	Rel. corr. (Breit–Pauli)	0.0169 ^a					
3	Rel. one-loop eVP		205.0282	205.0282	205.02821	205.02821	[80] Eq. (54)
19	Rel. RC to eVP, $\alpha(Z\alpha)^4$	(incl. in #2) ^b	−0.0041	−0.0041		−0.00208 ^c	[77,78]
4	Two-loop eVP (Källén–Sabry)	1.5079	1.5081	1.5081	1.50810	1.50810	[80] Eq. (57)
5	One-loop eVP in 2-Coulomb lines $\alpha^2(Z\alpha)^5$	0.1509	0.1509	0.1507	0.15102	0.15102	[80] Eq. (60)
7	eVP corr. to Källén–Sabry	0.0023	0.00223	0.00223	0.00215	0.00215	[80] Eq. (62), [87]
6	NR three-loop eVP	0.0053	0.00529	0.00529		0.00529	[87,88]
9	Wichmann–Kroll, “1:3” LBL		−0.00103	−0.00102	−0.00102	−0.00102	[80] Eq. (64), [89]
10	Virtual Delbrück, “2:2” LBL		0.00135	0.00115		0.00115	[74,89]
New	“3:1” LBL			−0.00102		−0.00102	[89]
20	μ SE and μ VP	−0.6677	−0.66770	−0.66788	−0.66761	−0.66761	[80] Eqs. (72) + (76)
11	Muon SE corr. to eVP $\alpha^2(Z\alpha)^4$	−0.005(1)	−0.00500	−0.004924 ^d		−0.00254	[85] Eq. (29a) ^e
12	eVP loop in self-energy $\alpha^2(Z\alpha)^4$	−0.001	−0.00150			^f	[74,90–92]
21	Higher order corr. to μ SE and μ VP		−0.00169	−0.00171 ^g		−0.00171	[86] Eq. (177)
13	Mixed eVP + μ VP		0.00007	0.00007		0.00007	[74]
New	eVP and μ VP in two Coulomb lines				0.00005	0.00005	[80] Eq. (78)
14	Hadronic VP $\alpha(Z\alpha)^4 m_r$	0.0113(3)	0.01077(38)	0.011(1)		0.01121(44)	[93–95]
15	Hadronic VP $\alpha(Z\alpha)^5 m_r$		0.000047			0.000047	[94,95]
16	Rad corr. to hadronic VP		−0.000015			−0.000015	[94,95]
17	Recoil corr.	0.0575	0.05750	0.0575	0.05747	0.05747	[80] Eq. (88)
22	Rel. RC $(Z\alpha)^5$	−0.045	−0.04497	−0.04497	−0.04497	−0.04497	[80] Eq. (88), [74]
23	Rel. RC $(Z\alpha)^6$	0.0003	0.00030		0.0002475	0.0002475	[80] Eq. (86)+Tab.II

(continued on next page)

Lamb shift in μ_p : r_p independent



Table 1 (continued)

#	Contribution	Pachucki [10,11]	Nature [13]	Borie-v6 [79]	Indelicato [80]	Our choice	Ref.
New	Rad. (only eVP) $RC \alpha(Z\alpha)^5$					0.000136	[85] Eq. (64a)
24	Rad. $RC \alpha(Z\alpha)^n$ (proton SE)	-0.0099	-0.00960	-0.0100		-0.01080(100)	[43] ^h [74]
	Sum	206.0312	206.02915	206.02862		206.03339(109)	

^a This value has been recalculated to be 0.018759 meV [77].

^b This correction is not necessary here because in #2 the Breit–Pauli contribution has been calculated using a Coulomb potential modified by eVP.

^c Difference between Eqs. (6) and (4) in [78]: $E_{VP}^{(rel)}(2P_{1/2}-2S_{1/2}) - E_{VP}^{(0)}(2P_{1/2}-2S_{1/2}) = 0.018759 - 0.020843 = -0.002084$ meV (see also Table IV). Using these corrected values, the various approaches are consistent. Pachucki becomes $205.0074 + 0.018759 = 205.0262$ meV and Borie $205.0282 - 0.0020843 = 205.0261$ meV.

^d In Appendix C, incomplete.

^e Eq. (27) in [85] includes contributions beyond the logarithmic term with modification of the Bethe logarithm to the Uehling potential. The factor 10/9 should be replaced by 5/6.

^f This term is part of #22, see Fig. 22 in [86].

^g Borie includes wave-function corrections calculated in [87]. The actual difference between Ref. [13] and Borie-v6 [79] is given by the inclusion of the Källén–Sabry correction with muon loop.

^h This was calculated in the framework of NRQED. It is related to the definition of the proton radius.

- 43 R.J. Hill, G. Paz, Phys. Rev. Lett. 107, 160402 (2011)
- 74 M.I. Eides, H. Grotch, V.A. Shelyuto, Phys. Rep. 342, 63 (2001)
- 77 U.D. Jentschura, Phys. Rev. A 84, 012505 (2011)
- 78 S.G. Karshenboim, V.G. Ivanov, E.Y. Korzinin, Phys. Rev. A 85, 032509 (2012)
- 79 E. Borie, Ann. Phys. 327, 733 (2012); arXiv:1103.1772-v6
- 80 P. Indelicato, arXiv:1210.5828v2 [PRA 87, 022501 (2013)]
- 85 U.D. Jentschura, B.J. Wundt, Eur. Phys. J. D 65, 357 (2011)
- 86 E. Borie, G.A. Rinker, Rev. Mod. Phys. 54, 67 (1982)
- 87 V.G. Ivanov, E.Y. Korzinin, S.G. Karshenboim, Phys. Rev. D 80, 027702 (2009)
- 88 T. Kinoshita, M. Nio, Phys. Rev. Lett. 82, 3240 (1999)
- 89 S.G. Karshenboim, E.Y. Korzinin, V.G. Ivanov, V.A. Shelyuto, JETP Lett. 92, 8 (2010)
- 90 R. Barbieri, M. Caffo, E. Remiddi, Lett. Nuovo Cimento 7, 60 (1963)
- 91 H. Suura, E.H. Wichmann, Phys. Rev. 105, 1930 (1957)
- 92 A. Petermann, Phys. Rev. 105, 1931 (1957)
- 93 J. Friar, J. Martorell, D. Sprung, Phys. Rev. A 59, 4061 (1999)
- 94 A.P. Martynenko, R. Faustov, Phys. Atomic Nuclei 63, 845 (2000)
- 95 A.P. Martynenko, R. Faustov, Phys. Atomic Nuclei 64, 1282 (2001)

A. Antognini, RP *et al.*, Ann. Phys. 331, 127 (2013), Tab 1

Lamb shift in μp 2: r_p -dependent

Table 2

Proton-structure-dependent contributions to the Lamb shift in μp from different authors and the one we selected. Values are in meV, $\langle r^2 \rangle$ in fm². The entry # in the first column refers to Table 1 in Ref. [13] supplementary information [9]. Entry # 18 is under debate. TPE: two-photon exchange, VP: vacuum polarization, SE: self-energy, Rel: relativistic.

#	Contribution	Borie-v6 [79]	Karshenboim [78]	Pachucki [10,11]	Indelicato [80]	Carroll [84]	Our choice
	Non-rel. finite-size	$-5.1973 \langle r^2 \rangle$	$-5.1975 \langle r^2 \rangle$	$-5.1975 \langle r^2 \rangle$			
	Rel. corr. to non-rel. finite size	$-0.0018 \langle r^2 \rangle$		-0.0009 meV^a			
	Rel. finite-size						
	Exponential				$-5.1994 \langle r^2 \rangle$	$-5.2001 \langle r^2 \rangle$	$-5.1994 \langle r^2 \rangle$
	Yukawa					$-5.2000 \langle r^2 \rangle$	
	Gaussian					$-5.2001 \langle r^2 \rangle$	
New	Finite size corr. to one-loop eVP	$-0.0110 \langle r^2 \rangle$	$-0.0110 \langle r^2 \rangle$	$-0.010 \langle r^2 \rangle$	$-0.0282 \langle r^2 \rangle$		$-0.0282 \langle r^2 \rangle$
	Finite size to one-loop eVP-it.	$-0.0165 \langle r^2 \rangle$	$-0.0170 \langle r^2 \rangle$	$-0.017 \langle r^2 \rangle$	(incl. in -0.0282)		
	Finite-size corr. to Källén–Sabry	^b			$-0.0002 \langle r^2 \rangle$		$-0.0002 \langle r^2 \rangle$
	Finite size corr. to μ self-energy	$(0.00699)^c$			$0.0008 \langle r^2 \rangle$	$0.0009(3) \langle r^2 \rangle^d$	
25	ΔE_{TPE} [46]						$0.0332(20) \text{ meV}$
	Elastic (third Zemach) ^e						
	Measured $R_{(2)}^3$	$0.0365(18) \langle r^2 \rangle^{3/2}$					(incl. above)
	Exponential			$0.0363 \langle r^2 \rangle^{3/2}$	$0.0353 \langle r^2 \rangle^{3/2}^f$	$0.0353 \langle r^2 \rangle^{3/2}$	
	Yukawa					$0.0378 \langle r^2 \rangle^{3/2}$	
	Gaussian					$0.0323 \langle r^2 \rangle^{3/2}$	
New 26	Inelastic (polarizability)	$0.0129(5)$ meV [101]		$0.012(2) \text{ meV}$			(incl. above)
	Rad. corr. to TPE eVP corr. to polarizability	$-0.00062 \langle r^2 \rangle$					$-0.00062 \langle r^2 \rangle$ 0.00019 meV [95]

(continued on next page)

A. Antognini, RP *et al.*, Ann. Phys. 331, 127 (2013), Tab 2

Lamb shift in μ_p 2: r_p -dependent

Table 2 (continued)

#	Contribution	Borie-v6 [79]	Karshenboim [78]	Pachucki [10,11]	Indelicato [80]	Carroll [84]	Our choice
27	SE corr. to polarizability						-0.00001 meV [95]
18	Finite-size to rel. recoil corr.	(0.013 meV) ^g		^h			(incl. in ΔE_{TPE})
	Higher order finite-size corr.	-0.000123 meV			0.00001(10) meV		0.00001(10) meV
	2P _{1/2} finite-size corr.	-0.0000519(r^2) ⁱ			(incl. above)	(incl. above)	(incl. above)

^a Corresponds to Eq. (6) in [11] which accounts only for the main terms in F_{REL} and F_{NREL} .

^b This contribution has been accounted already in both the -0.0110 meV/fm² and -0.0165 meV/fm² coefficients.

^c Given only in Appendix C. Bethe logarithm is not included.

^d This uncertainty accounts for the difference between all-order in $Z\alpha$ and perturbative approaches [82].

^e Corresponds to Eq. (20).

^f This value is slightly different from Eq. (22) because here an all-order in finite-size and an all-order in eVP approaches were used.

^g See Appendix F of [96]. This term is under debate.

^h Included in ΔE_{TPE} . This correction of $0.018 - 0.021 = -0.003$ meV is given by Eq. (64) in [10] and Eq. (25) in [11]. This correction is also discussed in [76] where the 6/7 factor results from 0.018/0.021.

ⁱ Eq. (6a) in [79].

- 46 M.C. Birse, J.A. McGovern, Eur. Phys. J. A 48, 120 (2012); arXiv:1206.3030
- 76 U.D. Jentschura, Ann. Phys. 326, 500 (2011)
- 79 E. Borie, Ann. Phys. 327, 733 (2012); arXiv:1103.1772-v6
- 82 P. Indelicato, P.J. Mohr, 2012 (in preparation)
- 95 A.P. Martynenko, R. Faustov, Phys. Atomic Nuclei 64, 1282 (2001)
- 96 J.L. Friar, Ann. Phys. 122, 151 (1979)
- 101 C.E. Carlson, M. Vanderhaeghen, Phys. Rev. A 84, 020102 (2011)

HFS in μp


Table 3

All known contributions to the 2S-HFS in μp from different authors and the one we selected. Values are in meV, radii in fm. SE: self-energy, VP: vacuum polarization, Rel: relativistic, RC: recoil correction, PT: perturbation theory, p: proton, int: interaction, AMM: anomalous magnetic moment.

Contribution	Martynenko [72]	Borie-v6 [79]	Indelicato	Our choice [80]	Ref.
h1 Fermi energy, $(Z\alpha)^4$	22.8054	22.8054			
h2 Breit corr., $(Z\alpha)^6$	0.0026	0.00258			
h3 Dirac energy (+ Breit corr. in all-order)			22.807995	22.807995	Eq. (107) in [80]
h4 μ AMM corr., $\alpha(Z\alpha)^4$, $\alpha(Z\alpha)^4$	0.0266	0.02659		0.02659	
h5 eVP in 2nd-order PT, $\alpha(Z\alpha)^5$ (ϵ_{VP2})	0.0746	0.07443			
h6 All-order eVP corr.			0.07437	0.07437	Eq. (109) in [80]
h7 Two-loop corr. to Fermi-energy (ϵ_{VP2})		0.00056		0.00056	
h8 One-loop eVP in 1γ int., $\alpha(Z\alpha)^4$ (ϵ_{VP1})	0.0482	0.04818		0.04818	
h9 Two-loop eVP in 1γ int., $\alpha^2(Z\alpha)^4$ (ϵ_{VP1})	0.0003	0.00037		0.00037	
h10 Further two-loop eVP corr.		0.00037		0.00037	[113,114]
h11 μ VP (similar to ϵ_{VP2})		0.00091		0.00091	
h12 μ VP (similar to ϵ_{VP1})	0.0004	(incl. in h13)		(incl. in h13)	
h13 Vertex, $\alpha(Z\alpha)^5$		-0.00311		-0.00311	^a
h14 Higher order corr. of (h13), (part with $\ln(\alpha)$)		-0.00017		-0.00017	[115]
h15 μ SE with p structure, $\alpha(Z\alpha)^5$	0.0010				
h16 Vertex corr. with proton structure, $\alpha(Z\alpha)^5$	-0.0018				
h17 "Jellyfish" corr. with p structure, $\alpha(Z\alpha)^5$	0.0005				
h18 Hadron VP, α^6	0.0005(1)	0.00060(10)		0.00060(10)	
h19 Weak interaction contribution	0.0003	0.00027		0.00027	[116]
h20 Finite-size (Zemach) corr. to ΔE_{Fermi} , $(Z\alpha)^5$	-0.1518 ^b	-0.16037 r_z	-0.16034 r_z	-0.16034 r_z	Eq. (107) in [80]

(continued on next page)

HFS in μ p



Table 3 (continued)

Contribution	Martynenko [72]	Borie-v6 [79]	Indelicato	Our choice [80]	Ref.
h21 Higher order finite-size corr. to ΔE_{Fermi}			$-0.0022 r_E^2 + 0.0009$	$-0.0022 r_E^2 + 0.0009$	Eq. (107) in [80]
h22 Proton polarizability, $(Z\alpha)^5$, $\Delta E_{\text{HFS}}^{\text{pol}}$	0.0105(18)	0.0080(26)		0.00801(260)	[117,118]
h23 Recoil corr.	(incl. in h20)	0.02123		0.02123	[112]
h24 eVP + proton structure corr., α^6	-0.0026				
h25 eVP corr. to finite-size (similar to $\epsilon_{\text{VP}2}$)		-0.00114		-0.0018 $r_Z - 0.0001$	Eq. (109) in [80]
h26 eVP corr. to finite-size (similar to $\epsilon_{\text{VP}1}$)		-0.00114		-0.00114(20)	
h27 Proton structure corr., $\alpha(Z\alpha)^5$	-0.0017				
h28 Rel. + radiative RC with p AMM, α^6	0.0018				
Sum	22.8148(20) ^c	22.9839(26) - 0.1604 r_Z		22.9858(26) - 0.1621(10) $r_Z - 0.0022(5) r_E^2$	
Sum with $r_E = 0.841 \text{ fm}, r_Z = 1.045 \text{ fm}$ [28]	22.8148 meV	22.8163 meV		22.8149 meV	

^a Includes a correction $\alpha(Z\alpha)^5$ due to μ VP.

^b Calculated using the Simon et al. form factor.

^c The uncertainty is 0.0078 meV if the uncertainty of the Zemach term (h20) is included (see Table II of [72]).

- 28 M.O. Distler, J.C. Bernauer, T. Walcher, Phys. Lett. B 696, 343 (2011)
- 80 P. Indelicato, arXiv:1210.5828v2 [PRA 87, 022501 (2013)]
- 112 C.E. Carlson, V. Nazaryan, K. Griffioen, Phys. Rev. A 78, 022517 (2008)
- 113 S.G. Karshenboim, E.Y. Korzinin, V.G. Ivanov, JETP Lett. 88, 641 (2008)
- 114 S.G. Karshenboim, E.Y. Korzinin, V.G. Ivanov, JETP Lett. 89, 216 (2009)
- 115 S.J. Brodsky, G.W. Erickson, Phys. Rev. 148, 26 (1966)
- 116 M.I. Eides, Phys. Rev. A 85, 034503 (2012)
- 117 C.E. Carlson, V. Nazaryan, K. Griffioen, Phys. Rev. A 83, 042509 (2011)
- 118 E. Cherednikova, R. Faustov, A. Martynenko, Nuclear Phys. A 703, 365 (2002)

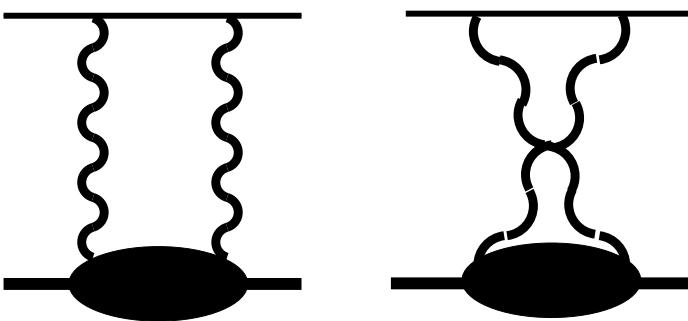
Discussions: 3rd Zemach moment



- PLB 693, 555 De Rujula: “*QED is not endangered by the proton’s size*” (1008.3861)
A large **third Zemach moment** $\langle r_p^3 \rangle_{(2)} = \int d^3r_1 d^3r_2 \rho(r_1) \rho(r_2) |r_1 - r_2|^3$ of the proton can explain all three measurements: μ_p , H, e-p
 $\rho(r)$ is not a simple Dipole, but has “core” and “tail”
- PRC 83, 012201 Cloet, Miller: “*Third Zemach moment of the proton*” (1008.4345)
Such a large third Zemach moment is **impossible**.
$$\langle r_p^3 \rangle_{(2)} \text{ (De Rujula)} = 36.6 \pm 6.9 \text{ fm}^3$$
$$\langle r_p^3 \rangle_{(2)} \text{ (Sick)} = 2.71 \pm 0.13 \text{ fm}^3$$
- PLB 696, 343 Distler *et al*: “*The RMS radius of the proton and Zemach moments*” (1011.1861)
$$\langle r_p^3 \rangle_{(2)} \text{ (Mainz 2010)} = 2.85 \pm 0.08 \text{ fm}^3$$

Discussions: Proton polarizability

proton polarizability aka. two-photon exchange



Seems to be the only contribution which *might* be able to solve the proton size puzzle by changing theory in μ_p .

