## Polarized τ and μ Lepton Flavor Violation in the Littlest Higgs Model with T-parity.

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#### Yasuhiro Yamamoto (Sokendai/KEK)

with T. Goto (KEK) and Y. Okada (KEK/Sokendai)

Based on arXiv:1012.4385[hep-ph]

## The Hierarchy Problem





# The Little Hierarchy Problem



The BEH doublet is embedded in a part of NG bosons.

$$\mathcal{L}_{\text{BEH}} = \mathcal{L}_{G/H} + \mathcal{L}_{G1} + \mathcal{L}_{G2}$$



'01 N.Arkani-Hamed, A.G.Cohen, H.Georgi

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 $\mathcal{L}_{\rm mass} = g_1 g_2 \langle O_1 O_2 \rangle H^{\dagger} H$ 

Quadratic divergences are suppressed at 1-loop.

<u>'01 N.Arkani-Hamed, A.G.Cohen, H.Georgi</u>



'02 N.Arkani-Hamed, A.G.Cohen, E.Katz, A.E.Nelson



✓ New particles and mixing matrices are introduced
 → Investigate flavor signals in LHT!

#### Flavor Changing Neutral Current (FCNC)

Don't exist at tree level in the SM



Contributions of new physics are relatively large.

✓ New physics is strongly constrained (c.f.  $K^{\circ}-\overline{K^{\circ}}$  mixing → 1 PeV).

Parity structure is good friend with loop induced proceses.

# Lepton Flavor Violation (LFV)



6

 $\checkmark$  Only new physics contribute to the processes.

✓ QCD contamination is suppressed.

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The number of silicon atom in the earth  $\sim \mathcal{O}(10^{53})$ 

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✓ QCD contamination is suppressed.

It difficult to study detail structure of models.



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# Work Done up to Now

Neutral meson mixings	'05 J.Hubisz, S.J.Lee, G.Paz
Various FCNC processes	'06~09 M.Blanke, A.J.Buras, C.Tarantino et al.
$K \to \pi \nu \nu$	'08 T.Goto, Y.Okada, Y.Y.
<u>μ-LFV</u>	'08,10 F.del Aguila, J.I.Illana, M.D.Jenkins

V Lepton flavor violating decays of polarized  $\tau$  and  $\mu$ .

V Nuclide dependence of  $\mu$ - e conversion.

" $\tau$  and  $\mu$  lepton flavor violation in the littlest Higgs model with T-parity", arXiv: 1012.4385, T. Goto, Y. Okada, Y.Y.

# Contents

The Littlest Higgs Model with T-parity Symmetry, particle contents and new flavor mixing.

 Lepton Flavor Violation and Asymmetry Current status and asymmetries of LFV.

✓ Numerical Results

Correlations among branching ratios and asymmetries.

✓Conclusion

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Global Symmetry of the LHT



Gauge Symmetry of the LHT

$$SU(5) \supset [SU(2) \times U(1)]_{1} \times [SU(2) \times U(1)]_{2} \\ \bigstar \\ SO(5) \supset SU(2)_{L} \times U(1)_{Y} \\ \mathcal{L}_{gauge} = \sum_{i=1,2} -\frac{1}{4} (W_{i\mu\nu}^{a} W_{i}^{a\mu\nu} + B_{i\mu\nu} B_{i}^{\mu\nu}) \quad \text{T-parity} : 1 \Leftrightarrow 2 \\ Q_{1}^{a} = \frac{1}{2} \begin{pmatrix} \sigma^{a} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \qquad Q_{2}^{a} = \frac{1}{2} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & -\sigma^{a*} \end{pmatrix}, \\ Y_{1} = \frac{1}{10} \text{diag}(3, 3, -2, -2, -2), \quad Y_{2} = \frac{1}{10} \text{diag}(2, 2, 2, -3, -3) \\ W_{L, H} = \frac{W_{1} \pm W_{2}}{\sqrt{2}} \longrightarrow M_{WH, ZH} = fg \left(1 - \frac{v^{2}}{8f^{2}}\right) \\ M_{AH} = \frac{fg'}{\sqrt{5}} \left(1 - \frac{5v^{2}}{8f^{2}}\right) \\ \end{cases}$$