Keep in mind:

Discrepancy: 0.31 meV

Polarizability: 0.015(4) meV **20 times smaller!**

Discussions: Proton polarizability



- G.A. Miller *et al.*, PRA **84**, 020101(R) (2011)
“Toward a resolution of the proton size puzzle”
 - New off-mass-shell effect $\sim \alpha \frac{m^4}{M^3}$ solves puzzle.
- R.J. Hill, G. Paz, PRL, **107**, 160402 (2011)
“Model independent analysis of proton structure for hydrogenic bound states”
 - forward Compton amplitude’s $W_1(0, Q^2)$ is now well known
 - “Crazy” functional behaviour can give any correction.
 - No numbers given.
- C.E. Carlson, M. Vanderhaeghen, PRA **84**, 020102(R) (2011)
“Higher-order proton structure corrections to the Lamb shift in muonic hydrogen”
 - All off-shell effects are automatically included in standard treatment.
- C.E. Carlson, M. Vanderhaeghen, arXiv 1109.3779 (atom-ph)
“Constraining off-shell effects using low-energy Compton scattering”
 - Off-shell effects are 100 times smaller than needed to explain the puzzle.

Discussions: Proton polarizability



- M.C. Birse, J.A. McGovern, Eur. Phys. J. A 48, 120 (2012)
“Proton polarisability contribution to the Lamb shift in muonic hydrogen at fourth order in chiral perturbation theory”
 - Calculate $T_1(0, Q^2)$ in heavy-baryon chiral pert. theory.
 - Proton polarizability is **not** responsible for the radius puzzle.
- Gorchtein, Llanes-Estrada, Szczepaniak, PRA 87, 052501 (2013)
“ μ -H Lamb shift: dispersing the nucleon-excitation uncertainty with a finite energy sum rule”
 - Sum rule + virtual photoabsorption data.
 - *“We conclude that nucleon structure-dependent uncertainty by itself is unlikely to resolve the large discrepancy...”*
- Karshenboim, McKeen, Pospelov, arXiv 1401.6156 [hep-ph]
“Constraints on muon-specific dark forces”
 - *“These estimates show that if indeed large muon-proton interactions are responsible for the r_p discrepancy, one can no longer insist that theoretical calculations of the muon $g - 2$ are under control. Thus, a resolution of the r_p problem is urgently needed in light of the new significant investments made in the continuation of the experimental $g - 2$ program.”*

Discussions: Proton polarizability



- Proton off-shell effects can in principle shift the μ_p value.
- Evil subtraction function.
- Evidence is growing, that this effect can **NOT** solve the puzzle.
- Clarification needed [$(g - 2)_\mu$!]

What may be wrong?

$$\tilde{L}_{\mu p}^{\text{theo.}}(r_p^{\text{CODATA}}) - \tilde{L}_{\mu p}^{\text{exp.}} = \begin{cases} 75 \text{ GHz} \\ 0.31 \text{ meV} \\ 0.15 \% \end{cases}$$

μp theory wrong?
 μp experiment wrong?
 H theory wrong?
 H experiments wrong? → R_∞ wrong?
 AND e-p scattering exp. wrong?

Standard Model wrong?!?

Discussions: New Physics



- Jaeckel, Roy, PRD **82**, 125020 (2010)
“Spectroscopy as a test of Coulomb’s law - A probe of the hidden sector”
hidden photons, minicharged particles → deviations from Coulomb’s law.
 μp transition can NOT be explained this. (contradicts Lamb shift in H)
- U.D. Jentschura, Ann. Phys. **326**, 516 (2011)
“Lamb shift in muonic hydrogen – II. Analysis of the discrepancy of theory and experiment”
no millicharged particles, no unstable neutral vector boson.
- Barger, Chiang, Keung, Marfatia, PRL **106**, 153001 (2011)
“Proton size anomaly”
decay of Υ , J/ψ , π^0 , η , neutron scattering, muon g-2, $\mu^{24}\text{Mg}$, $\mu^{28}\text{Si}$
⇒ It’s NOT a new flavor-conserving spin-0, 1 or 2 particle
- Tucker-Smith, Yavin, PRD **83**, 101702 (2011)
“Muonic hydrogen and MeV forces”
MeV force carrier can explain discrepancies for r_p and $(g-2)_\mu$
IF coupling to e , n is suppressed relative to coupling to μ , p
prediction for μHe^+ , $\mu^+\mu^-$

Discussions: New Physics



- Batell, McKeen, Pospelov, PRL **107**, 011803 (2011)
“*New Parity-violating muonic forces and the proton charge radius*”
10...100 MeV heavy photon (“light Higgs”) can explain r_p and $(g-2)_\mu$
prediction for μHe^+ , enhanced PNC in muonic systems
- Barger, Chiang, Keung, Marfatia, PRL **108**, 081802 (2011)
“*Constraint on Parity-violating muonic forces*”
No missing mass events observed in leptonic Kaon decay.
⇒ constraints on light Higgs.
- Pospelov (private comm.)
Lack of missing mass events in leptonic Kaon decays no problem.
Light Higgs is short-lived (decays inside the detector).
- C.E. Carlson, B.C. Rislow, PRD **86**, 035013 (2012)
“*New physics and the proton radius problem*”
“*New physics with fine-tuned couplings may be entertained as a possible explanation for the Lamb shift discrepancy.*”

Discussions: New Physics



- Wang, Ni, Mod. Phys. Lett. A **28**, 1350094 (2013)
“*Proton puzzle and large extra dimensions*” (arXiv 1303.4885)
“*Extra gravitational force between the proton and the muon at very short range provides an energy shift which accounts for the discrepancy...*”
- Li, Chen, arXiv 1303.5146
“*Can large extra dimensions solve the proton radius puzzle?*”
“*We find that such effect could be produced by four or more large extra dimensions which are allowed by the current constraints from low energy physics.*”
- R. Onofrio, Eur. Phys. Lett. **104**, 20002 (2013)
“*Proton radius puzzle and quantum gravity at the Fermi scale*” (1312.3469)
“*We show how the proton radius puzzle ... may be solved by means of ... an effective Yukawian gravitational potential related to charged weak interactions. [...] Muonic hydrogen plays a crucial role to test possible scenarios for a gravitoweak unification, with weak interactions seen as manifestations of quantum gravity effects at the Fermi scale.*”

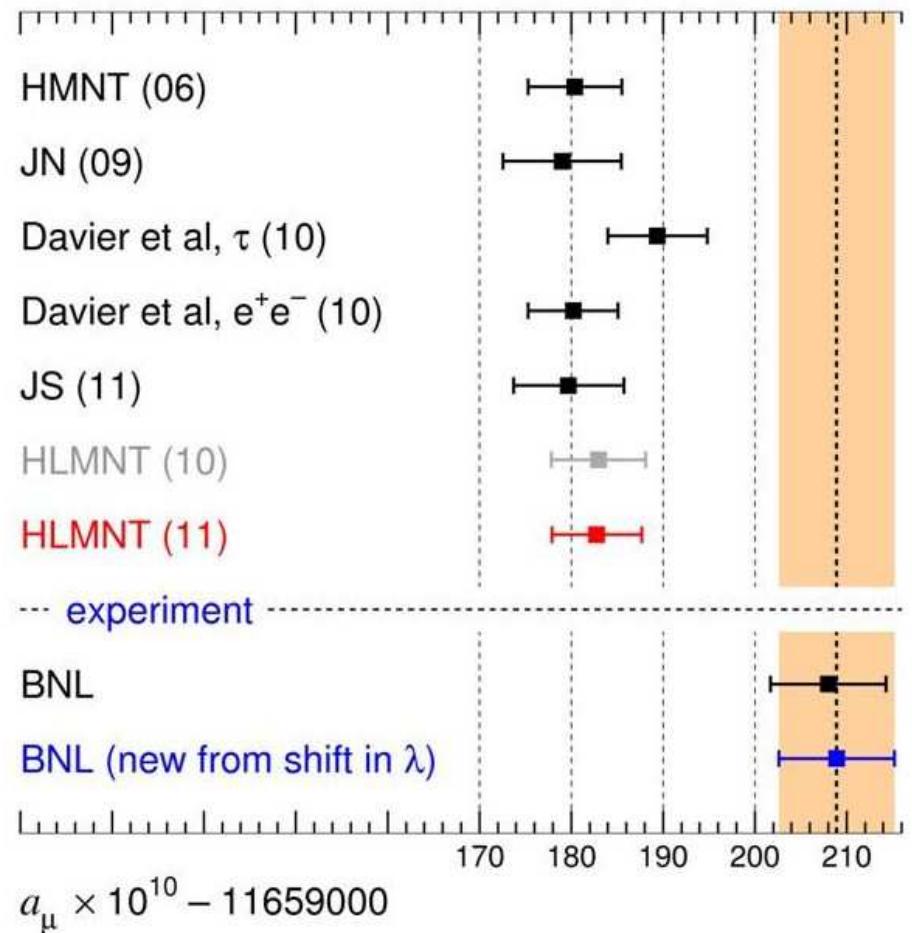
There are **TWO** muon puzzles.

Two muon puzzles

- **Anomalous magnetic moment** of the muon

The measured value of $a_\mu = (g - 2)/2$ of the muon has been in disagreement with the SM predictions for >10 years now!

The discrepancy stands at $\sim 3.6\sigma$



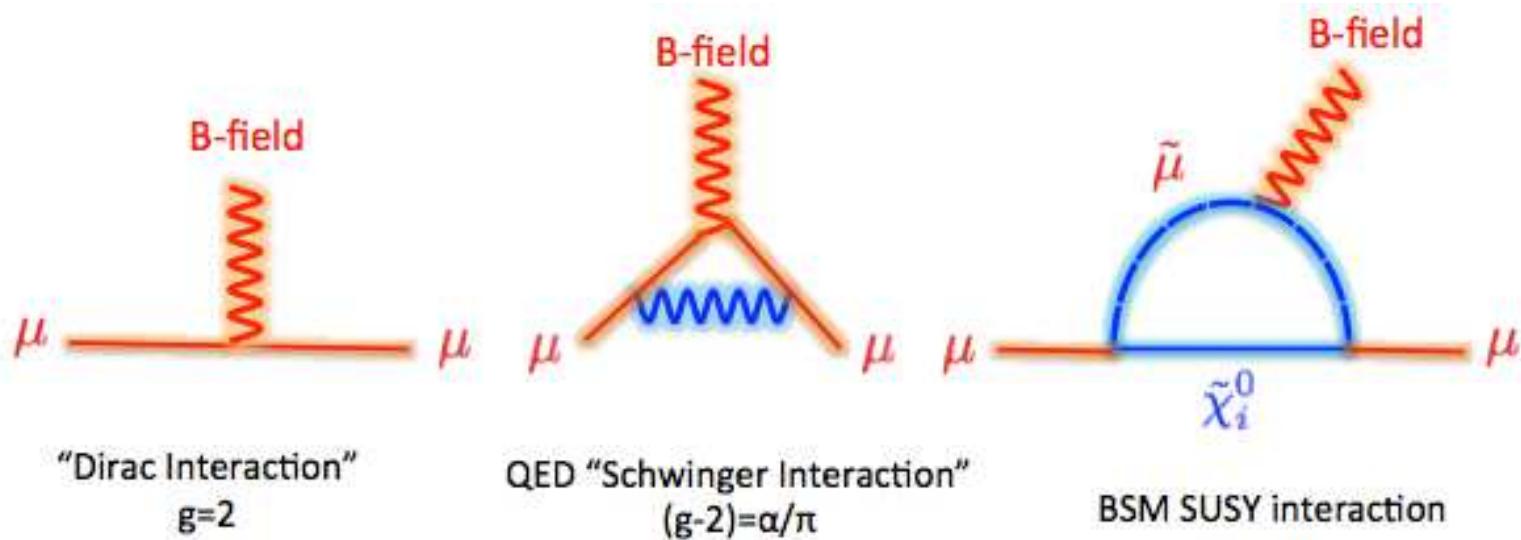
J. Phys. G 38, 085003 (2011)

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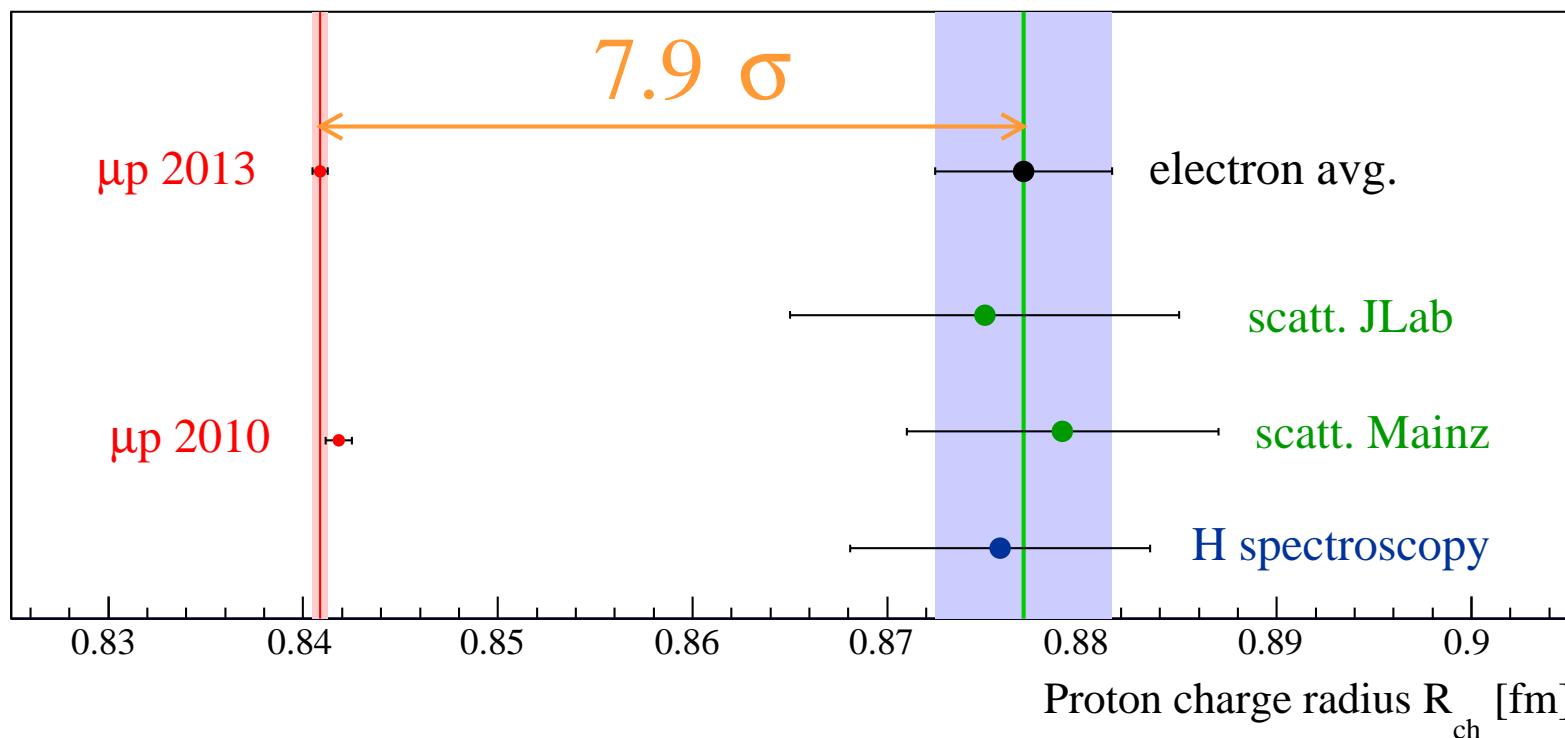


<http://www.hep.ucl.ac.uk/muons/g-2/>

Two muon puzzles

- Anomalous magnetic moment of the muon $\sim 3.6\sigma$
- Proton radius from muonic hydrogen

The measured value of the proton rms charge radius from muonic hydrogen μp is 10 times more accurate, but 4% smaller than the value from both **hydrogen spectroscopy** and **elastic electron proton scattering**.



RP et al., Nature 466, 213 (2010); Science 339, 417 (2013); ARNPS 63, 175 (2013).

Two muon puzzles

- Anomalous magnetic moment of the muon $\sim 3.6\sigma$
- Proton radius from muonic hydrogen $\sim 7.9\sigma$
- These 2 discrepancies may be **connected**.

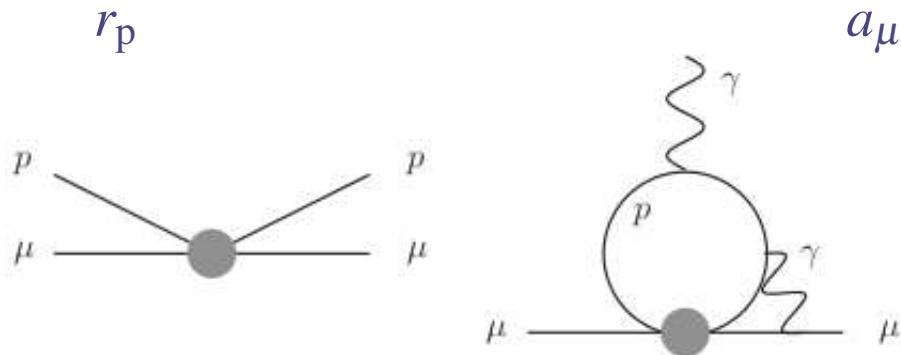
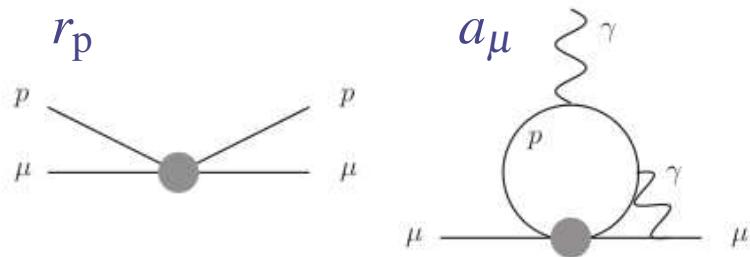


FIG. 1. Left:the effective proton-muon interaction resulting from unexpectedly large QCD effects or new physics that is responsible for the r_p discrepancy. Right: the two-loop contribution to the muon $g - 2$ that results from the interaction on the left after integrating out the proton.

Karshenboim, McKeen, Pospelov, arXiv 1401.6156

r_p and a_μ

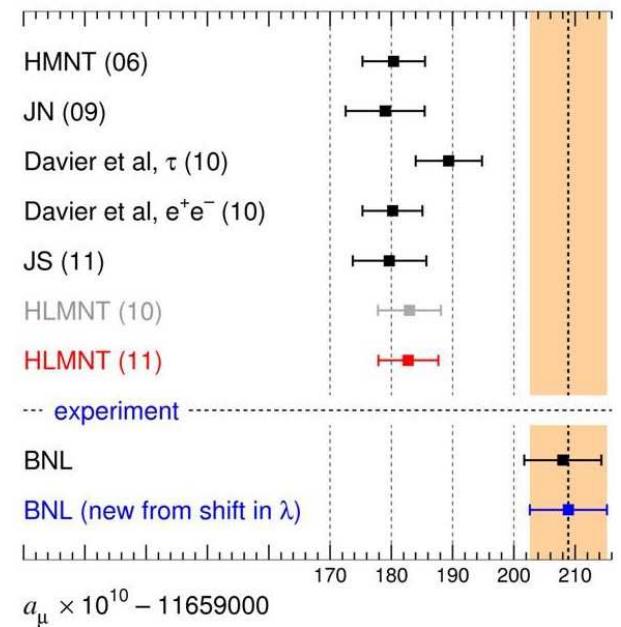
Both the r_p and the a_μ discrepancy could originate from the same new proton structure effect (two-photon-exchange) or “New light Physics” ($m \approx \text{MeV}$)



Fixing r_p could give rise to

$$5 \times 10^{-9} < |\Delta(a_\mu)| < 10^{-7} \quad (\text{for } \Lambda_{\text{had}} = m_\pi \dots m_p).$$

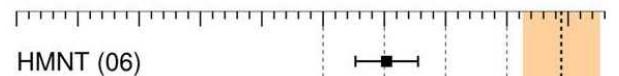
This is much larger than the $(g-2)_\mu$ discrepancy of $\sim 1 \times 10^{-9}$.



J. Phys. G 38, 085003 (2011).

r_p and a_μ

Both the r_p and the a_μ discrepancy could originate from the same (e.g. gluon exchange) effect.



Fixing r_p could

$$5 \times 10^{-9} <$$

This is much

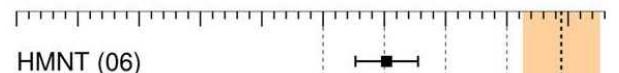


June 22 – July 25, 2013

after Pospelov
Karshenboim, McKeen, Pospelov, arXiv 1401.6156

r_p and a_μ

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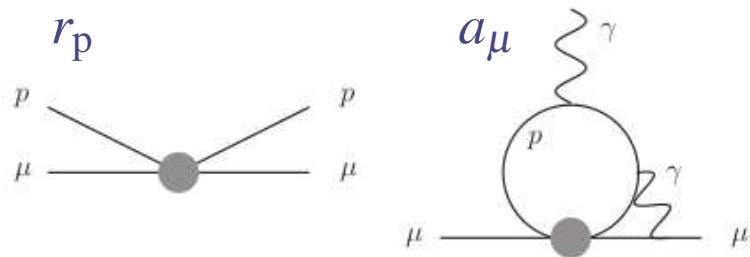


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r_p and a_μ

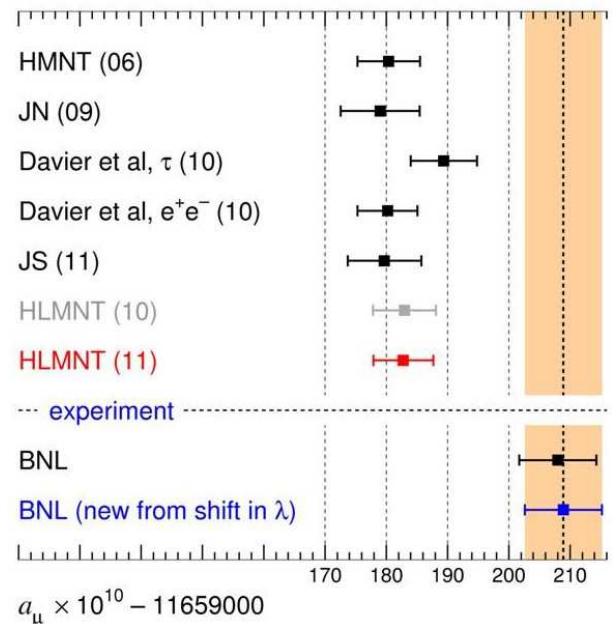
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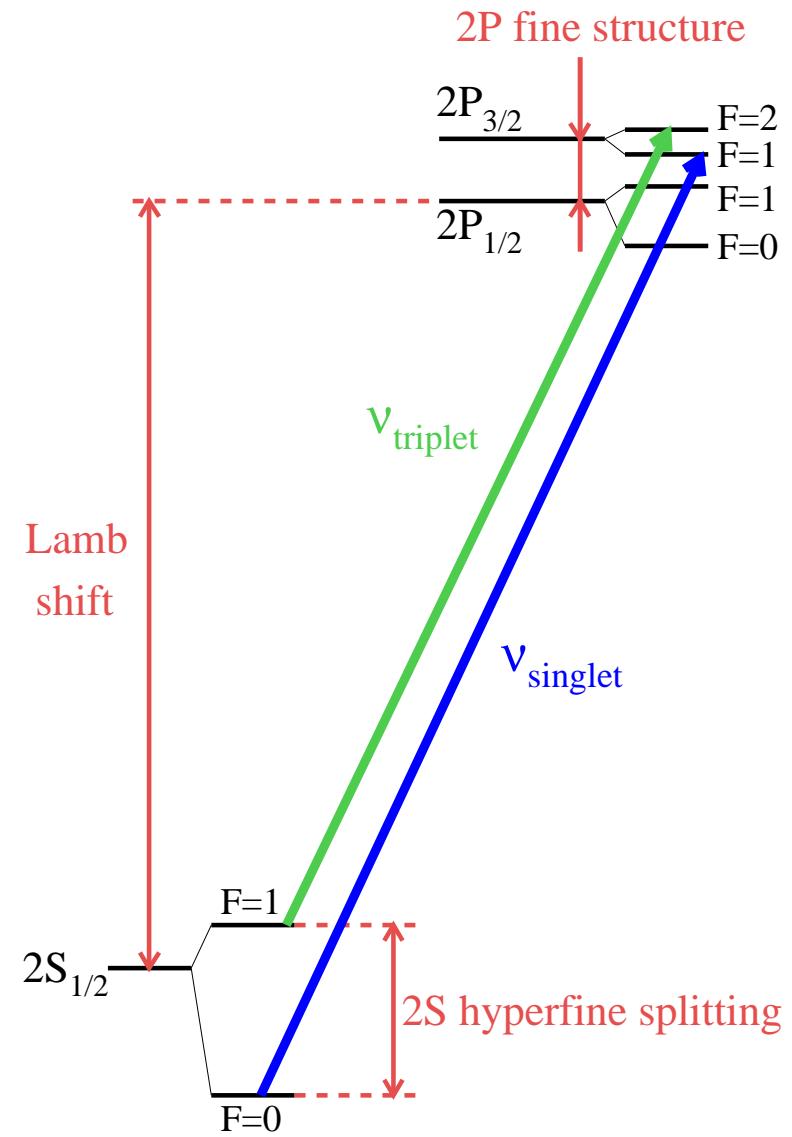


J. Phys. G 38, 085003 (2011).

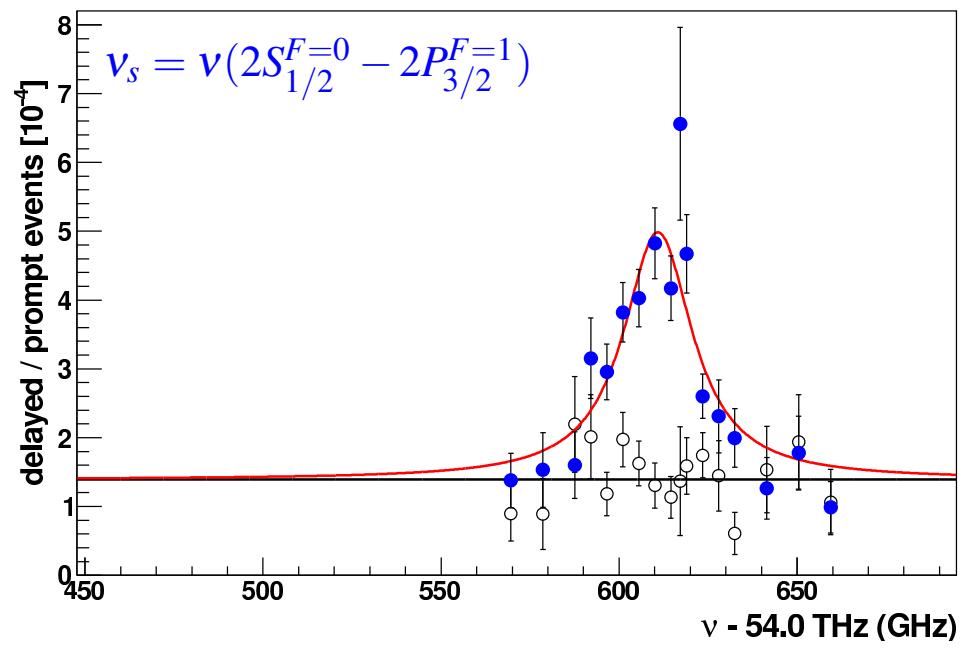
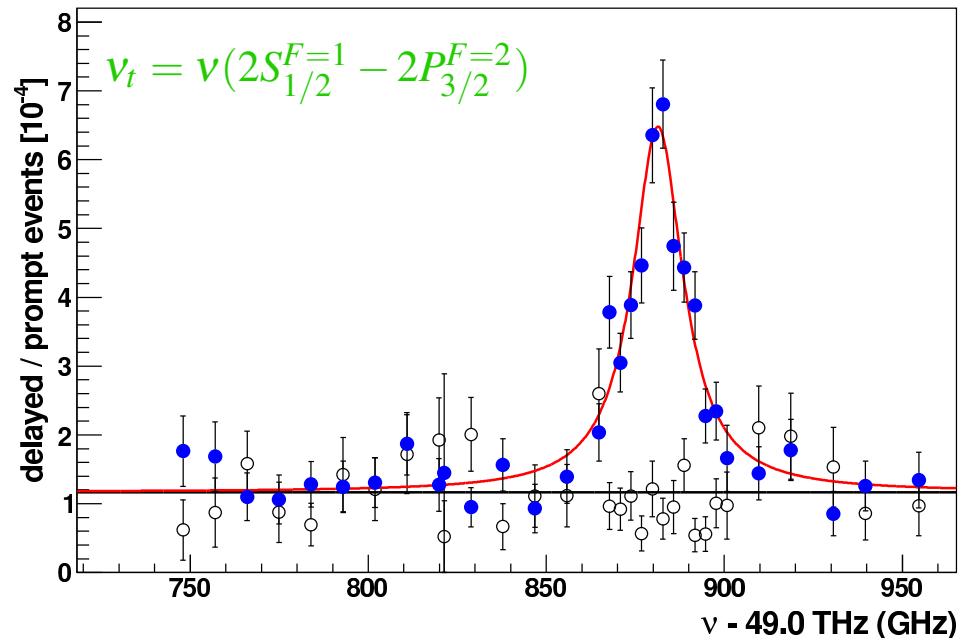
Maybe one can invert the argument:

a_μ “not so wrong” $\implies r_p$ is not due to proton TPE or this kind of BSM

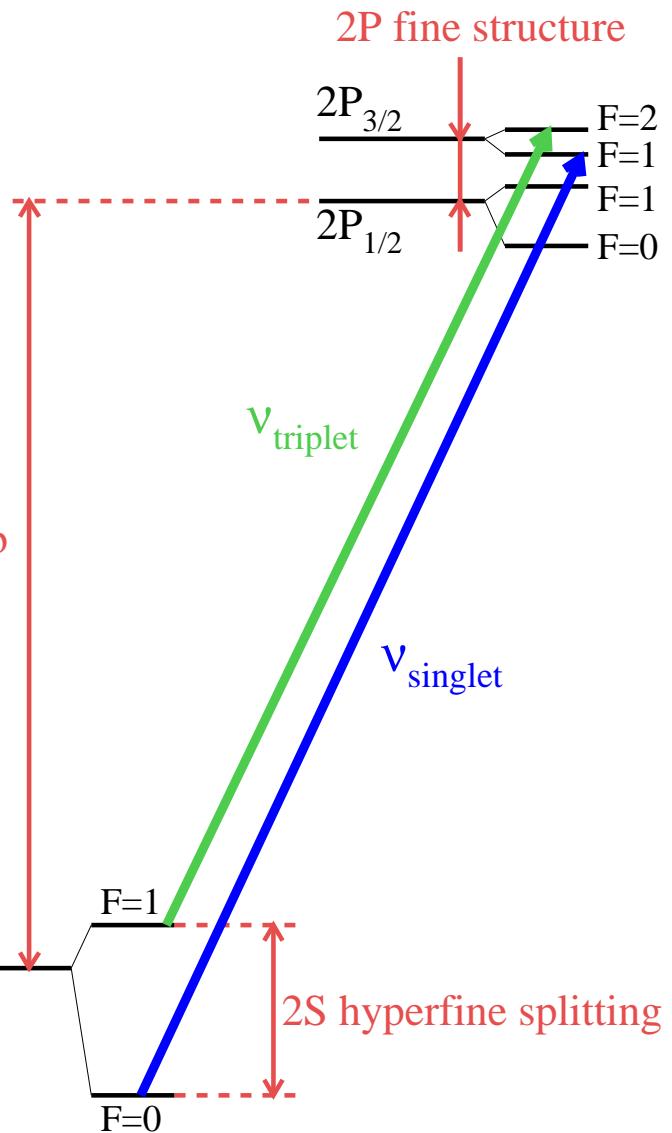
We have measured two transitions in μ p



R. Pohl *et al.*, Nature 466, 213 (2010).
A. Antognini, RP *et al.*, Science 339, 417 (2013).



We have measured two transitions in μ p



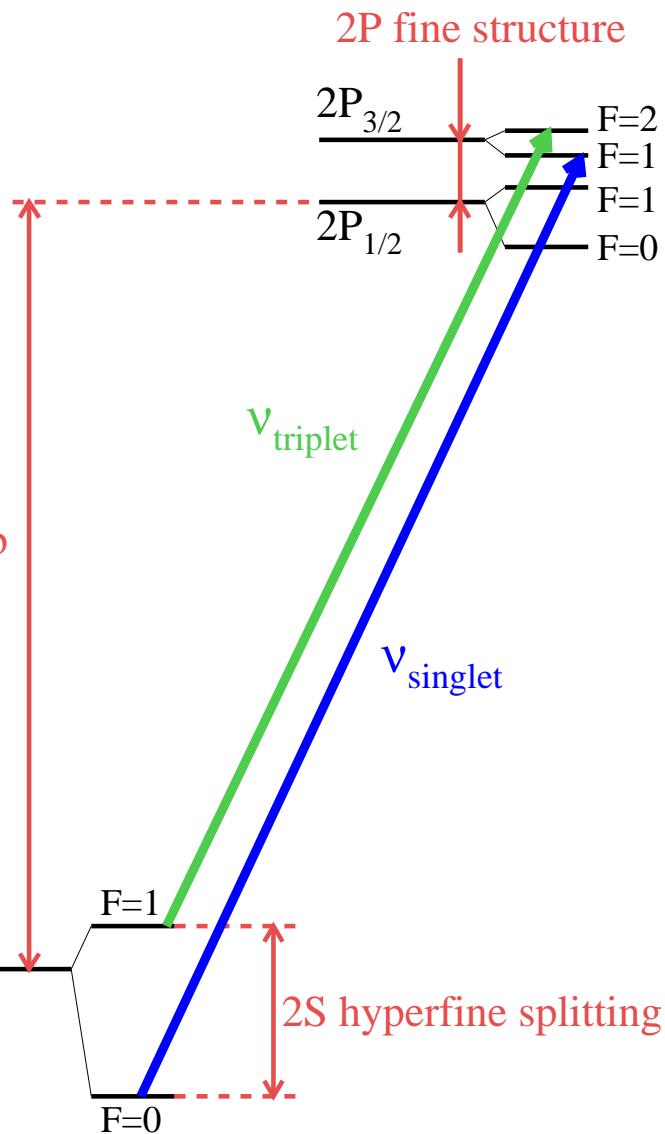
- Consider the two measurements separately

Two independent determinations of r_p

($v_t \rightarrow r_p$, $v_s \rightarrow r_p$)

Consistent results!

We have measured two transitions in μ p



- Consider the two measurements separately

Two independent determinations of r_p

($v_t \rightarrow r_p$, $v_s \rightarrow r_p$)

Consistent results!

- Combine the two measurements

Two measurements \rightarrow determine two parameters

$v_t, v_s \rightarrow \Delta E_L, \Delta E_{\text{HFS}} \rightarrow r_p, r_z$

$$\begin{aligned}\frac{3}{4}v_t + \frac{1}{4}v_s &= \Delta E_L(r_p) + 8.8123 \text{ meV} \\ v_s - v_t &= \Delta E_{\text{HFS}}(r_z) - 3.2480 \text{ meV}\end{aligned}$$

R. Pohl *et al.*, Nature 466, 213 (2010).

A. Antognini, RP *et al.*, Science 339, 417 (2013).

Proton Zemach radius

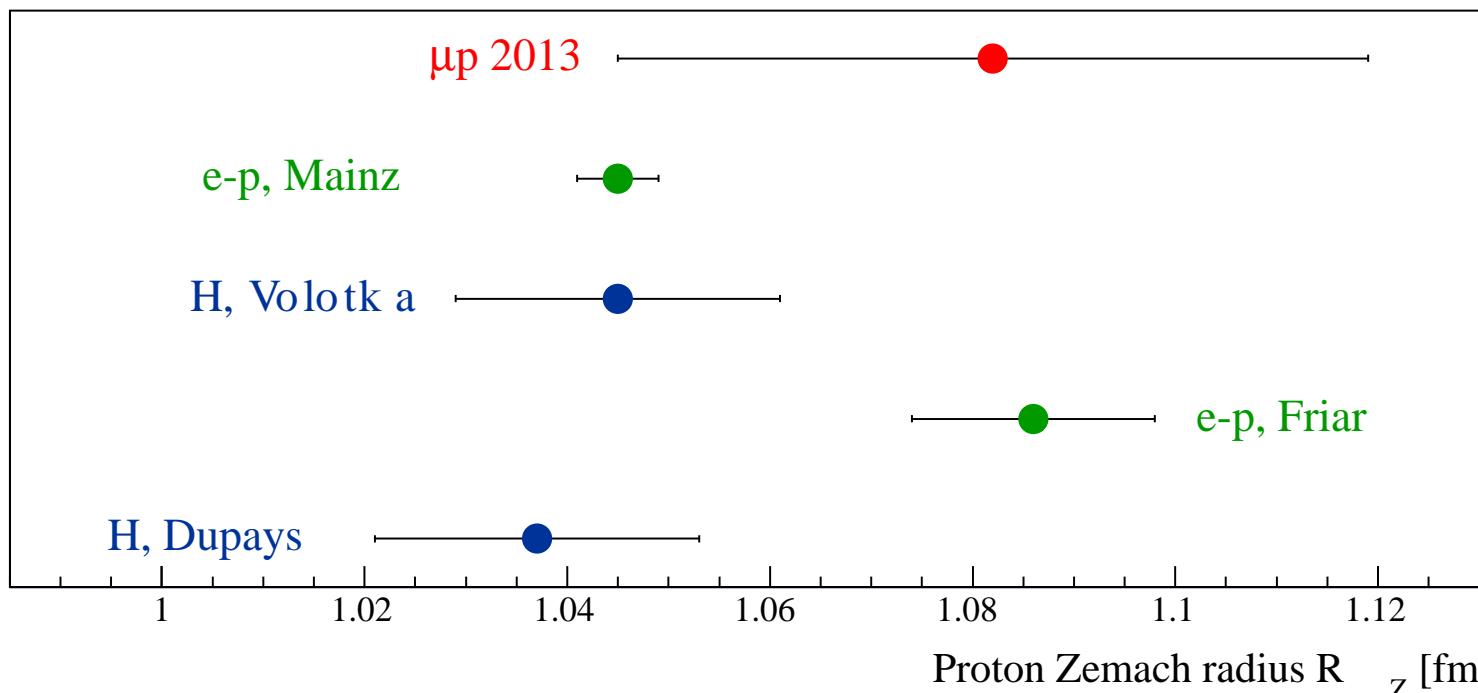
2S hyperfine splitting in μp is: $\Delta E_{\text{HFS}} = 22.9843(30) - 0.1621(10) r_Z$ [fm] meV