Gauge Symmetry of the LHT

$$\begin{split} & \text{SU}(5) \ \supseteq \left[ \begin{array}{c} \text{SU}(2) \times \text{U}(1) \right]_{1} \times [\text{SU}(2) \times \text{U}(1)]_{2} \\ & \bigstar \\ & \text{SO}(5) \ \supseteq \left[ \begin{array}{c} \text{SU}(2) \times \text{U}(1) \right]_{1} \times [\text{SU}(2) \times \text{U}(1)]_{2} \\ & \swarrow \\ & \text{SU}(2)_{L} \times \text{U}(1)_{Y} \end{array} \right] \\ \mathcal{L}_{\text{gauge}} &= \sum_{i=1,2} -\frac{1}{4} (W_{i\mu\nu}^{a} W_{i}^{a\mu\nu} + B_{i\mu\nu} B_{i}^{\mu\nu}) \quad \text{T-parity} : 1 \div 2 \\ & Q_{1}^{a} = \frac{1}{2} \begin{pmatrix} \sigma^{a} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \qquad Q_{2}^{a} = \frac{1}{2} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & -\sigma^{a*} \end{pmatrix}, \\ & Y_{1} &= \frac{1}{10} \text{diag}(3, 3, -2, -2, -2), \quad Y_{2} &= \frac{1}{10} \text{diag}(2, 2, 2, -3, -3) \\ & \xi &= \exp \left[ \begin{array}{c} i \\ f \end{pmatrix} \begin{pmatrix} \omega & H & \Phi \\ H^{\dagger} & \eta & H^{T} \\ & \Phi^{\dagger} & H^{*} \end{pmatrix} \right] \\ & \text{Physical Scalar} \\ & \text{SM BEH doublet} \\ & \text{Eaten by} \\ & \text{heavy gauge bosons} \\ \end{array}$$

Fermions in the LHT  

$$\frac{\mathcal{L}_{L} = \bar{\Psi}_{1}iD\Psi_{1} + \bar{\Psi}_{2}iD\Psi_{2}}{\Psi_{1} = (L_{1}, 0, 0_{2}), \Psi_{2} = (0_{2}, 0, L_{2}) \quad (L_{i} = (-\ell_{i}, \nu_{i}))}$$

$$\Rightarrow L_{\pm} = \frac{L_{1} \mp L_{2}}{\sqrt{2}}$$

$$\frac{\mathcal{L}_{HR} = \bar{\Psi}_{R}\xi^{\dagger}(i\partial - gA)\xi\Psi_{R}}{\Psi_{R} = (L_{HR}, \chi_{R}, \psi_{R}) \quad (L_{HR} = (-\ell_{HR}, \nu_{HR}))}$$

$$\Rightarrow \xi \mapsto U\xiV^{\dagger}, \Psi_{R} \mapsto V\Psi_{R} \quad (U \in SU(5), V \in SO(5))$$

$$\Rightarrow \frac{\mathcal{L}_{HY} = -\kappa_{ij}f(\bar{\Psi}_{2}^{i}\xi + \bar{\Psi}_{1}^{i}\Sigma_{0}\Omega\xi^{\dagger}\Omega)\Psi_{R}^{j} + H.c.}{m_{Hi}^{\nu} = \sqrt{2}\kappa_{i}f\left(1 - \frac{v^{2}}{8f^{2}}\right), m_{Hi}^{\ell} = \sqrt{2}\kappa_{i}f$$





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 $\mu$  -LFV

 $\bigvee \mathrm{Br}(\mu^+ \to e^+ \gamma) \leq 1.2 \times 10^{-11} \text{ by MEGA}$  $\mathrm{MEG}(@\mathrm{PSI}) \text{ is in progress: } 1.5 \times 10^{-11} \to 10^{-13}$ 

$$\checkmark \mathrm{Br}(\mu^+ \to e^+ e^+ e^-) \le 1.0 \times 10^{-12} \text{ by SINDRUM}$$

$$\sqrt{\mathbf{R}(\mu^{-}A \to e^{-}A)} \leq \begin{cases} 4.3 \times 10^{-12} \text{ (Ti)} \\ 0.7 \times 10^{-12} \text{ (Au)} & \text{by SINDRUM II} \\ 4.6 \times 10^{-11} \text{ (Pb)} \end{cases}$$

COMET(@J-PARC) and mu2e(@FNAL) are planned:  $\rightarrow 10^{-16}~{\rm with~Al}$ 



τ-LFV

$$\checkmark \tau^+ \to \ell^+ \gamma \lesssim \mathcal{O}(10^{-8})$$

$$\checkmark \tau^+ \to \mu^+ \mu^+ \mu^-, \ \tau^+ \to \mu^+ e^+ e^-, \ \tau^+ \to \mu^+ \mu^+ e^- \lesssim \mathcal{O}(10^{-8})$$

$$\checkmark \tau^+ \to \ell^+ \pi^0, \, \eta \operatorname{or} \eta', \, \tau^+ \to \ell^+ \rho^0, \, \omega \operatorname{or} \phi \lesssim \mathcal{O}(10^{-8})$$

by Belle @ KEK and BaBar @ SLAC

Belle II(@KEK) and SuperB(@INFN) are planned  $\tau \rightarrow 3 \mu$  and  $\tau \rightarrow 1 \phi$  can be tested in LHC  $\rightarrow 10^{-9}$ 