$$\text{with } r_Z = \int d^3r \int d^3r' r \rho_E(r) \rho_M(r - r')$$

We measured

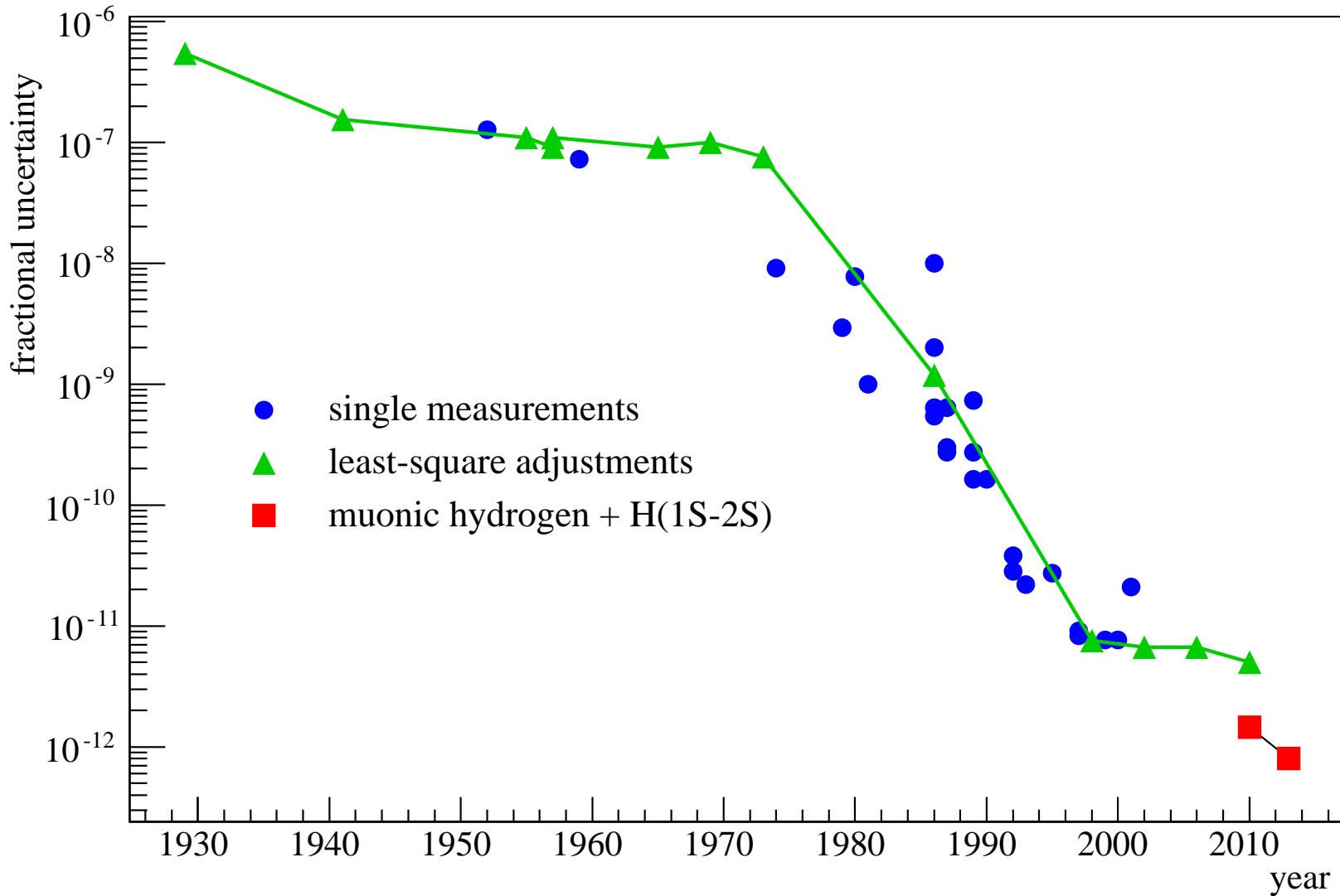
$$\Delta E_{\text{HFS}} = 22.8089(51) \text{ meV}$$

This gives a proton Zemach radius $r_Z = 1.082(31)_{\text{exp}}(20)_{\text{th}} = 1.082(37) \text{ fm}$



A. Antognini, RP et al., Science 339, 417 (2013)

Rydberg constant



H(1S-2S): C.G. Parthey, RP *et al.*, PRL 107, 203001 (2011).

r_p : A. Antognini, RP *et al.*, Science 339, 417 (2013).

Rydberg constant

Hydrogen spectroscopy (Lamb shift):

$$L_{1S}(r_p) = 8171.636(4) + 1.5645 \langle r_p^2 \rangle \text{ MHz}$$



2S ————— 2P

$$E_{nS} \simeq -\frac{R_\infty}{n^2} + \frac{L_{1S}}{n^3}$$

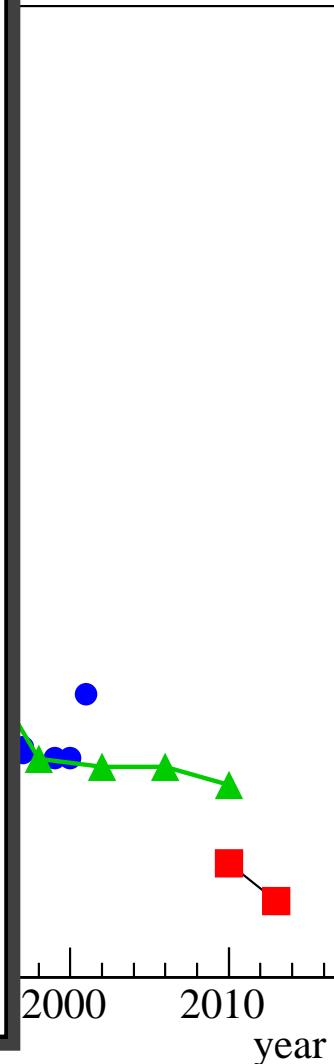
1S-2S

2 unknowns \Rightarrow 2 transitions

- Rydberg constant R_∞
- Lamb shift $L_{1S} \leftarrow r_p$

1S

—
—

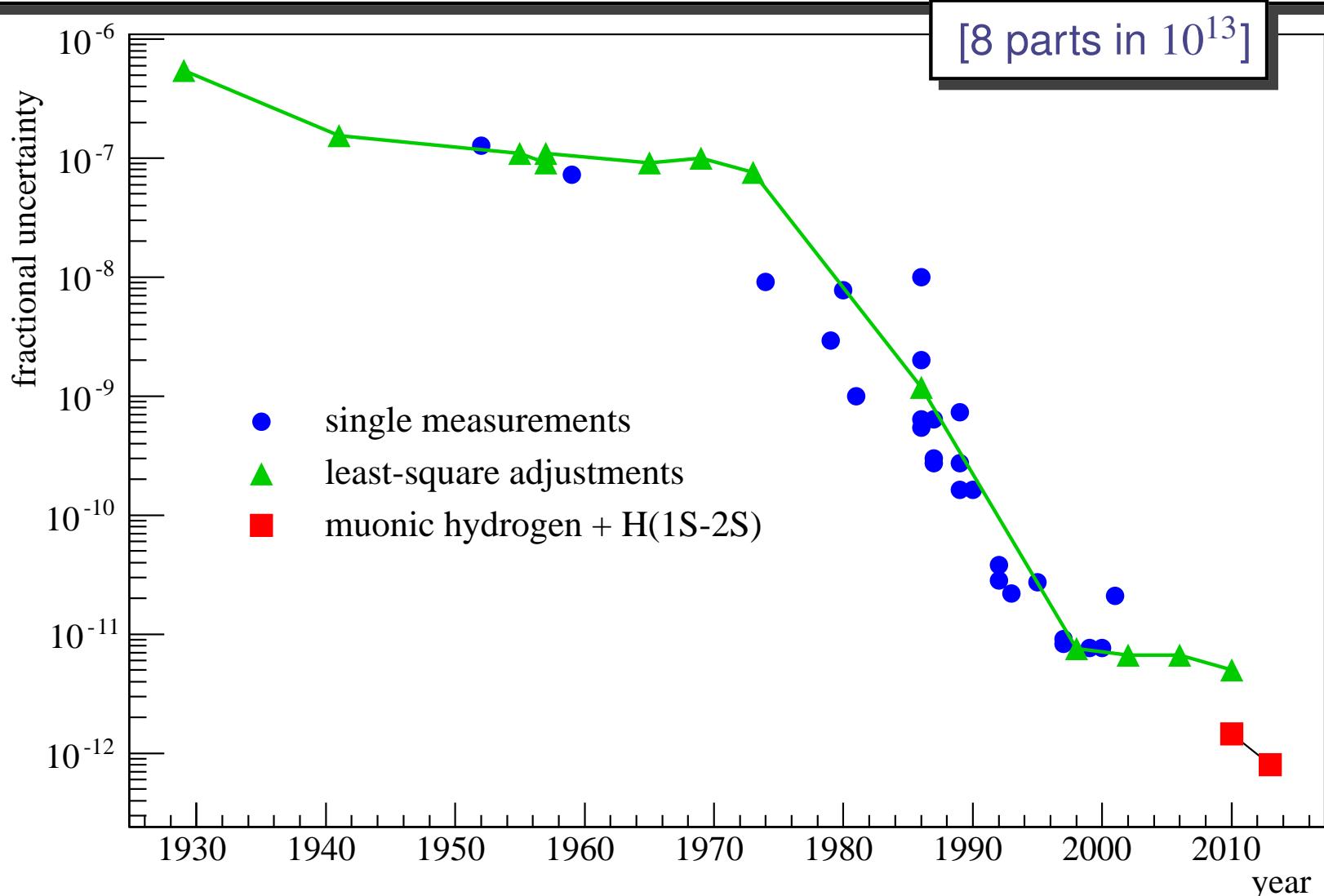


H(1S-2S): C.G. Parthey, RP *et al.*, PRL 107, 203001 (2011).

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Rydberg constant

$$R_\infty = 3.289\ 841\ 960\ 249\ 5 (10)^{r_p} (25)^{\text{QED}} \times 10^{15} \text{ Hz/c}$$

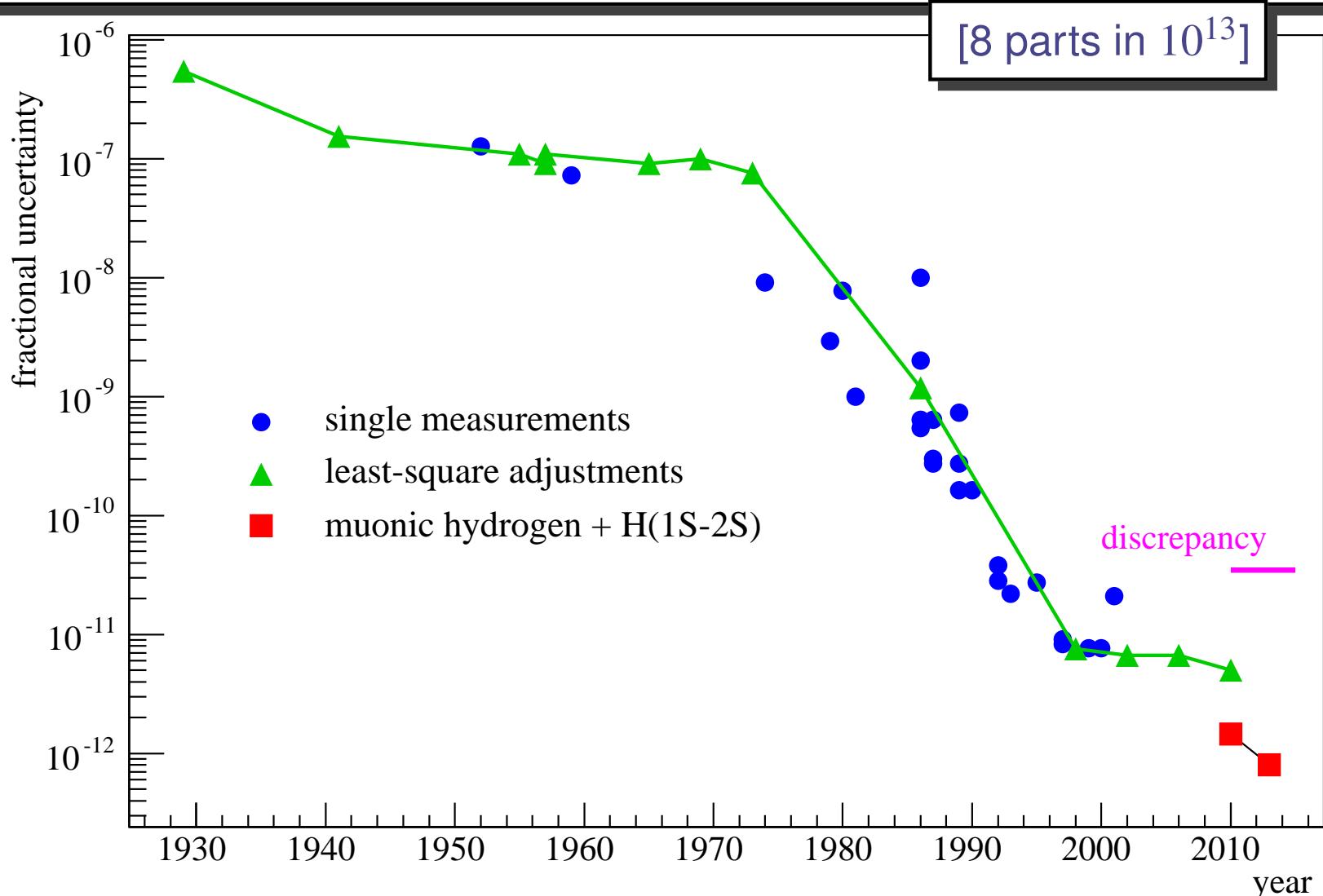


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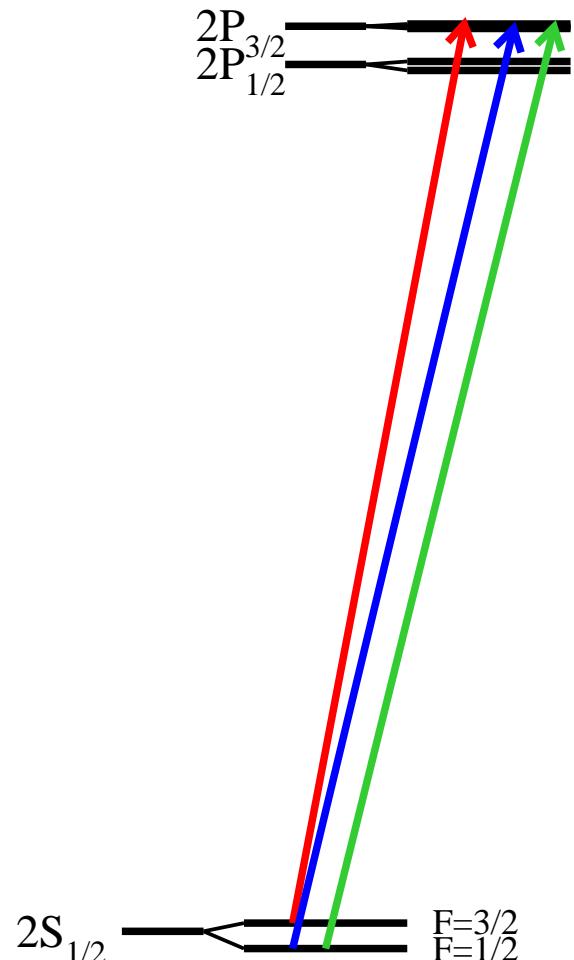


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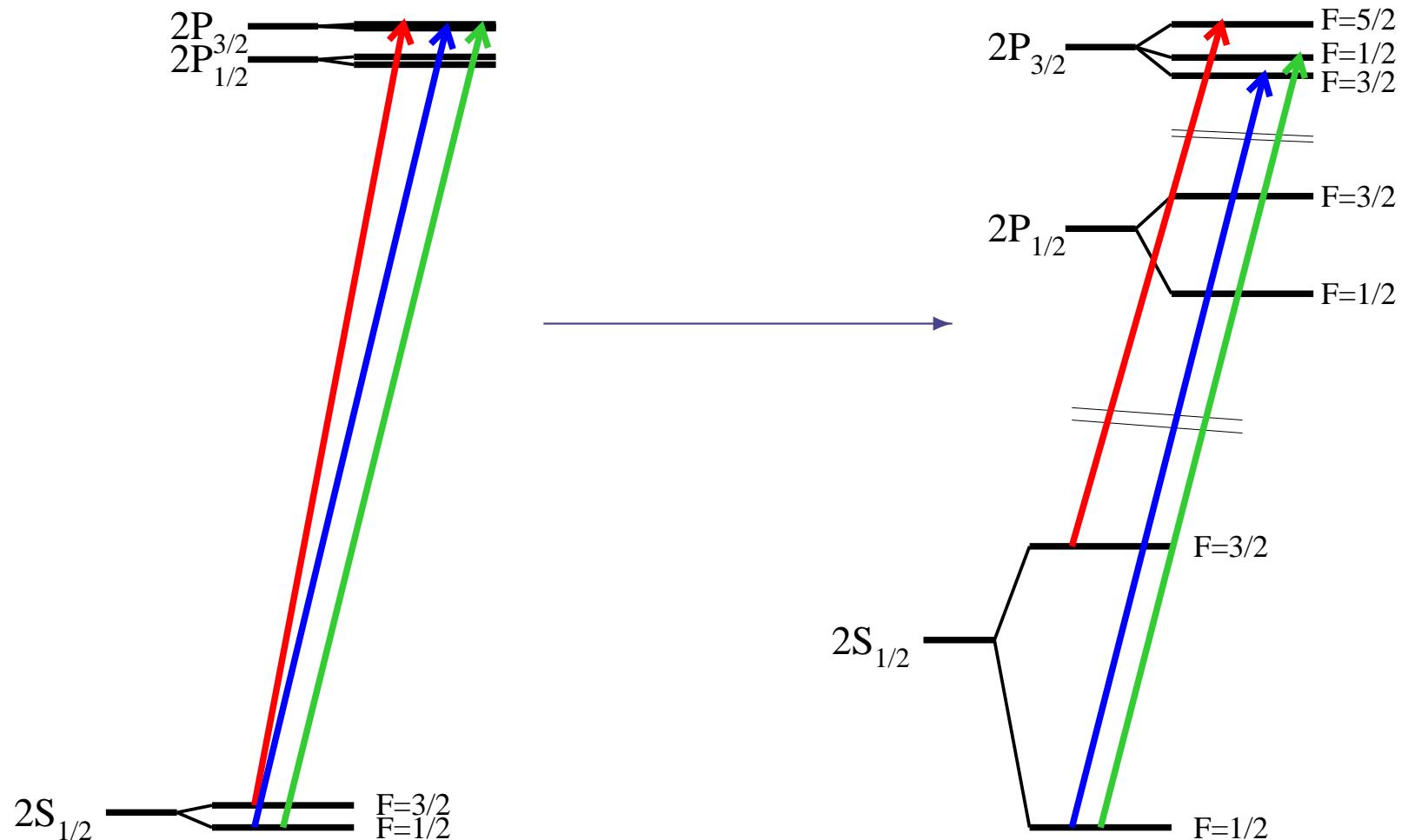
r_p : A. Antognini, RP *et al.*, Science 339, 417 (2013).

Muonic deuterium

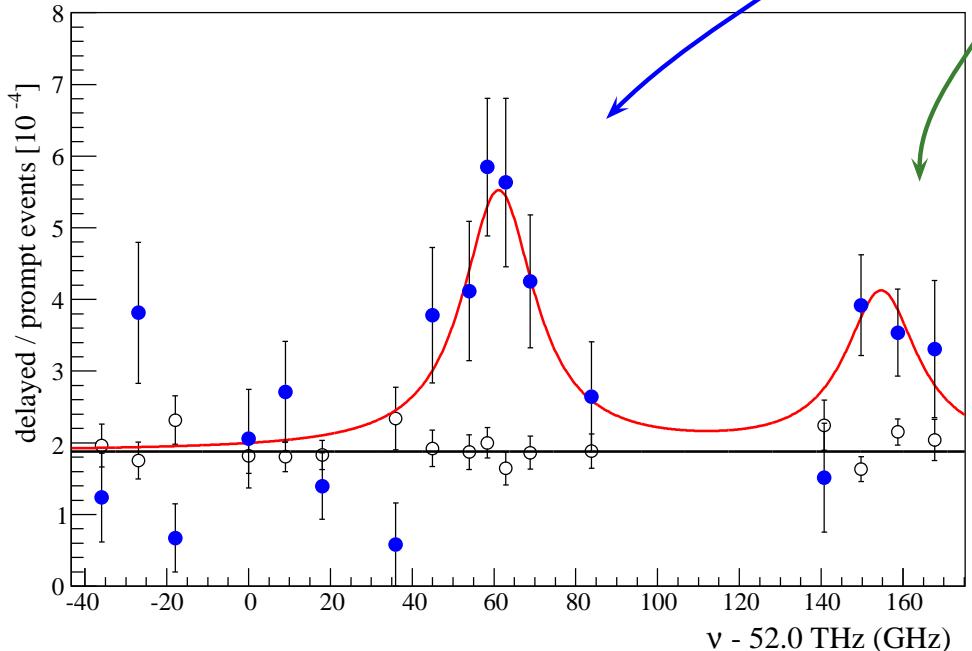
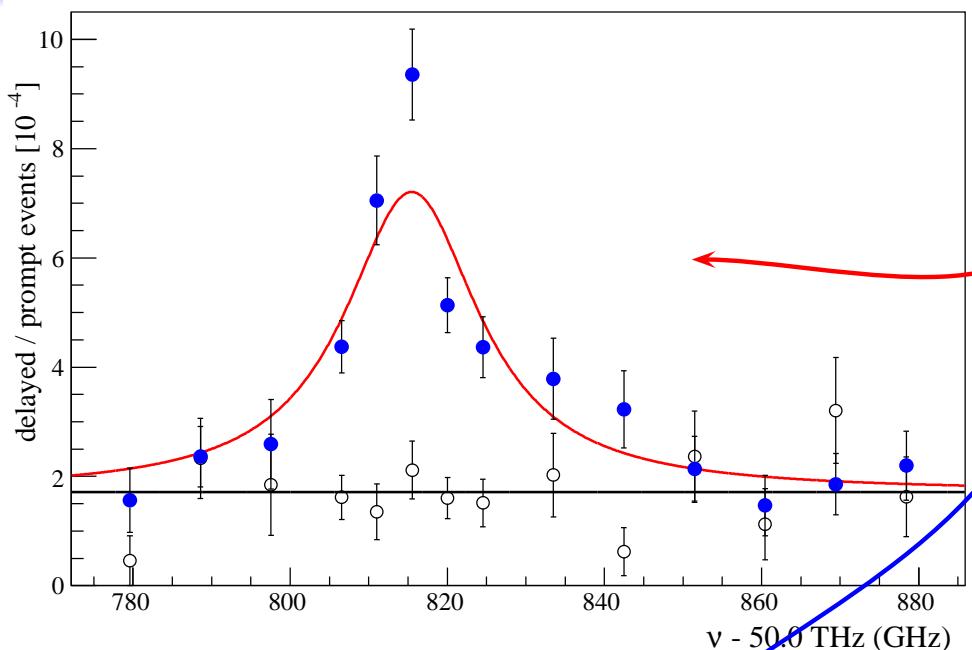
muonic deuterium



muonic deuterium



Muonic DEUTERIUM

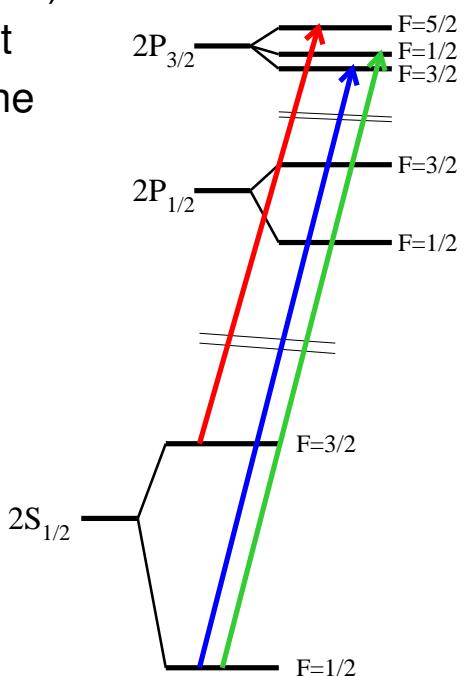


2.5 resonances in muonic **deuterium**

- μd [$2S_{1/2}(F=3/2) \rightarrow 2P_{3/2}(F=5/2)$]
20 ppm (stat., online)

- μd [$2S_{1/2}(F=1/2) \rightarrow 2P_{3/2}(F=3/2)$]
45 ppm (stat., online)

- μd [$2S_{1/2}(F=1/2) \rightarrow 2P_{3/2}(F=1/2)$]
70 ppm (stat., online)
only 5σ significant
identifies $F=3/2$ line



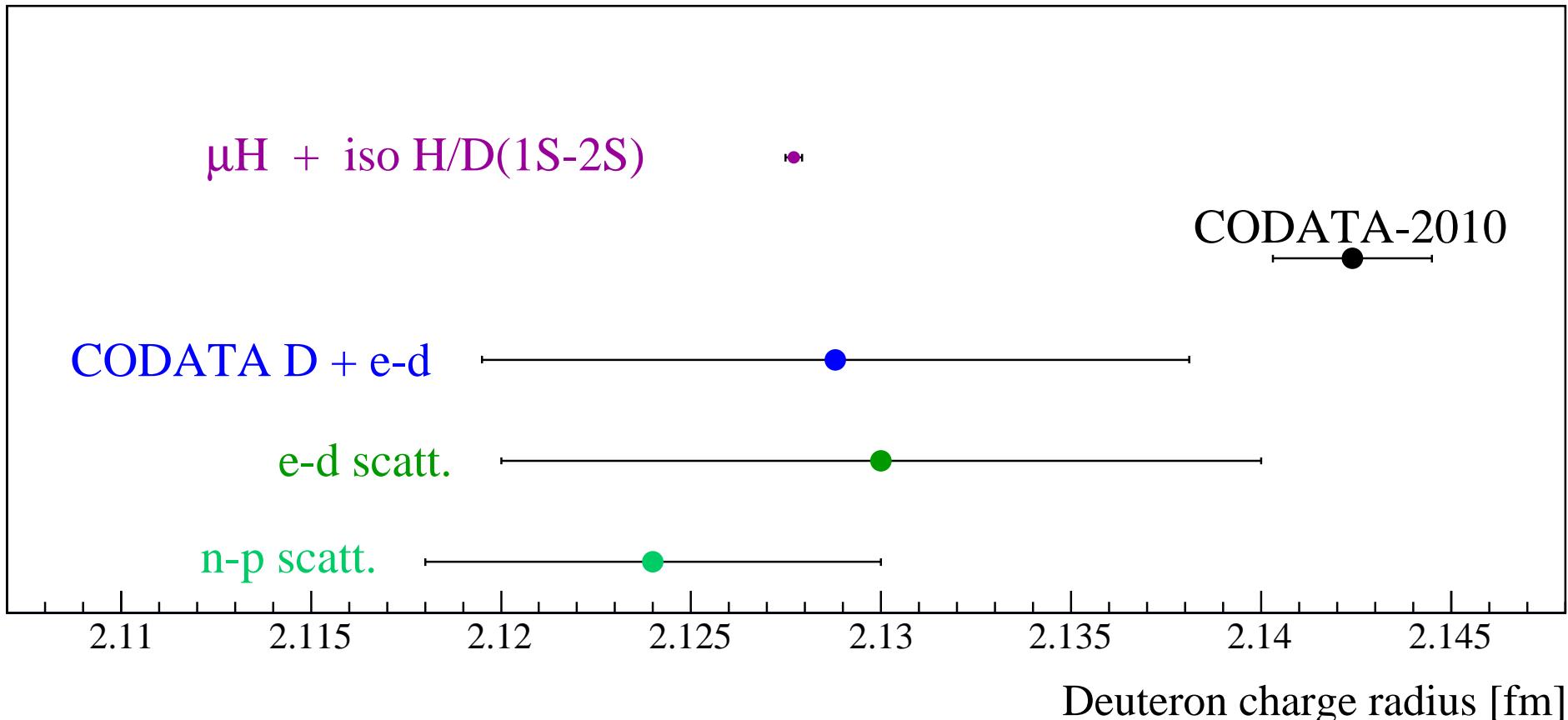
Deuteron charge radius

$$\text{H/D isotope shift: } r_d^2 - r_p^2 = 3.82007(65) \text{ fm}^2$$

C.G. Parthey, RP *et al.*, PRL **104**, 233001 (2010)

CODATA 2010 $r_d = 2.14240(210) \text{ fm}$

$r_p = 0.84087(39) \text{ fm}$ from μH gives $r_d = 2.12771(22) \text{ fm}$



Deuteron charge radius

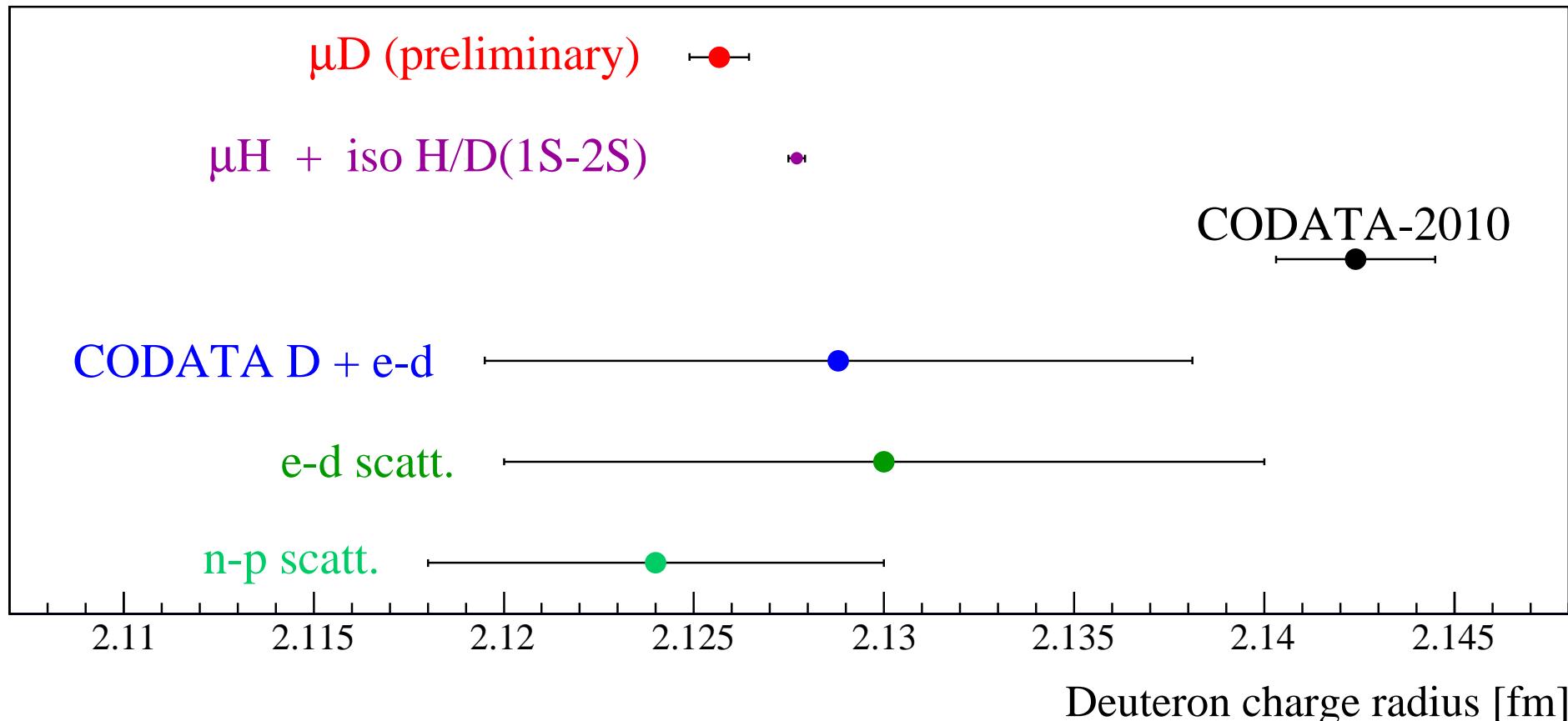
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Lamb shift in muonic DEUTERIUM $r_d = 2.125XX(13)_{\text{exp}}(77)_{\text{theo}} \text{ fm}$ PRELIM.!!



Results from muonic deuterium (prel.)



Lamb shift in muonic deuterium:

$$\Delta E_{\text{LS}}^{\text{theo}} = 228.7766(10) \text{ meV} + \Delta E^{\text{TPE}} - 6.1103(3) r_d^2 \text{ meV/fm}^2$$

with deuteron polarizability (TPE) $\Delta E^{\text{TPE}}(\text{theo}) = 1.7096(200) \text{ meV}$

J.J. Krauth *et al.*, Ann. Phys. (accepted) [1506.01298]

$$r_d(\mu d) = 2.125\text{XX}(13)_{\text{exp}}(77)_{\text{theo}} \text{ fm} \quad (\text{preliminary})$$

$$r_d(\mu p + \text{iso}) = 2.12771(22) \text{ fm} \quad (\text{from } r_p(\mu p) \text{ and H/D(1S-2S)}) \quad 2.6\sigma$$

$$r_d(\text{CODATA}) = 2.14240(210) \text{ fm} \quad 7.5\sigma$$

$$\text{Discrepancy to } \Delta E_{\text{LS}}(r_d(\text{CODATA})) = 0.438(59) \text{ meV}$$

$$(\text{"proton radius puzzle"} \text{ (}\mu p\text{ discrepancy)} = 0.329(47) \text{ meV})$$

CREMA coll., submitted (2016)

Muonic helium ions.

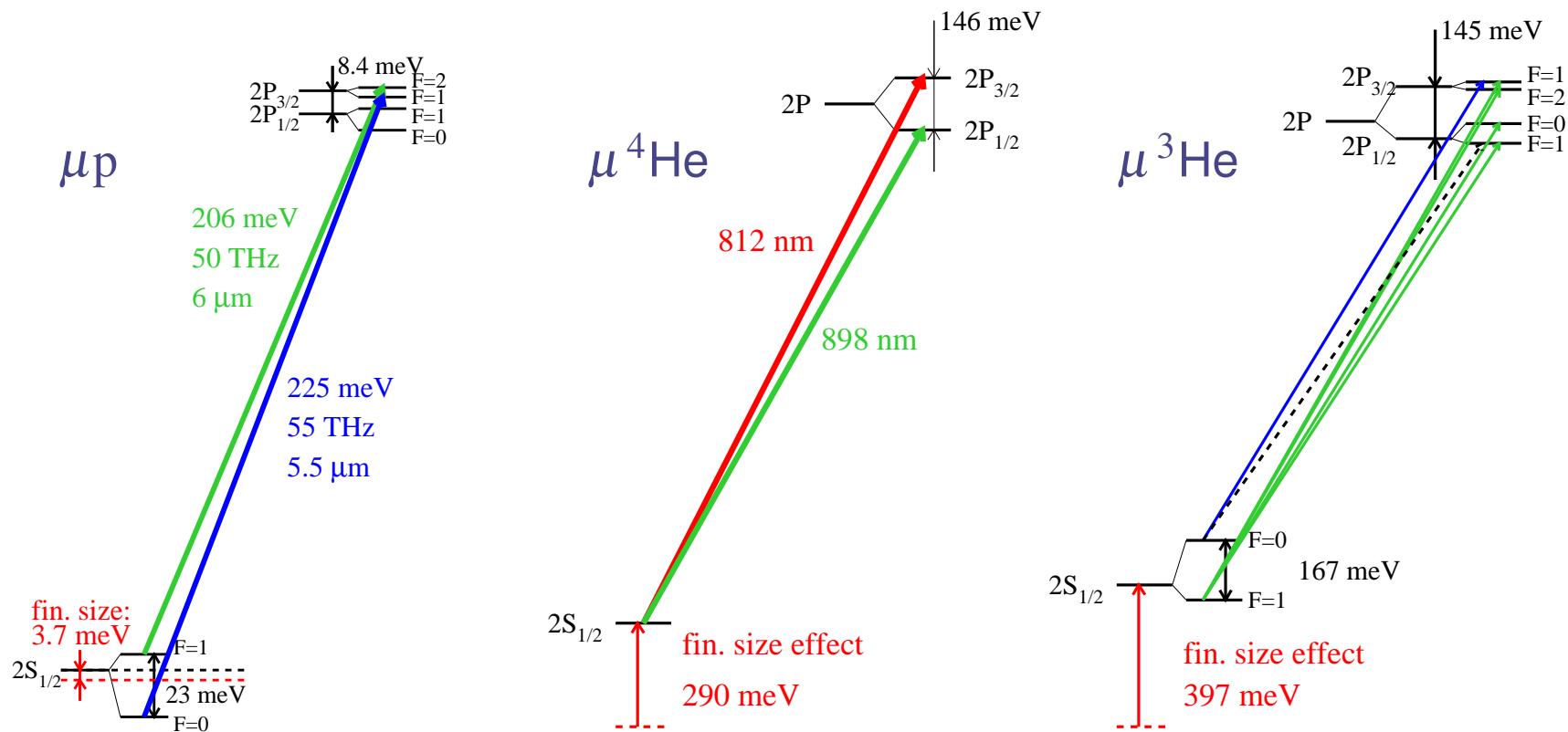
Lamb shift in muonic helium



- Goal: Measure $\Delta E(2S-2P)$ in $\mu^4\text{He}$, $\mu^3\text{He}$ to ~ 50 ppm
- ⇒ alpha particle and helion charge radius to 3×10^{-4} (± 0.0005 fm),
This is **10 times better** than from electron scattering.
- Solve discrepancy in ${}^3\text{He} - {}^4\text{He}$ isotope shift.