# Asymmetry for 2 Body Decays 16 $\ell \to \ell' \gamma, \ \tau \to \ell P, \ \tau \to \ell V$ $\mathcal{L}_{\gamma} = -\frac{4G_{\rm F}}{\sqrt{2}} \left[ m_a A_{\rm R} \bar{\ell}_{a\rm R} \sigma^{\mu\nu} \ell_{b\rm L} F_{\mu\nu} + m_a A_{\rm L} \bar{\ell}_{a\rm L} \sigma^{\mu\nu} \ell_{b\rm R} F_{\mu\nu} \right],$ $\stackrel{\text{d}\Gamma}{=} \frac{\mathrm{d}\Gamma}{\mathrm{d}\cos\theta} \propto |A_{\mathrm{L}}|^2 (1+\cos\theta) + |A_{\mathrm{R}}|^2 (1-\cos\theta),$ $\operatorname{Br}(\ell \to \ell' \gamma) \propto |A_{\rm L}|^2 + |A_{\rm R}|^2$ $A_{\gamma} = \frac{1}{2} \frac{|A_{\rm L}|^2 - |A_{\rm R}|^2}{|A_{\rm L}|^2 + |A_{\rm R}|^2}$ Parity asymmetry



'00 Y.Okada, K.Okumura, Y.Shimizu



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 $\hat{z} : \cos \theta \sim \vec{s} \cdot \vec{p}_a$  $\hat{x} : \sin \theta \cos \phi \sim \vec{s} \cdot ((\vec{p}_a \times \vec{p}_b) \times \vec{p}_a)$  $\hat{y} : \sin \theta \sin \phi \sim \vec{s} \cdot (\vec{p}_a \times \vec{p}_b)$ 

'00 Y.Okada, K.Okumura, Y.Shimizu







# **Chirality Structure**

Only the left handed SM leptons interact with the T-odd leptons



$$\mathcal{L}_{\rm LHT} = -\frac{4G_F}{\sqrt{2}} \left[ m_{\tau} \underline{A_{\rm R}} \bar{\tau}_{\rm R} \sigma^{\mu\nu} \mu_{\rm L} F_{\mu\nu} + \underline{g_{\rm Ll}} (\tau_{\rm L} \gamma^{\mu} \mu_{\rm L}) (\mu_{\rm L} \gamma_{\mu} \mu_{\rm L}) \right. \\ \left. + \underline{g_{\rm Lr}} (\tau_{\rm L} \gamma^{\mu} \mu_{\rm L}) (\mu_{\rm R} \gamma_{\mu} \mu_{\rm R}) + \text{H.c.} \right]$$

Some asymmetries are independent of the Wilson coefficients.

$$A_{\gamma}(\ell \to \ell'\gamma) = -\frac{1}{2}, \quad A_{P}(\tau \to \ell P) = \frac{1}{2},$$
$$A_{X}(\tau^{+} \to \mu^{+}\mu^{+}e^{-}) = 0, \quad A_{Z}(\tau^{+} \to \mu^{+}\mu^{+}e^{-}) = -\frac{1}{2},$$
$$A_{X}(\tau^{+} \to \mu^{+}e^{+}e^{-}) : A_{FB} : A_{Z,FB} = -\frac{4\pi}{35} : -\frac{1}{4} : \frac{1}{8}.$$

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#### Parameters

There are 19 relevant parameters.

✓ Decay Constant (1): f = 500 GeV

✓ Masses of T-odd leptons and quarks (6):  $m_{H\ell}^i$ ,  $m_{Hq}^i$ 100 GeV ≤  $m_{H\ell}^i$  ≤ 1 TeV,  $m_{Hq}^i$  = 500 GeV

 $\checkmark \text{New mixing angles and phases (12): } \theta^\ell_{ij}, \, \phi^\ell_{ij}, \, \theta^q_{ij}, \, \phi^q_{ij}, \, \phi^q_{ij},$ 

Scatter plots on 7 parameters.

Br( $\mu \rightarrow e \gamma$ )<10<sup>-13</sup><Br( $\mu \rightarrow e \gamma$ )<10<sup>-12</sup><Br( $\mu \rightarrow e \gamma$ )<1.2x10<sup>-11</sup>

## Branching Ratios of $\mu$ LFV



'<u>07 M.Blanke, A.J.Buras, B.Duling, A.Poschenrieder, C.Tarantino</u> '<u>08 F.del Aguila, J.I.Illana, M.D.Jenkins</u>

✓ Dipole dominant signal is not favored in  $\mu \rightarrow e \gamma$  vs  $\mu \rightarrow 3e$ . ✓  $\mu \rightarrow e \gamma$  is independent of  $\mu$ -e conversion.

#### $\mu$ - e Conversion



 $\checkmark$   $\mu$ -e conversion should be test with various atoms.

## Branching Ratios of $\tau$ LFV



'07 M.Blanke, A.J.Buras, B.Duling, A.Poschenrieder, C.Tarantino

V Dipole dominant signals are not favored.

## Parity Asymmetry



Large parity asymmetries are allowed.

#### **Time Reversal Asymmetry**



V Large time reversal asymmetry is allowed in  $\mu$ -LFV.

#### **Proportional Relation**



## **Vector Meson Emission**



 $\checkmark$  Parity asymmetries are positive if we can measure them.



#### Conclusion

# Model x Process

## Conclusion