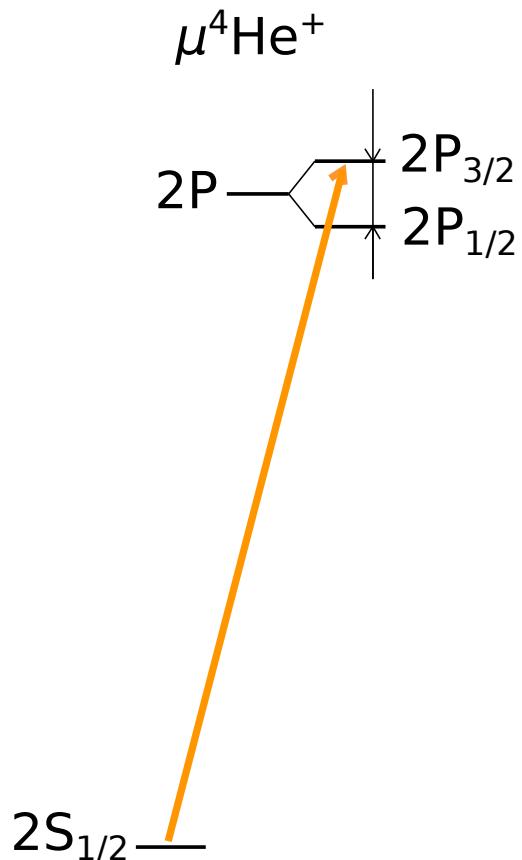
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Lamb shift in muonic helium

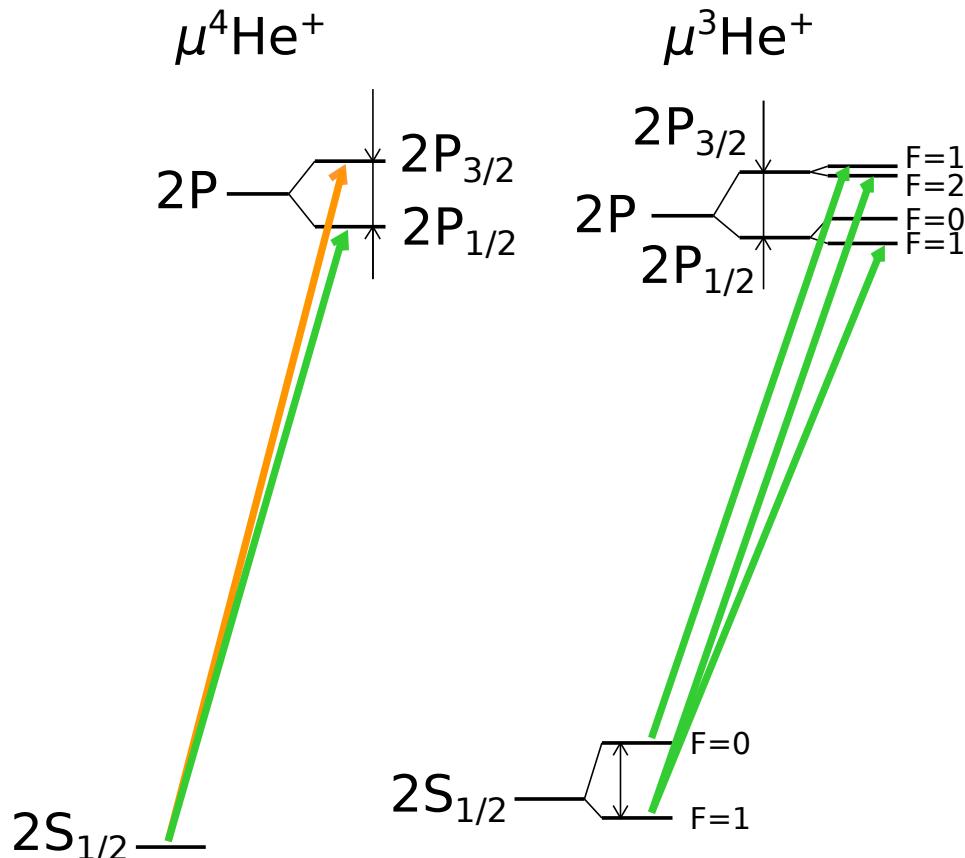
Measured transitions:



- Sept. 23 – Dec. 23, 2013

Lamb shift in muonic helium

Measured transitions:

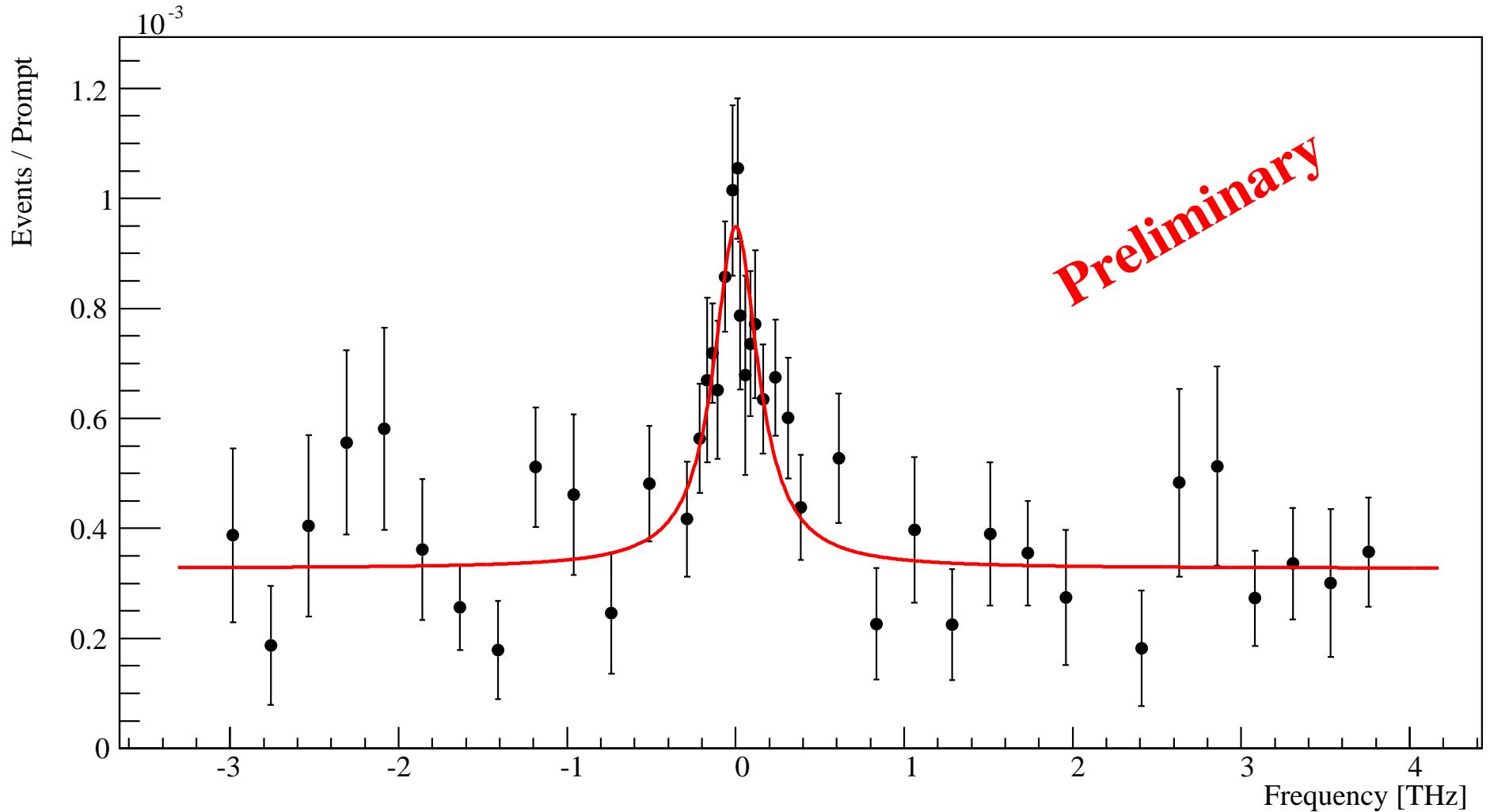


- Sept. 23 – Dec. 23, 2013
- May 15 – Aug. 6, 2014

SUCCESS!

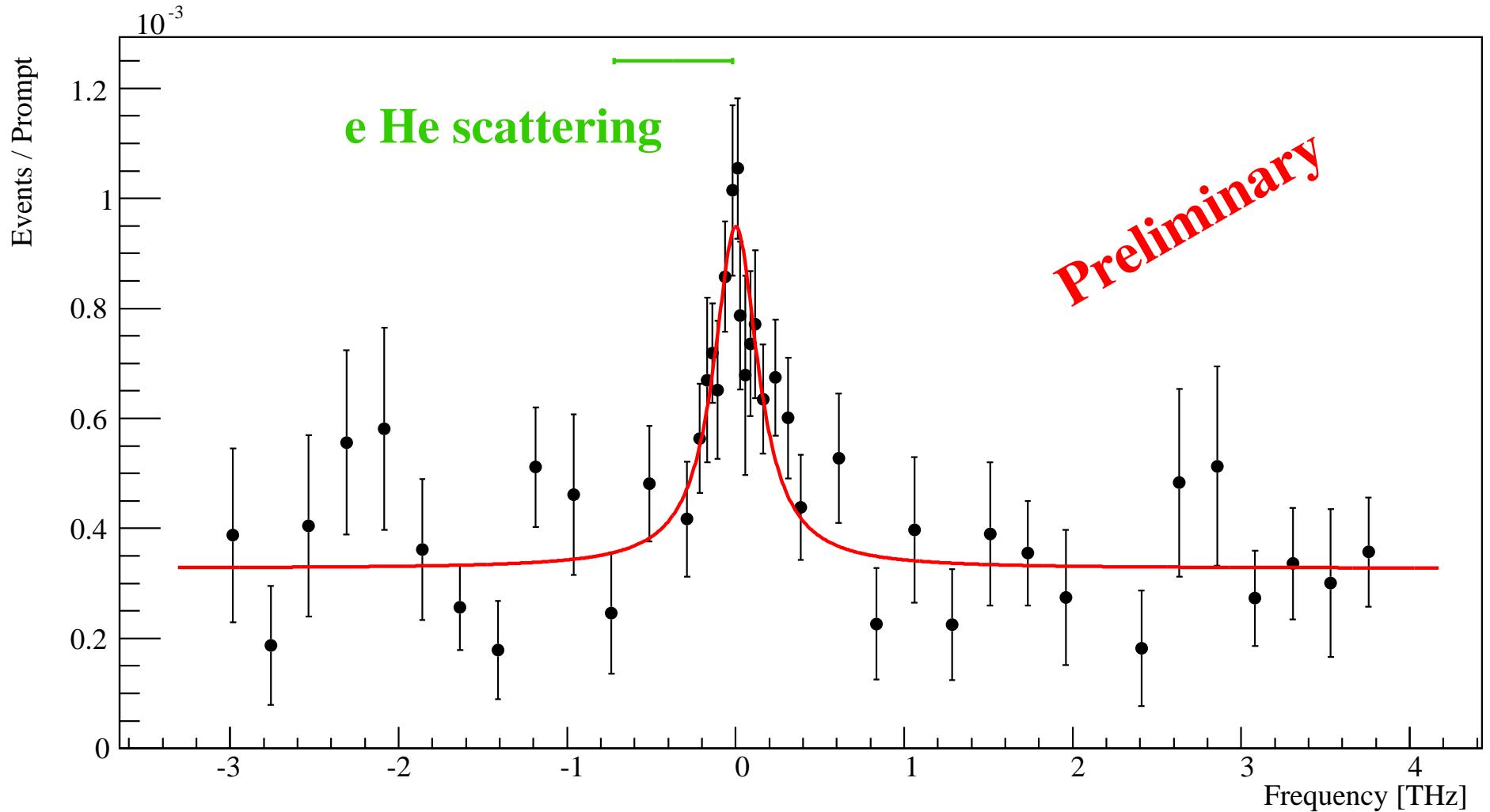
1st resonance in muonic He-4

$\mu^4\text{He}(2\text{S}_{1/2} \rightarrow 2\text{P}_{3/2})$ at $\sim 813\text{ nm}$ wavelength



1st resonance in muonic He-4

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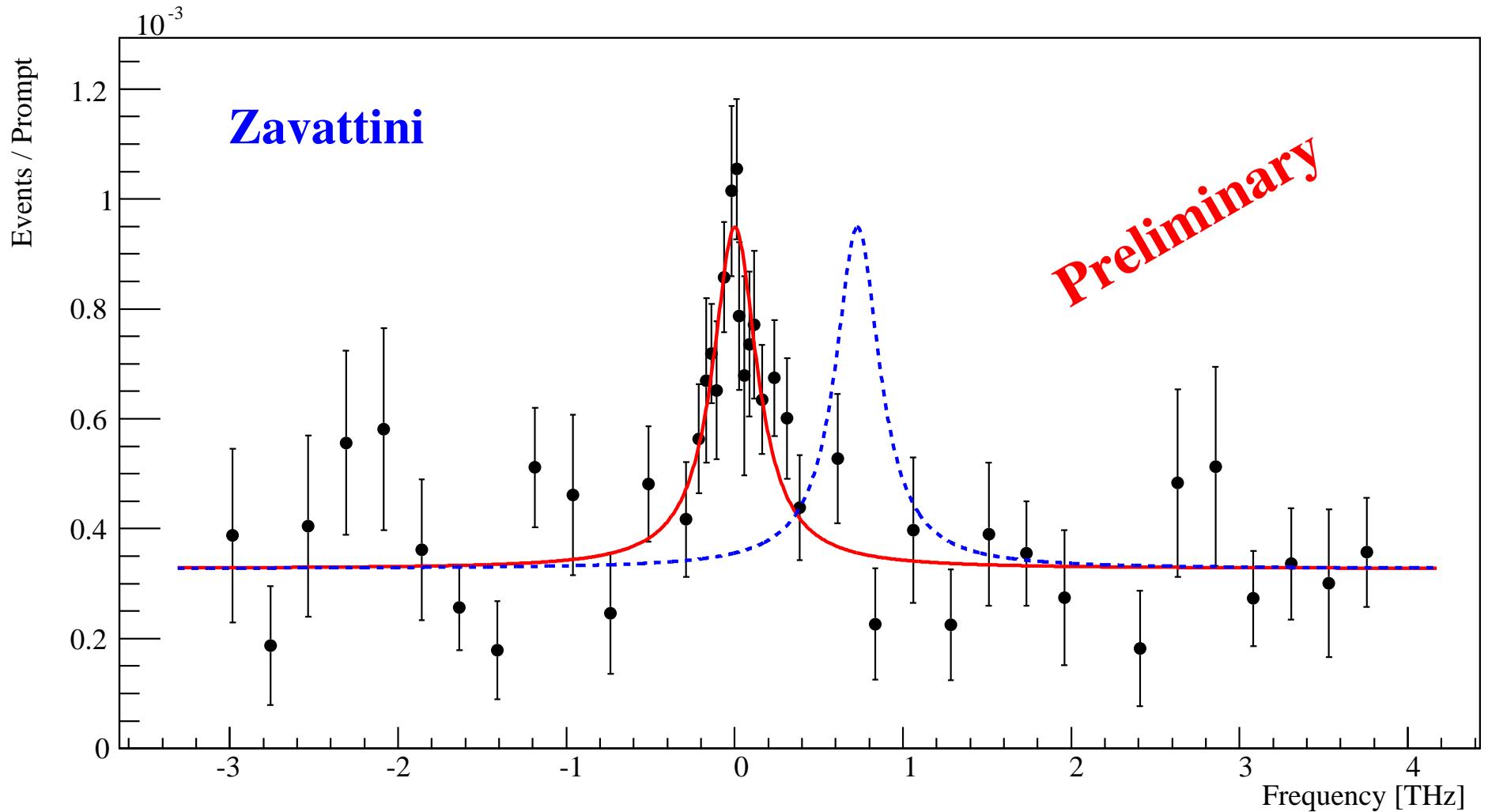


Sick, PRD 77, 040302(R) (2008)

Borie, Ann. Phys. 327, 733 (2012)

1st resonance in muonic He-4

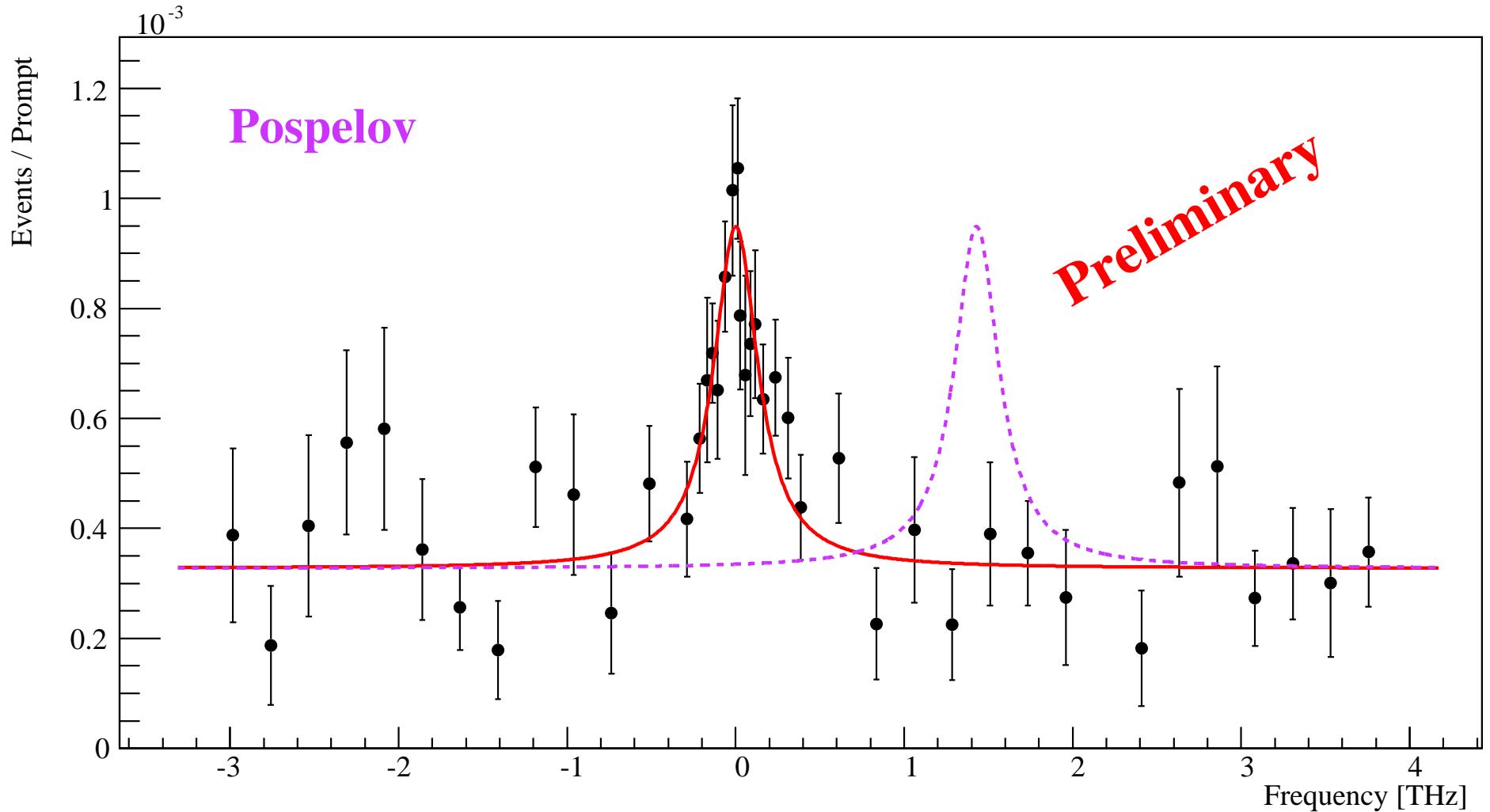
$\mu^4\text{He}(2\text{S}_{1/2} \rightarrow 2\text{P}_{3/2})$ at $\sim 813 \text{ nm}$ wavelength



Carboni et al, Nucl. Phys. A273, 381 (1977)

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Batell, McKeen, Pospelov, PRL 107, 011803 (2011)

Muonic summary



- Muonic hydrogen gives:
 - Proton charge radius: $r_p = 0.84087(39)$ fm
 7σ away from electronic average (CODATA: H, e-p scatt.)
 - Deuteron charge radius: $r_d = 2.12771(22)$ fm from $\mu H + H/D(1S-2S)$
- Muonic deuterium:
 - Deuteron charge radius: $r_d = 2.125XX(13)_{\text{exp}}(77)_{\text{theo}}$ fm (PRELIMINARY!)
consistent with muonic proton radius, but
again 7σ away from CODATA: 2.14240(210) fm
- “Proton” Radius Puzzle is in fact “Z=1 Radius Puzzle”
- muonic helium-3 and -4 ions: No big discrepancy (PRELIMINARY)

RP *et al.*, submitted (2016)

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- “Proton” Radius Puzzle is in fact “Z=1 Radius Puzzle”
- muonic helium-3 and -4 ions: No big discrepancy (PRELIMINARY)
- Could ALL be solved if the Rydberg constant [and hence the (electronic) proton radius] was wrong.
Plus $\sim 2.6\sigma$ change in deuteron polarizability.
Plus: accept dispersion fits of e-p scattering
- Or: BSM physics, e.g. Tucker-Smith & Yavin (2011)

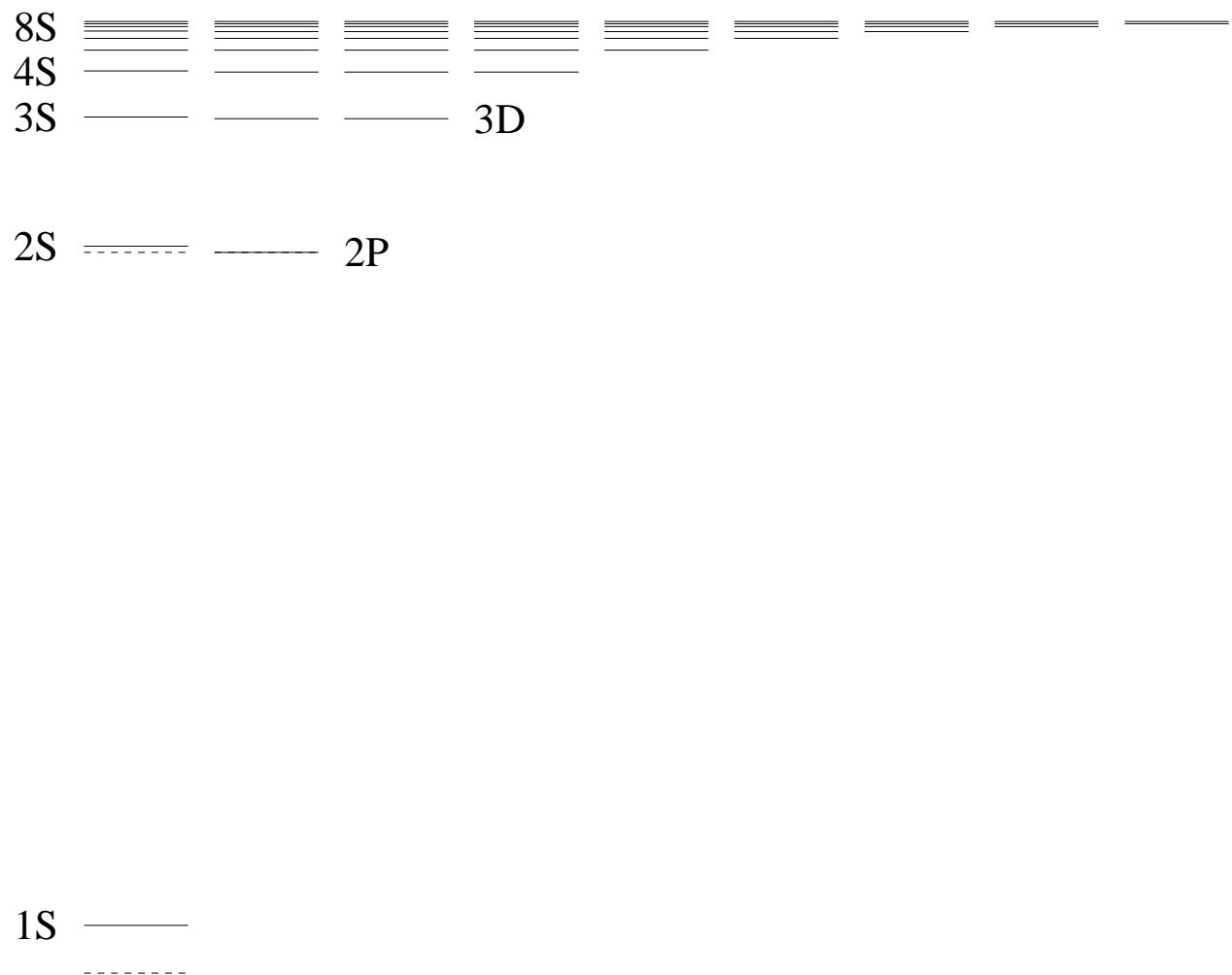
RP *et al.*, submitted (2016)

(Electronic) hydrogen.

Hydrogen spectroscopy

Lamb shift : $L_{1S}(r_p) = 8171.636(4) + 1.5645 \langle r_p^2 \rangle$ MHz

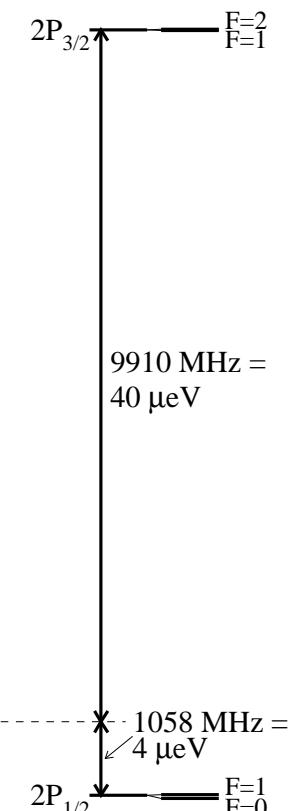
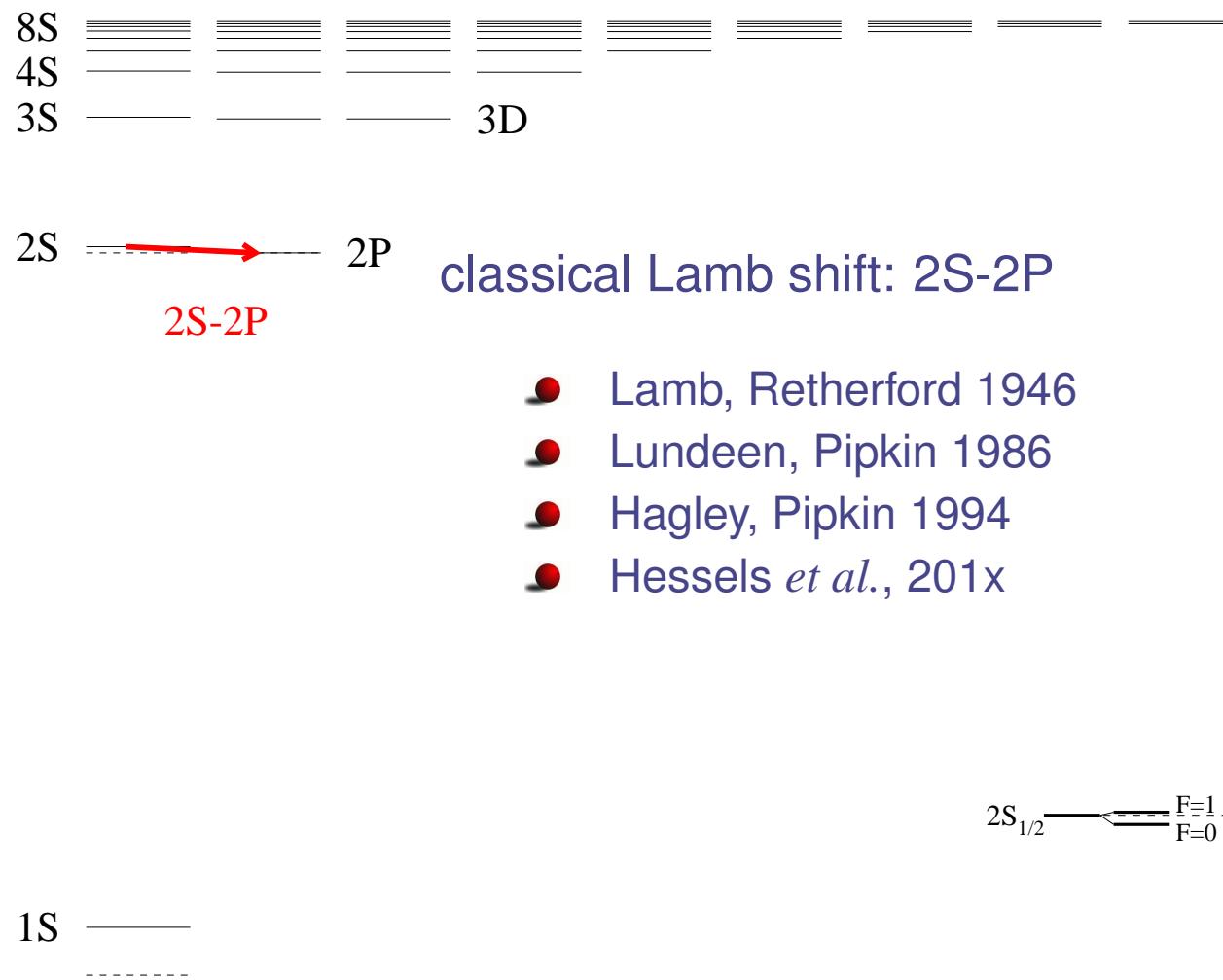
$$L_{nS} \simeq \frac{L_{1S}}{n^3}$$



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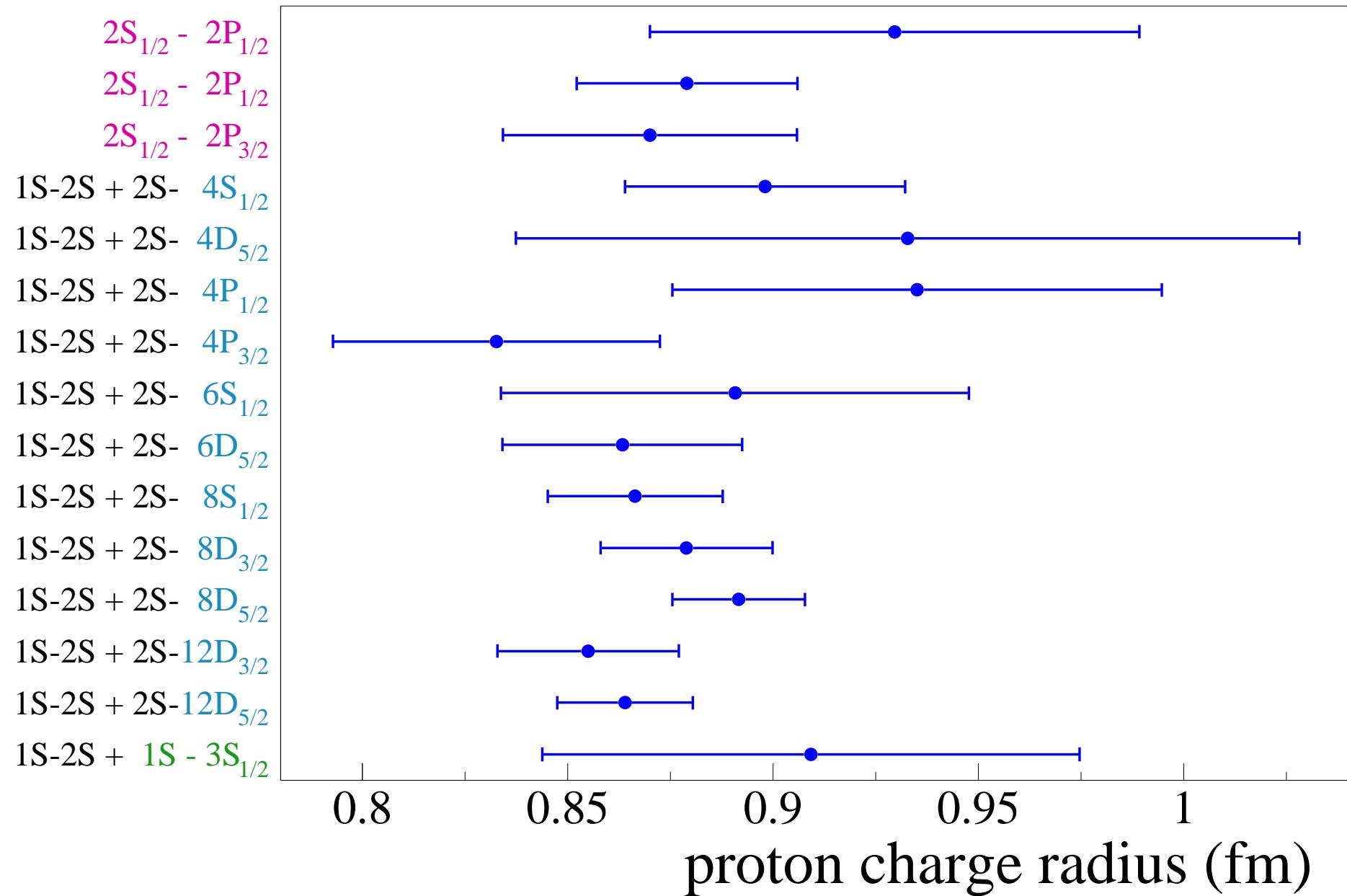


$$E_{nS} \simeq -\frac{R_\infty}{n^2} + \frac{L_{1S}}{n^3}$$

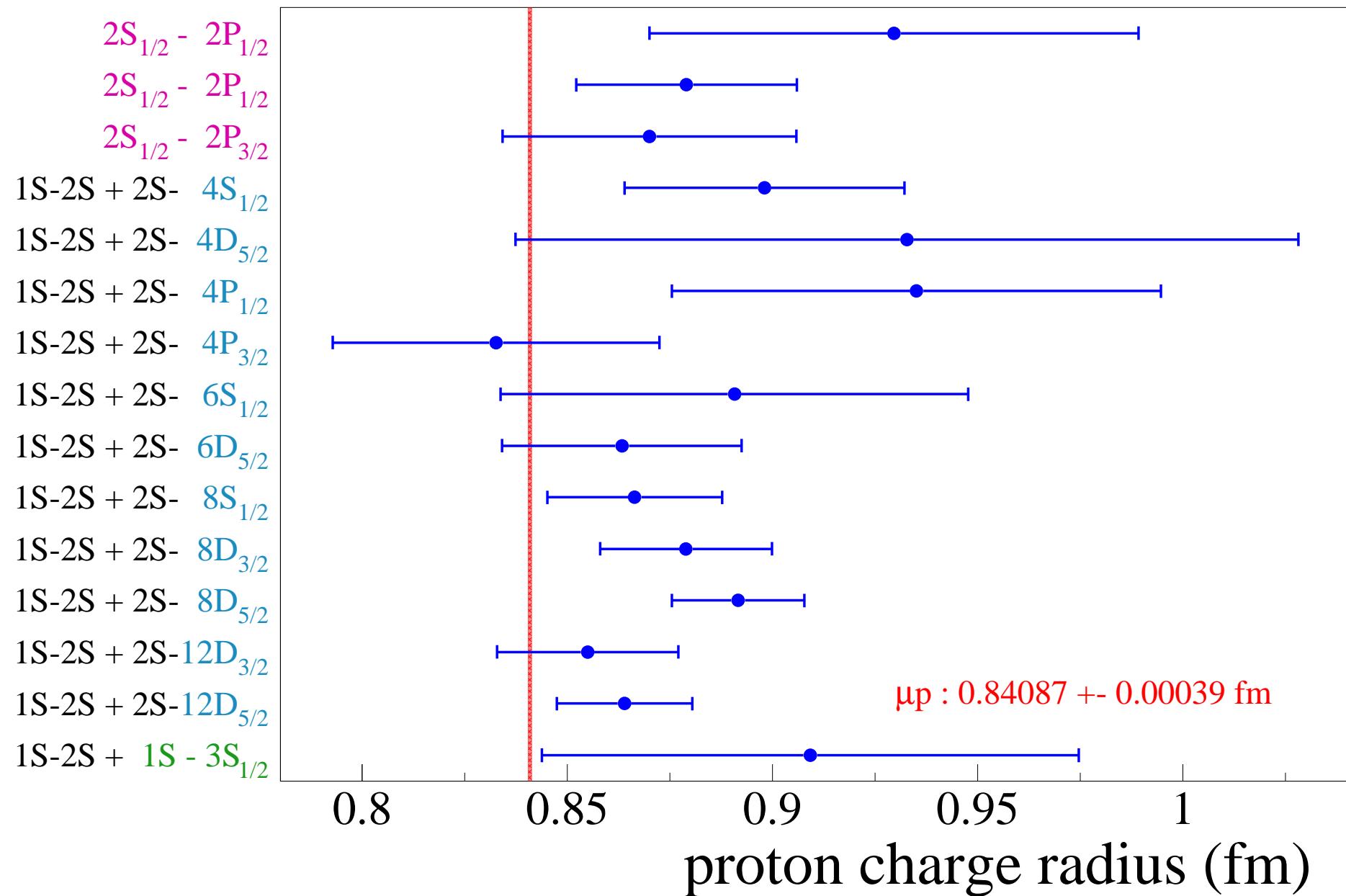
$1S-2S$ ↑ 2 unknowns \Rightarrow 2 transitions

- Rydberg constant R_∞
- Lamb shift $L_{1S} \leftarrow r_p$

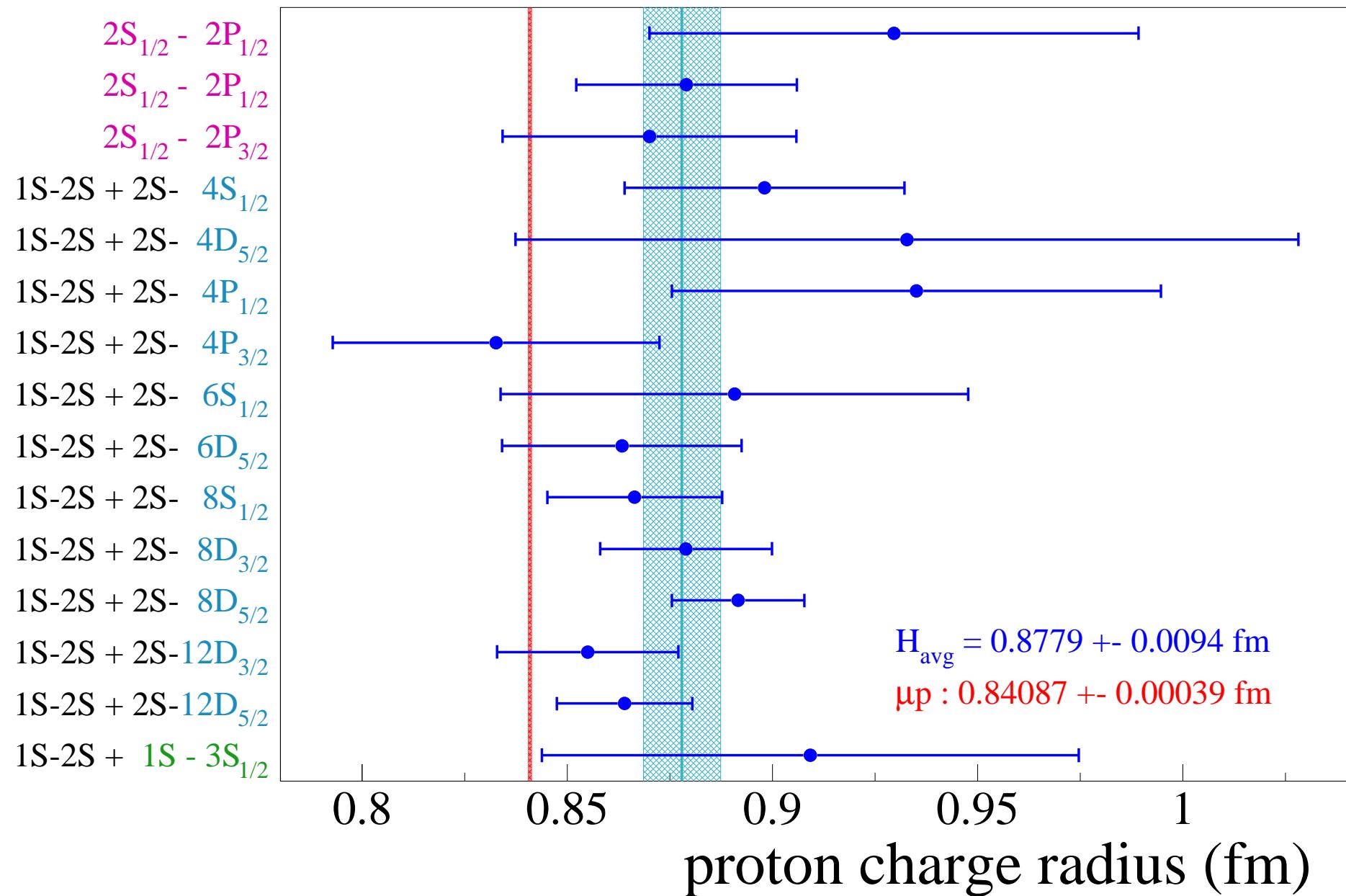
Hydrogen spectroscopy



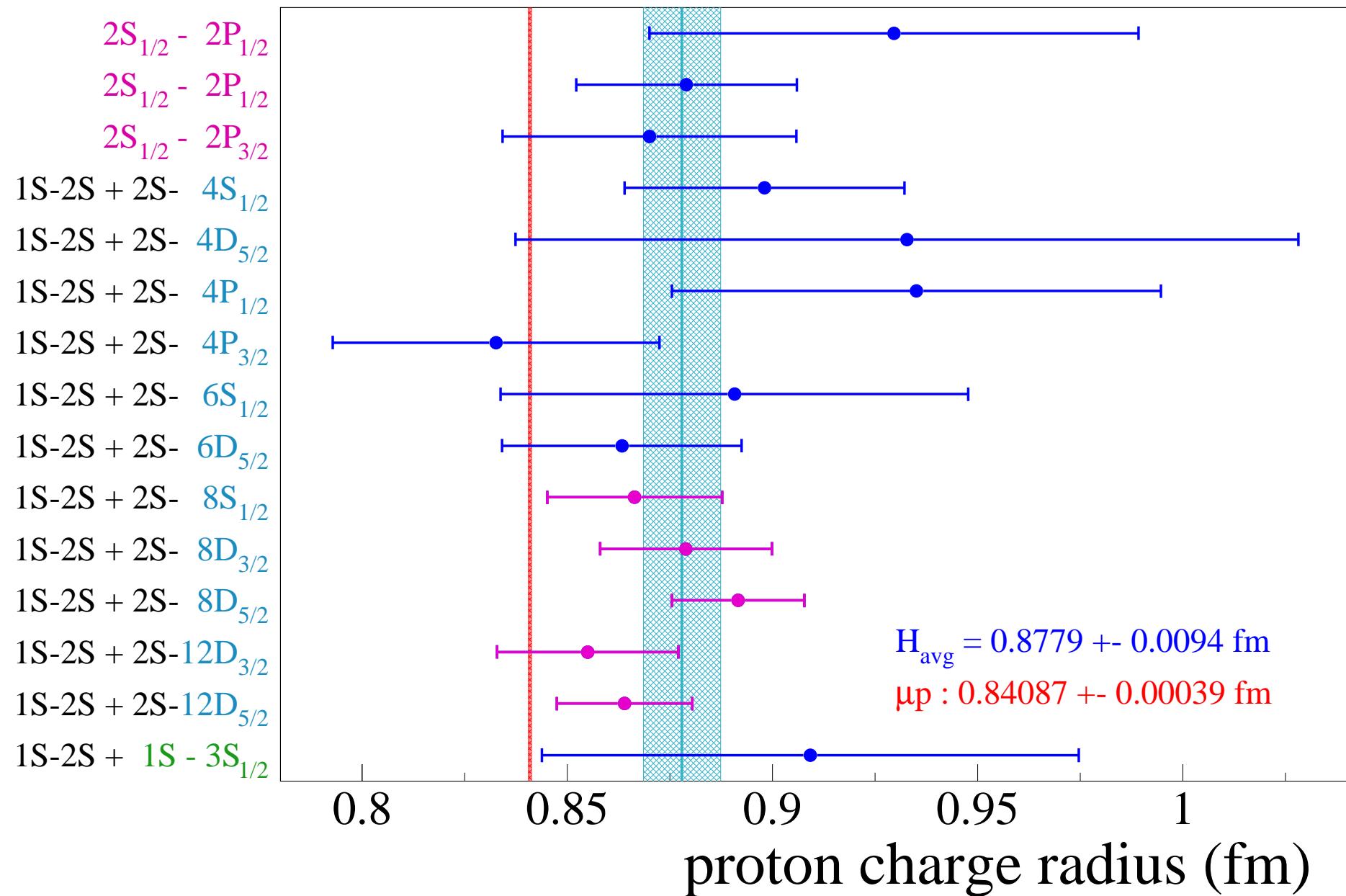
Hydrogen spectroscopy



Hydrogen spectroscopy

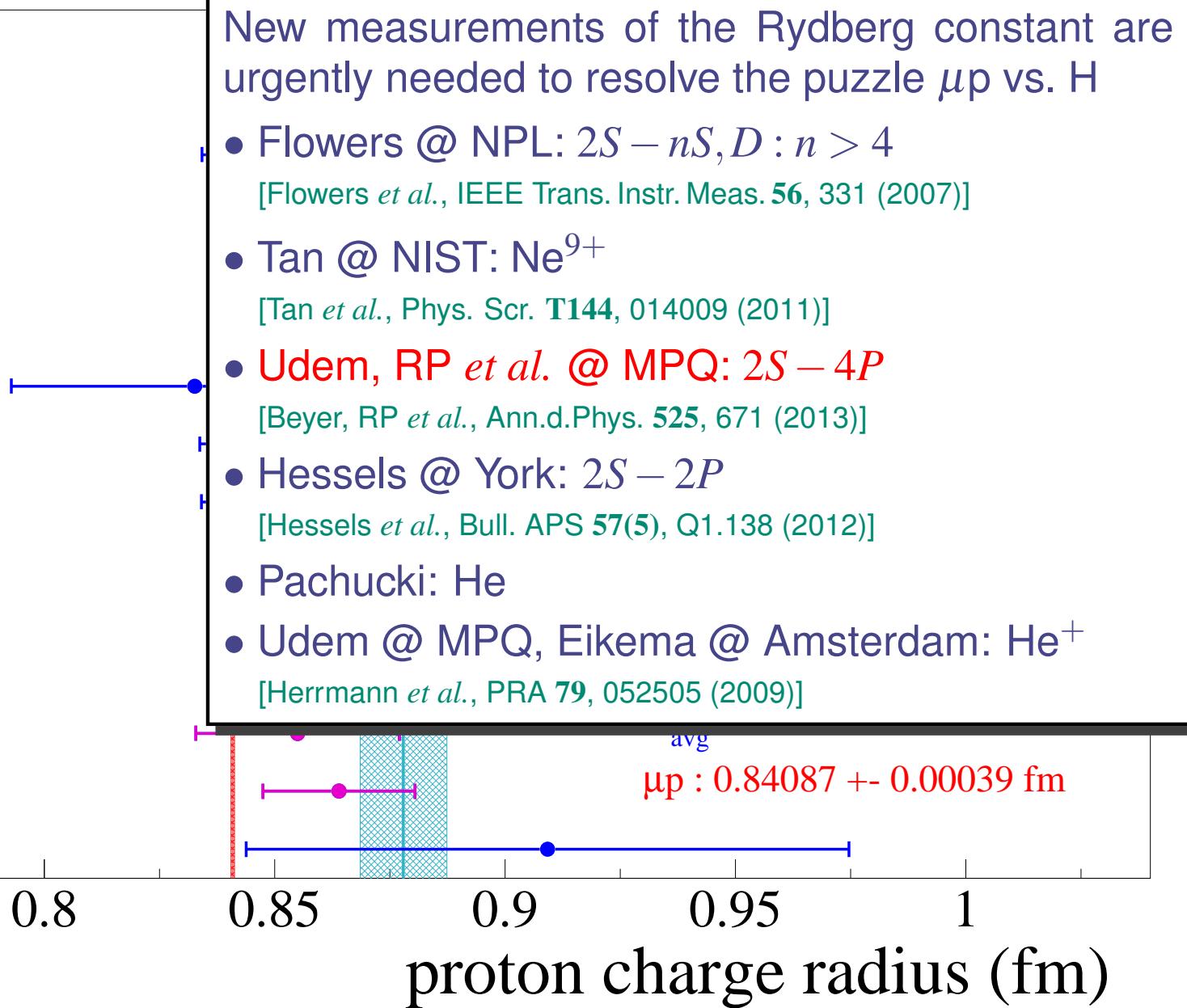


Hydrogen spectroscopy

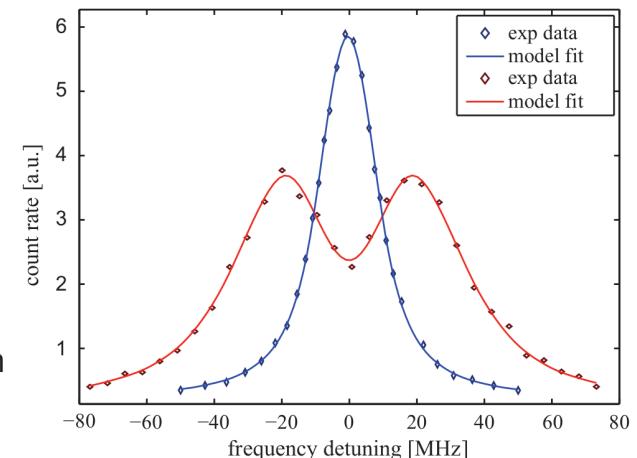
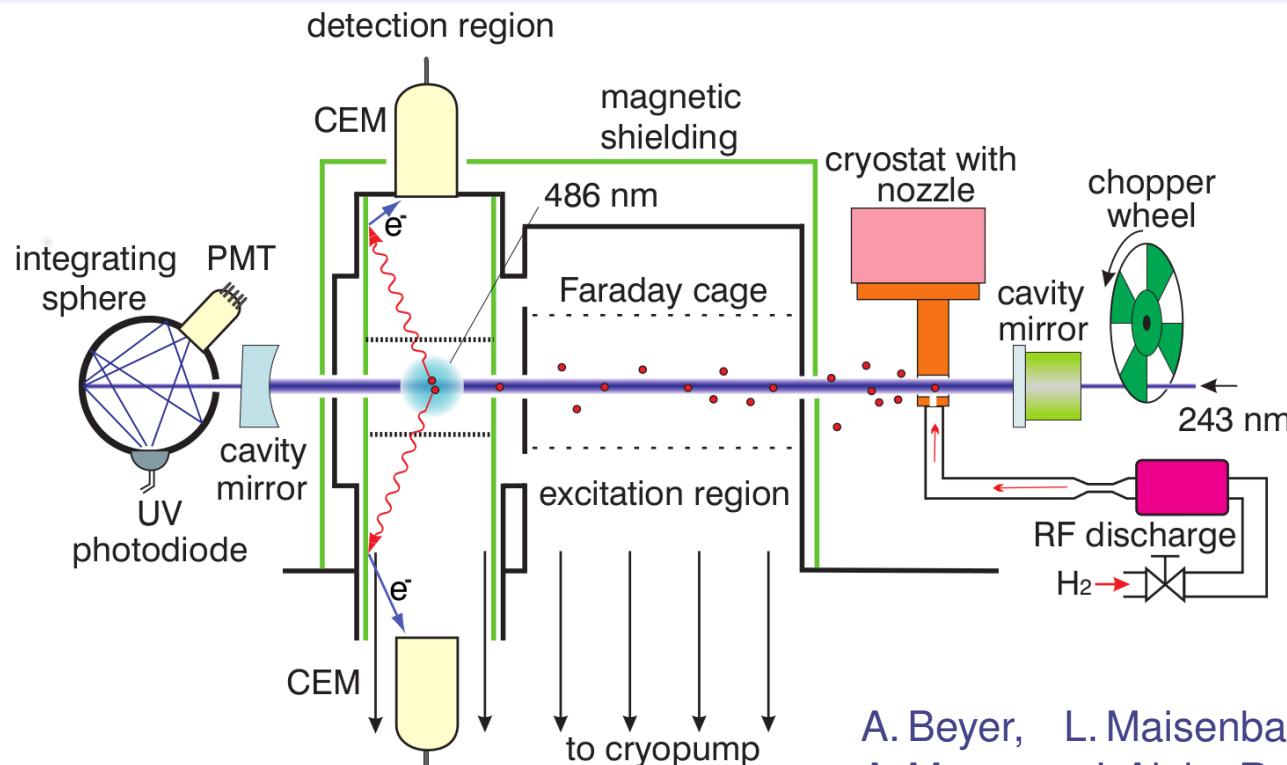


Hydrogen spectroscopy

$2S_{1/2} - 2P_{1/2}$
 $2S_{1/2} - 2P_{1/2}$
 $2S_{1/2} - 2P_{3/2}$
 $1S-2S + 2S- 4S_{1/2}$
 $1S-2S + 2S- 4D_{5/2}$
 $1S-2S + 2S- 4P_{1/2}$
 $1S-2S + 2S- 4P_{3/2}$
 $1S-2S + 2S- 6S_{1/2}$
 $1S-2S + 2S- 6D_{5/2}$
 $1S-2S + 2S- 8S_{1/2}$
 $1S-2S + 2S- 8D_{3/2}$
 $1S-2S + 2S- 8D_{5/2}$
 $1S-2S + 2S- 12D_{3/2}$
 $1S-2S + 2S- 12D_{5/2}$
 $1S-2S + 1S - 3S_{1/2}$



Rydberg constant from hydrogen

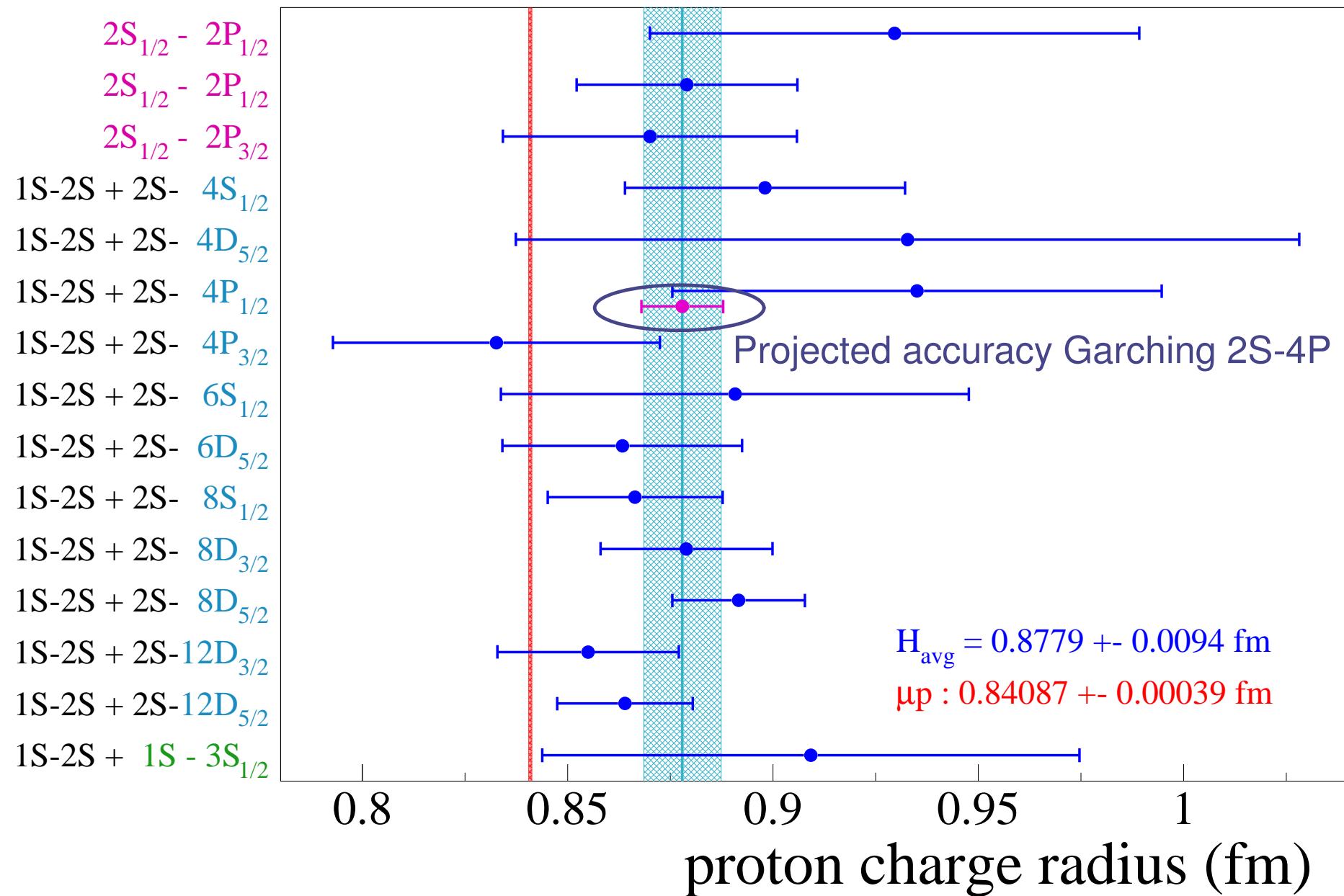


2S – 4P resonance at
 $88 \pm 0.5^\circ$ and $90 \pm 0.08^\circ$

A. Beyer, L. Maisenbacher, K. Khabarova, C.G. Parthey,
A. Matveev, J. Alnis, R. Pohl, N. Kolachevsky, Th. Udem and
T.W. Hänsch

- Apparatus used for H/D(1S-2S)
C.G. Parthey, RP *et al.*, PRL **104**, 233001 (2010)
C.G. Parthey, RP *et al.*, PRL **107**, 203001 (2011)
- 486 nm at 90° + Retroreflector \Rightarrow Doppler-free 2S-4P excitation
- 1st oder Doppler vs. ac-Stark shift
- ~ 2.5 kHz accuracy (vs. 15 kHz Yale, 1995)
- cryogenic H beam, optical excitation to 2S
A. Beyer, RP *et al.*, Ann. d. Phys. **525**, 671 (2013)

Hydrogen spectroscopy



Summary

- Muonic hydrogen gives:
 - Proton charge radius: $r_p = 0.84087(39)$ fm
 - Proton Zemach radius: $R_Z = 1.082(37)$ fm
 - Rydberg constant:

$$R_\infty = 3.289\,841\,960\,249\,5 (10)^{\text{radius}} (25)^{\text{QED}} \times 10^{15} \text{ Hz/c}$$
 - Deuteron charge radius: $r_d = 2.12771(22)$ fm from $\mu H + H/D(1S-2S)$
 - The “Proton radius puzzle”
- muonic deuterium: $r_d = 2.125XX(78)$ fm from μD (prel.!)
- muonic helium-3 and -4: charge radius 10x more precise.
- Proton radius puzzle deepened!
 New data needed:
 - Muonic T, He, Li, Be, ..
 - Hydrogen/Deuterium/Tritium, He^+
 - Positronium $\equiv e^+e^-$, Muonium $\equiv \mu^+e^-$
 - Electron scattering: H at lower Q^2 , D, He
 - Muon scattering: MUSE @ PSI
 - ...

CREMA in 2009...



Proton Size Investigators thank you for your attention



... and 2014



The cost for LHC



According to **Forbes** (Jul. 2012), the Higgs discovery cost

13.25 billion USD.

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Cost increase for Higgs discovery: 1.06 billion USD.

The cost for LHC



My apologies.

:-)